AUTOMATIC CHANGE DETECTION IN RAPIDEYE DATA USING THE COMBINED MAD AND KERNEL MAF METHODS

Allan A. Nielsen^a, Antje Hecheltjen^b, Frank Thonfeld^b and Morton J. Canty^c

 ^aTechnical University of Denmark, DTU Space – National Space Institute DK-2800 Kgs. Lyngby, Denmark
^bUniversity of Bonn, Center for Remote Sensing of Land Surfaces (ZFL) D-53113 Bonn, Germany
^cResearch Center Jülich, Institute of Chemistry and Dynamics of the Geosphere D-52425 Jülich, Germany

1. INTRODUCTION

Based on orthorectified, bi-temporal $2,000 \times 2,0005$ m pixel multispectral RapidEye data [1] short-term changes are detected associated with land-use and reclamation in connection with open pit mining in North Rhine-Westphalia, Germany. The changes are found automatically by means of a combination of the iteratively re-weighted MAD method [2], which produces a generalized multivariate difference image, and the kernel MAF method [3]. The IR-MAD method may also be used for automatic radiometric normalization of the data [4]. For the acquisition of ground data for orthorectification and for accuracy assessment, GPS data, supplied by courtesy of RWE Power AG [5], are used.

2. DATA AND PREPROCESSING

The study site is located west of Cologne and comprises the Rhenish lignite district, the largest open-cast mining site in Germany. With an annual excavation of 300 million cubic meters (Hambach), 140 million (Garzweiler) and 80 million cubic meters (Inden), respectively, and a total lignite extraction of about 100 million metric tons per year [5], this area is highly dynamic and fast changing. The open-cast mining sites are surrounded predominantly by agricultural areas and some forested areas around the Hambach site.

Two RapidEye images acquired on 24 May and 1 June 2009 were selected to perform the IR-MAD analysis for change detection purposes. The subsets used here cover a region of $2,000 \times 2,000$ pixels centered on the Garzweiler site, see Figure 1, where the most accurate GPS data were available for orthorectification. RapidEye is a constellation of five identical satellites operating in the same sun-synchronous orbit. Each of them has five spectral bands which cover the blue (440-510 nm), the green (520-590 nm), the red (630-685

nm), the red edge (690-730 nm), and the near infrared region (760-850 nm). Ground sampling distance is 6.5 m. Due to its off-nadir capabilities RapidEye is in principle able to achieve daily coverage [6].

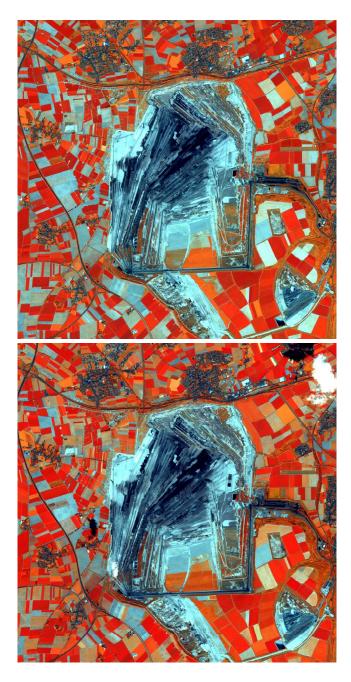
The imagery was delivered as level 1B basic product, which means that only radiometric and sensor corrections have been applied [6]. Orthorectification was performed with PCI's [7] Geomatica 10.3 OrthoEngine Module using the rational function option [8, 9] and a 10 m digital elevation model. An updated digital elevation model was created for each acquisition time by merging the 10 m base digital elevation model with the real time digital elevation model that was derived from the excavators GPS ground measurements. DEM resolution was 2 m. To achieve best performance the RapidEye data were converted to 5 m pixel spacing with cubic convolution interpolation as is done for the RapidEye level 3A ortho standard products [6]. The data are quantized to 16 bit.

Note the clouds (and their shadows) in the northeast corner of the image and in the southwest corner of the mine, Figure 1 bottom.

3. THE ITERATED MAD TRANSFORMATION

Change over time between the two RapidEye images is here detected by means of the iteratively reweighted multivariate alteration detection (IR-MAD) method followed by postprocessing by means of kernel maximum autocorrelation factor (kMAF) analysis. The IR-MAD method builds on an iterated version of an established method in multivariate statistics, namely canonical correlation analysis (CCA) [10]. It finds orthogonal (i.e., uncorrelated) linear combinations of the multivariate data at two time points that have maximal correlation. These linear combinations are called the canonical variates (CV) and the corresponding correlations are called the canonical correlations. There is one set of CVs for each time point. The difference between the two sets of

AAN's e-mail address is aa@space.dtu.dk and his homepage is http://www.imm.dtu.dk/ \sim aa.



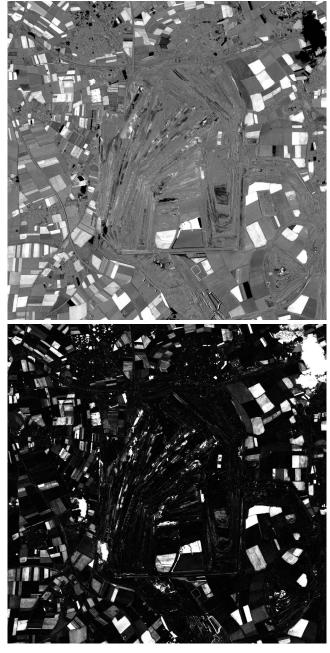


Fig. 1. Orthorectified RapidEye $2,000 \times 2,000$ 5 m pixels subsets, infrared/red edge/red as RGB, 24 May 2009 (top), 1 June 2009 (bottom). Includes material © (2009) RapidEye AG, Germany. All rights reserved.

CVs represent the change between the two time points and are called the MAD variates or the MADs for short. The MAD variates are invariant to linear and affine transformations of the original data.

The sum of the squared MAD variates (properly normed

Fig. 2. IR-MAD component 5 (top), χ^2 image (bottom).

to unit variance) gives us a change variable that will ideally follow a so-called χ^2 (chi-squared) distribution with p degrees of freedom for the no-change pixels; p is the number of spectral bands in the image data, here p = 5. The χ^2 image is the basis for calculating an image of probability for no-change, i.e., the probability for finding a higher value of the χ^2 statistic than the one actually found. This image is the weight image in the iteration scheme mentioned above. Itera-

tions stop when the canonical correlations stop changing.

Figure 2 shows the iterated MAD component corresponding to the difference between the highest correlated iterated canonical variates (top) and the χ^2 image (bottom). Gray pixels in the top image are no change pixels, bright and dark pixels are change pixels. The gray level in the bottom image reflects the probability of change: bright pixels are change pixels, dark pixels are no-change pixels.

4. THE KERNEL MAF TRANSFORMATION

A kernel formulation of principal component analysis (PCA) [11] may be obtained from Q-mode or dual formulation of the problem combined with kernel substitution also known as the kernel trick [12, 13].

In maximum autocorrelation factor (MAF) analysis [14, 15] we maximize the autocorrelation of linear combinations, $a^T x(r)$, of zero-mean original (spatial) variables, x(r). x(r) is a multivariate observation at location r and $x(r + \Delta)$ is an observation of the same variables at location $r + \Delta$; Δ is a spatial displacement vector.

4.1. R-mode Formulation

The autocovariance R of a linear combination $a^T x(r)$ of zero-mean x(r) is

$$R = \operatorname{Cov}\{a^T x(r), a^T x(r + \Delta)\}$$
(1)

$$= a^T \operatorname{Cov}\{x(r), x(r+\Delta)\}a$$
(2)

$$= a^T C_{\Delta} a \tag{3}$$

where C_{Δ} is the covariance between x(r) and $x(r + \Delta)$. Assuming or imposing second order stationarity of x(r), C_{Δ} is independent of location, r. Introduce the multivariate difference $x_{\Delta}(r) = x(r) - x(r + \Delta)$ with variance-covariance matrix $S_{\Delta} = 2 S - (C_{\Delta} + C_{\Delta}^T)$ where S is the variance-covariance matrix of x. Since

$$a^T C_{\Delta} a = (a^T C_{\Delta} a)^T \tag{4}$$

$$= a^T C_{\Delta}^T a \tag{5}$$

$$= a^T (C_\Delta + C_\Delta^T) a/2 \tag{6}$$

we obtain

$$R = a^T (S - S_\Delta/2)a. \tag{7}$$

To get the autocorrelation ρ of the linear combination we divide the covariance by its variance $a^T S a$

$$\rho = 1 - \frac{1}{2} \frac{a^T S_{\Delta} a}{a^T S a} \tag{8}$$

$$= 1 - \frac{1}{2} \frac{a^T X_{\Delta}^T X_{\Delta} a}{a^T X^T X a} \tag{9}$$

where X is the n by p data matrix with columns x_i^T and X_{Δ} is a similarly defined matrix for x_{Δ} with zero-mean columns.

 C_{Δ} above equals $X^T X_{\Delta}/(n-1)$. To maximize ρ we must minimize the Rayleigh coefficient $a^T X_{\Delta}^T X_{\Delta} a/(a^T X^T X a)$ or maximize its inverse. This is done by solving a symmetric generalized eigenvalue problem.

Unlike linear PCA, the result from linear MAF analysis is scale invariant: if x_i is replaced by some matrix transformation Tx_i the result of the MAF transformation is the same.

4.2. Q-mode Formulation and Kernelization

Q-mode formulation of kernel principal component analysis turns out to amount to the re-parameterization $a \propto X^T b$, [12, 13].

As with kernel PCA we use this re-parameterisation and the kernel trick to obtain an implicit nonlinear mapping for the MAF transformation. A detailed account of this is given in [3].

Figure 3 shows kernel MAF component 1 of the IR-MAD variates based on \sim 3,000 training observations (top) and component 6 (bottom) centered on the mine.

5. RESULTS AND DISCUSSION

The IR-MAD components show changes for a large part of the entire subset. Especially phenological changes in the agricultural fields surrounding the open pit are predominant. As opposed to this, kMAF components focus more on changes in the open-cast mine (and changes due to the two clouds and their shadows, not visible in the zoom). Ground data were available from bucket-wheel excavators on the extraction side (to the northwest in the open pit) in terms of elevation data for both dates. No ground data were available for changes due to backfill (southeastern part of the open pit) or changes due to mining machines other than the bucket-wheels.

A visual comparison shows that areas detected as change in the kMAF components are related to areas that differ significantly in the two input images. Two observations can be made when comparing the kMAF components with ground data: some areas of extraction were detected perfectly (e.g., the north-most contours in the upper left of Figure 3); others were not detected at all (e.g., the east-most contours in Figure 3). This illustrates the fact that only those changes are detectable which are represented by spectral reflectances in the bands of the sensor (this excludes height information). In the case of the undetected area (the east-most contours), brown coal was extracted leading to an elevation difference of three to seven meters. However, this remained undetected due to the negligible change in reflectance (the pixels being covered by brown coal in both images).

In conclusion the IR-MAD components show changes in the agricultural areas as well as in the mine, and the kMAF components focus on extreme changes in the mine. Due to lack of change in the spectral signal (the change occurs in the

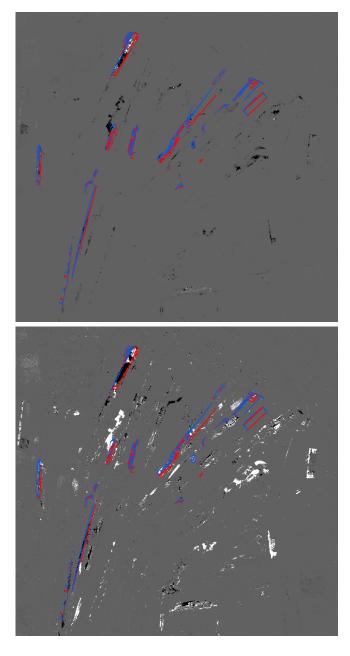


Fig. 3. Zoom of kMAF component 1 (top) and 6 (bottom) with ground data on bucket-wheel excavation; red: contours as of 24 May 2009, blue: contours as of 01 June 2009.

height of the surface only) excavation of material (here brown coal) leaving the same material behind is not detected.

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