

Analysis and Optimization of Mixed-Criticality Applications on Partitioned Distributed Architectures

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$f(x+\Delta x) = \sum_{i=0}^{\infty} \frac{(\Delta x)^i}{i!} f^{(i)}(x)$

$\int_a^b \varepsilon \Theta + \Omega \int \delta e^{i\pi} = \{2.7182818284\}$

χ^2

\sum

\gg

$!$

- Motivation
- Separation of mixed-criticality applications
 - At processing element level
 - At communication level
- Problem formulation and example
- Optimization strategy
- Experimental results
- Conclusions

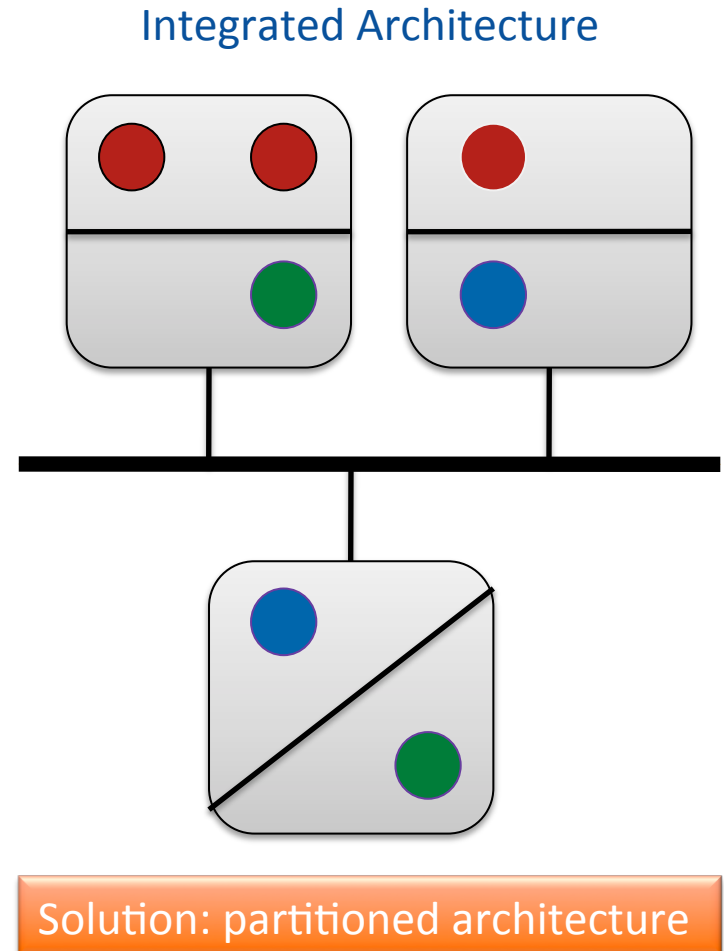
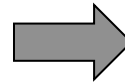
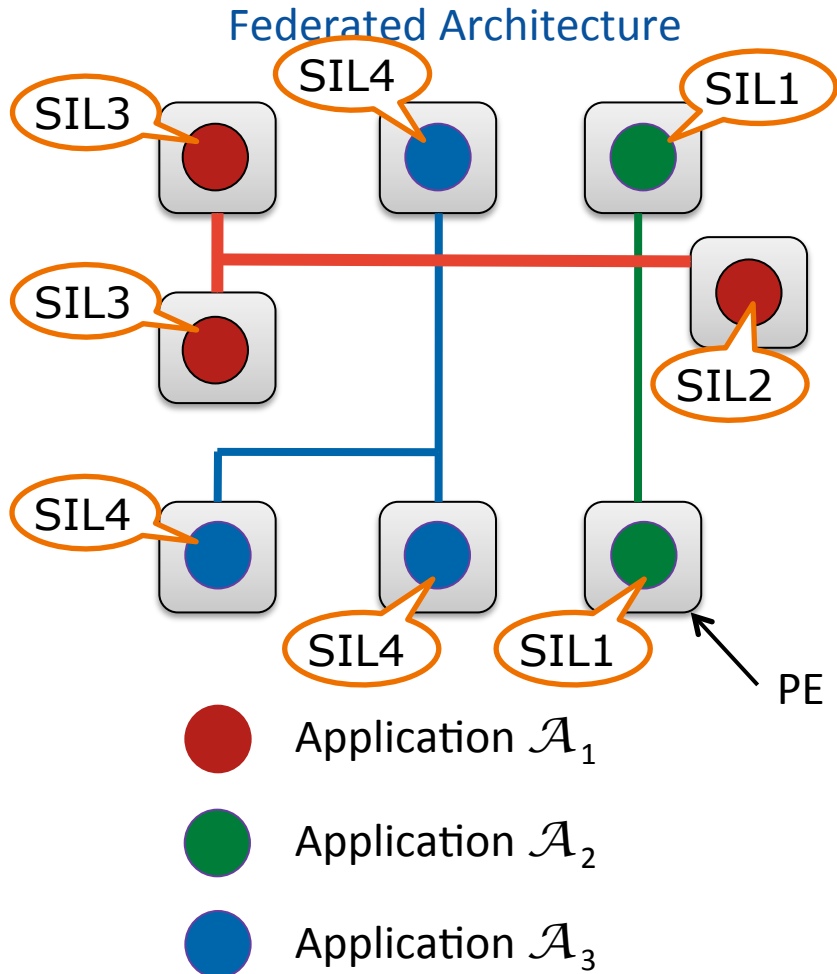
Motivation

- **Safety** is the property of a system that will not endanger human life or the environment
- A safety-related system needs to be **certified**
- A Safety Integrity Level (SIL) is assigned to each safety related function, depending on the required level of risk reduction
- There are 4 SILs:
 - SIL4 (most critical)
 - SIL1 (least critical)
 - SIL0 (non-critical) – not covered by standards
- SILs dictate the development process and certification procedures

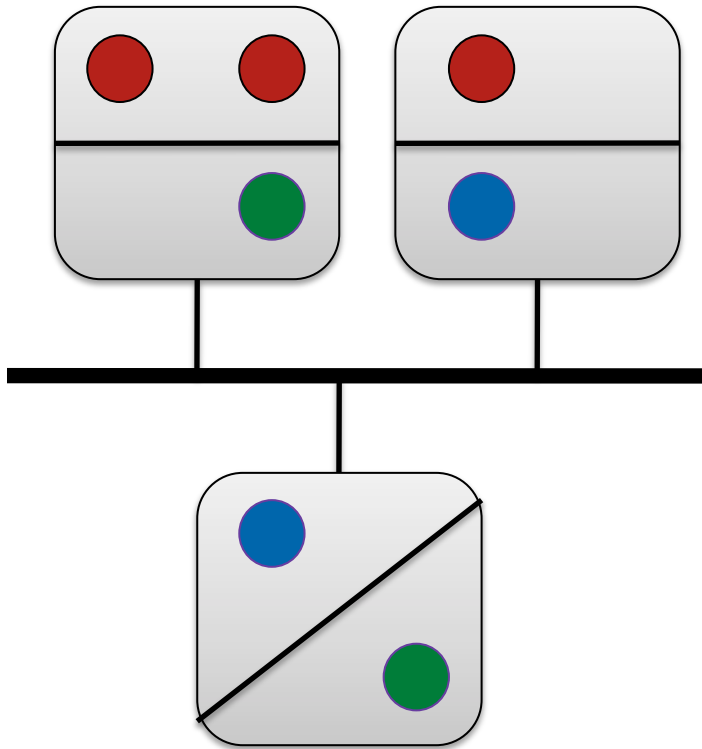
Motivation

- Real time applications implemented using distributed systems

- Mixed-criticality applications share the same architecture

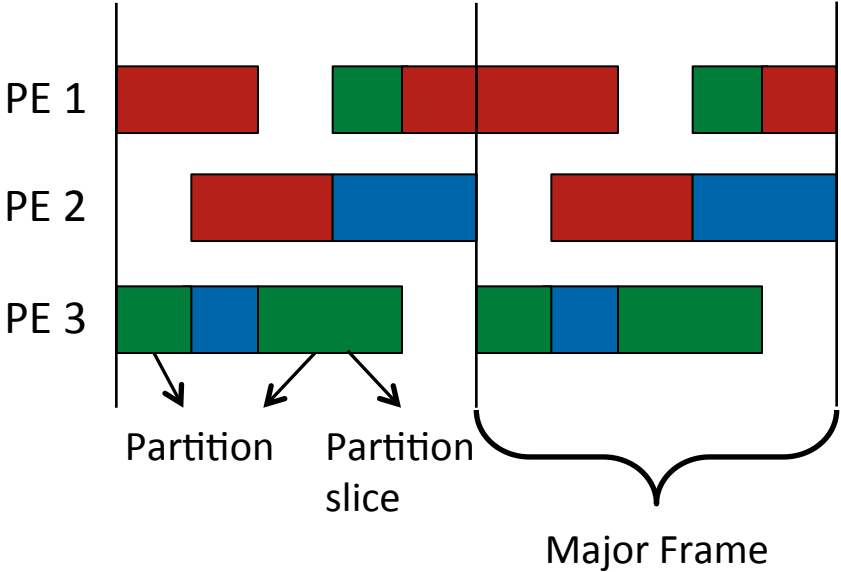
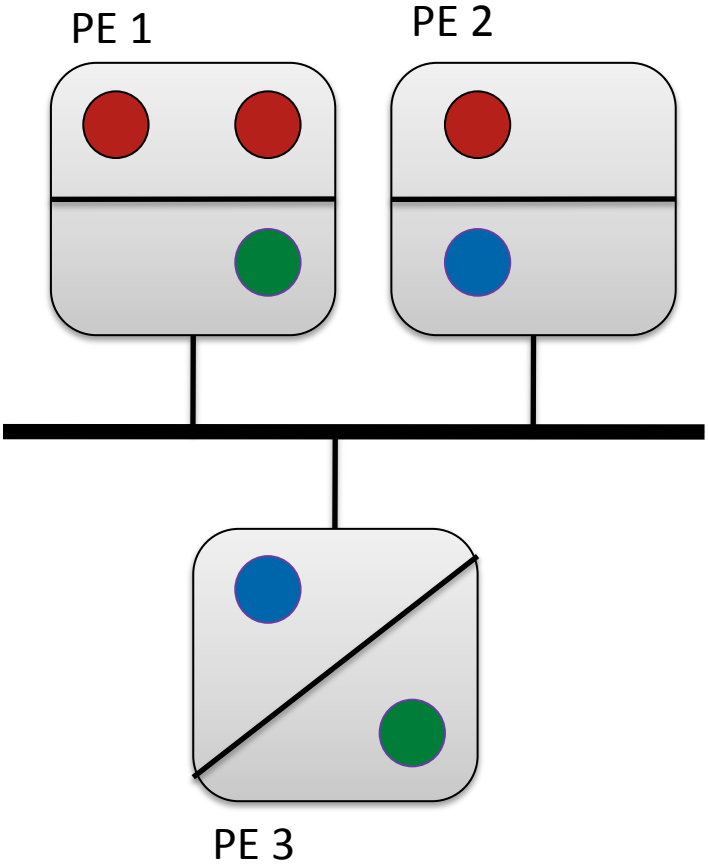


Separation at PE-level



- Partition = virtual dedicated machine
- Partitioned architecture
 - Spatial partitioning
 - protects one application's memory and access to resources from another application
 - Temporal partitioning
 - partitions the CPU time among applications

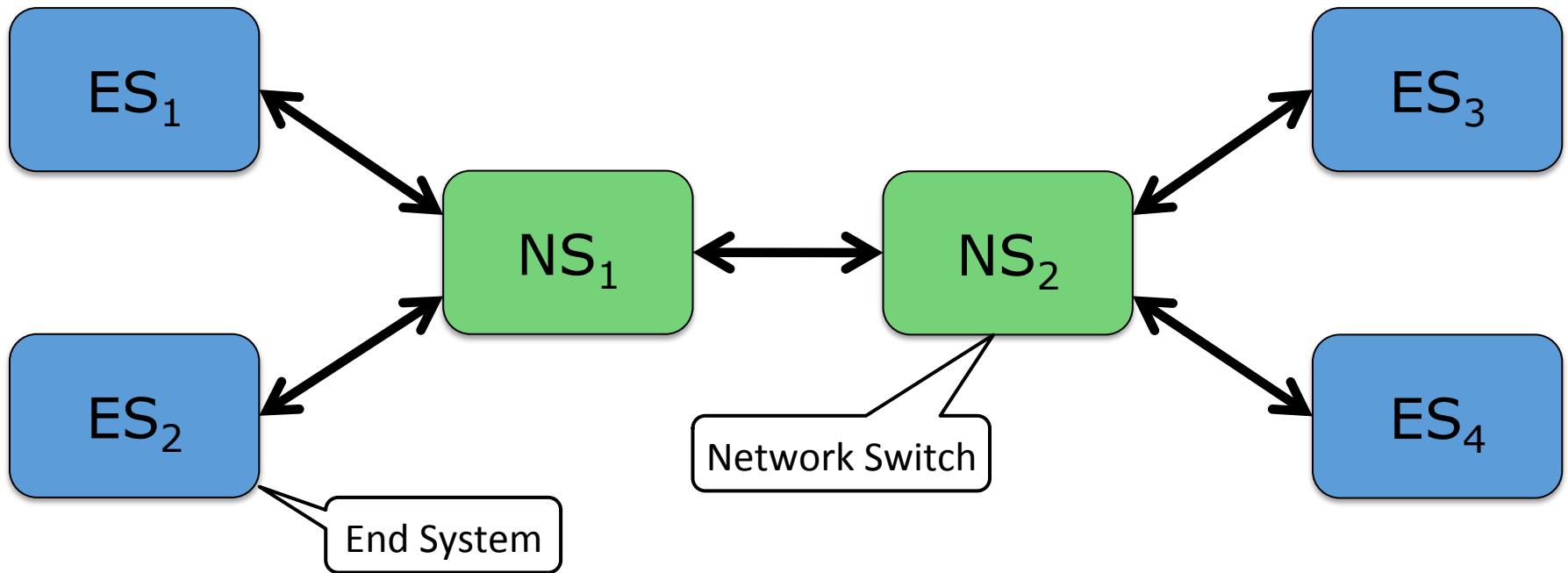
Separation at PE-level



- Temporal partitioning
 - Static partitioning
 - Re...
 - ...period MF
 - ...switch overhead
 - ...partition can have its own scheduling policy
 - A partition has a certain SIL

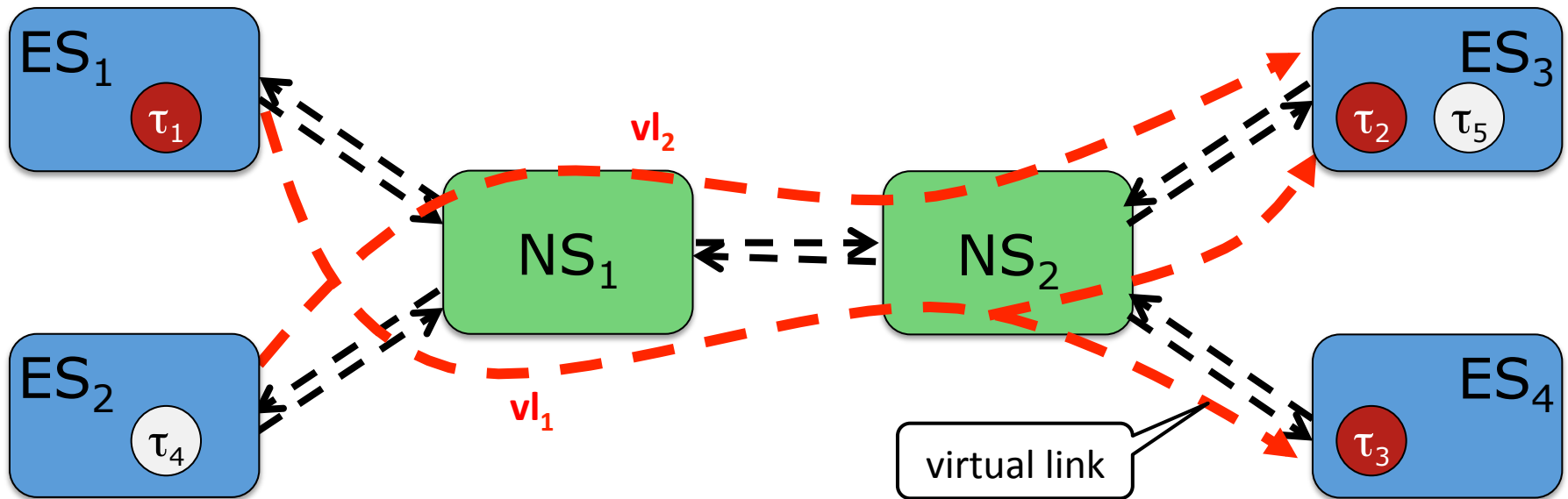
Problem: optimize task mapping and allocation of partitions

Separation at Network-level



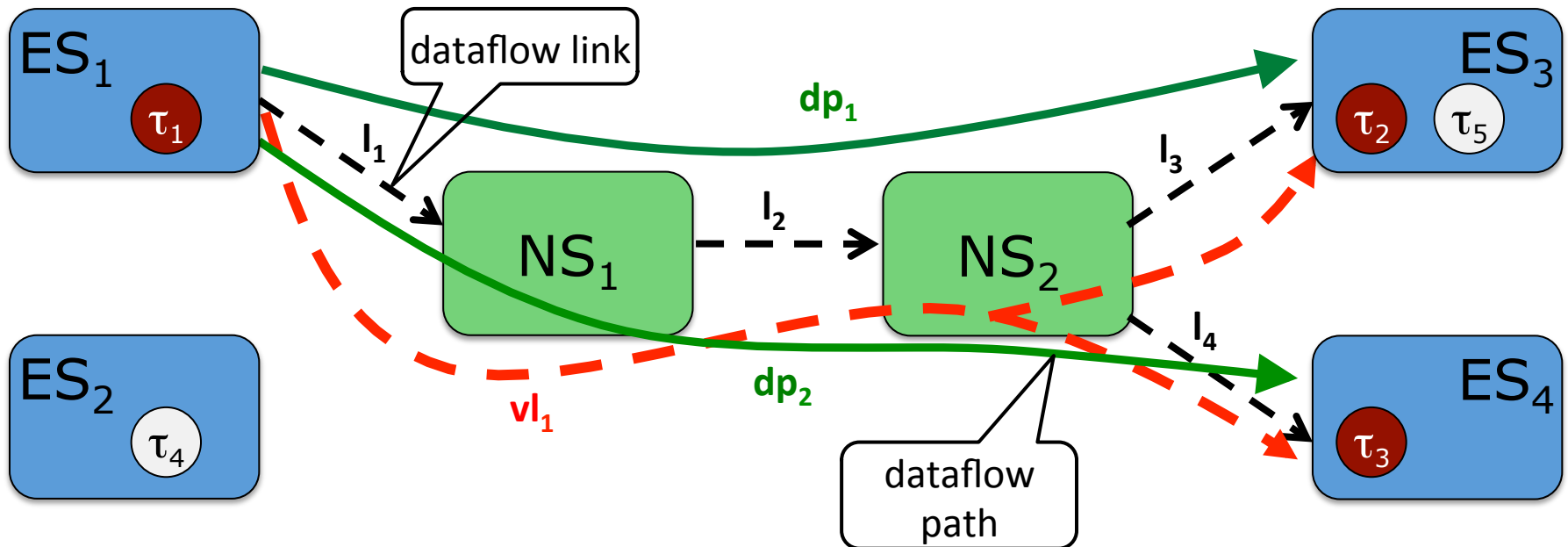
- Full-Duplex Ethernet-based data network for safety-critical applications
- Compliant with ARINC 664p7 “Aircraft Data Network”

Separation at Network-level



- Highly critical application \mathcal{A}_1 : τ_1 , τ_2 and τ_3
 - τ_1 sends message m_1 to τ_2 and τ_3
- Non-critical application \mathcal{A}_2 : τ_4 and τ_5
 - τ_4 sends message m_2 to τ_5

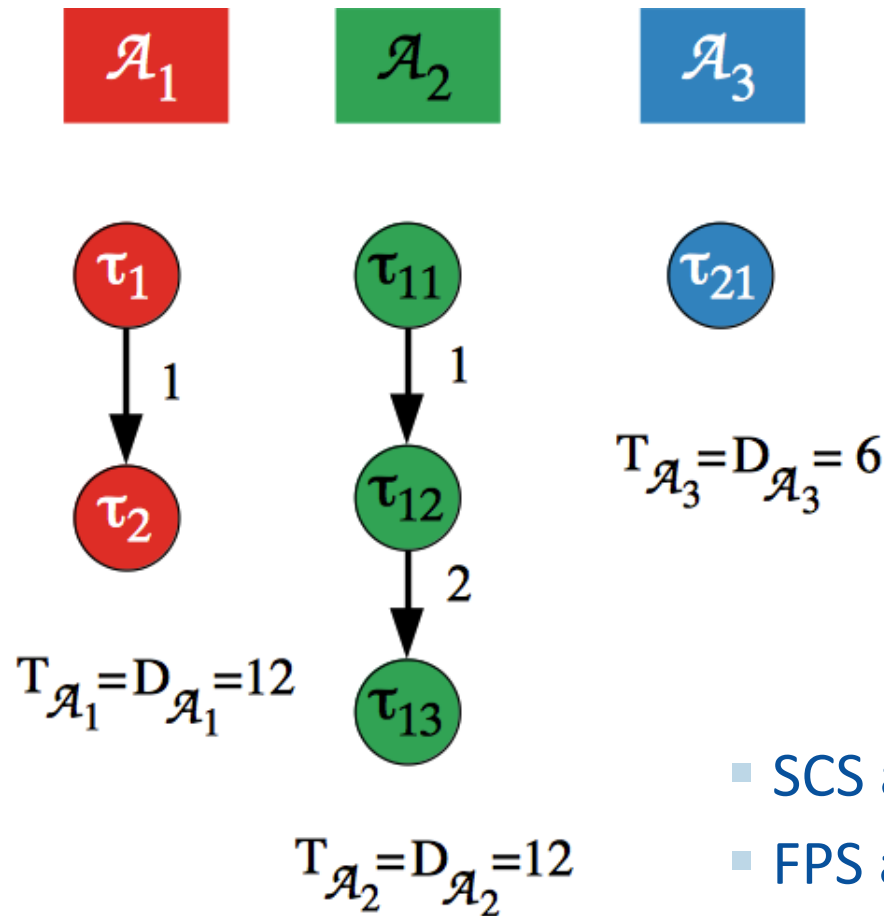
Separation at Network-level



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 - τ_1 sends message m_1 to τ_2 and τ_3
- Non-critical application \mathcal{A}_2 : τ_4 and τ_5
 - τ_4 sends message m_2 to τ_5

- Traffic classes
 - Time Triggered (TT)
 - based on static schedule tables
 - Rate Constrained (RC)
 - deterministic unsynchronized communication
 - ARINC 664p7 traffic
 - Best Effort (BE)
 - no timing guarantees provided

Application Model



| | \mathcal{A}_1 | | \mathcal{A}_2 | | | \mathcal{A}_3 |
|-------|-----------------|----------|-----------------|-------------|-------------|-----------------|
| | τ_1 | τ_2 | τ_{11} | τ_{12} | τ_{13} | τ_{21} |
| N_1 | 2 | x | 2 | 3 | 3 | 1 |
| N_2 | 4 | 5 | 3 | 5 | 4 | 2 |

WCET and mapping restrictions

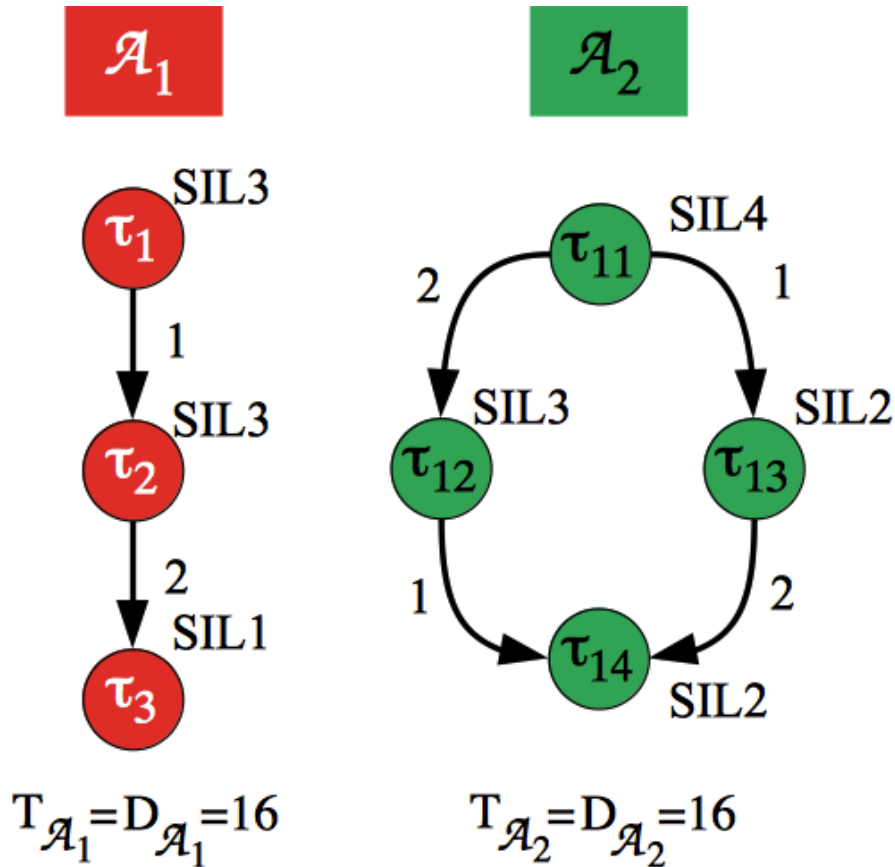
- SCS apps transmit TT messages
- FPS apps transmit RC messages

Problem formulation

- Given
 - A set of applications
 - The criticality level (or SIL) of each task
 - A set of N processing elements (PEs) and topology of the network
 - The set of TT and RC frames
 - The set of virtual links
 - The size of the Major Frame and of the Application Cycle
- Determine
 - The mapping of tasks to PEs
 - The sequence and length of partition slices on each processor
 - The assignment of tasks to partitions
 - The schedule for all the tasks and TT frames in the system
- Such that
 - All applications meet their deadline
 - The response times of the FPS tasks and RC frames is minimized

Motivational Example 1

- Mapping and partitioning optimization

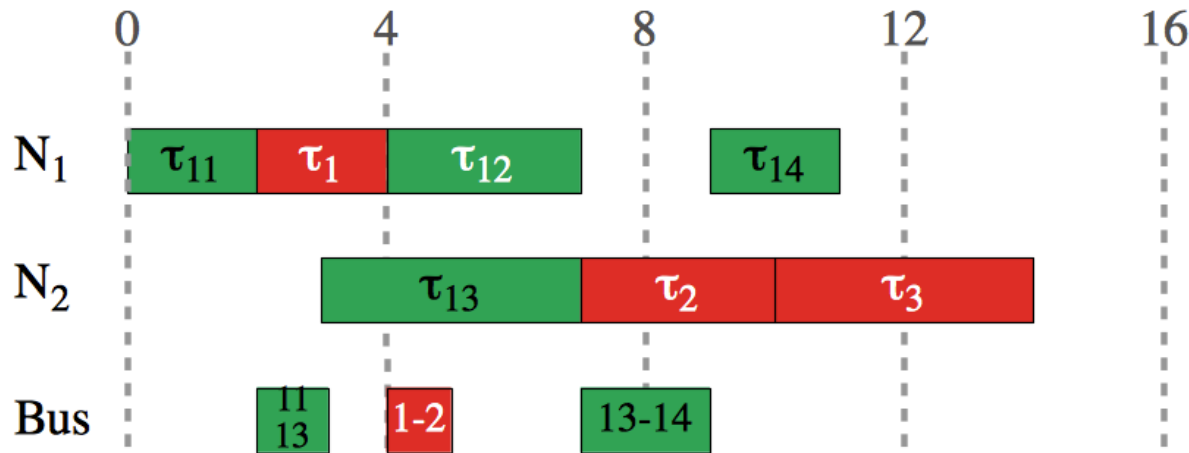


Mixed-criticality applications

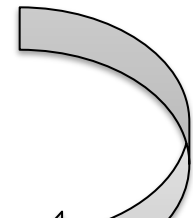
| | N_1 | N_2 | |
|-----------------|-------------|-------|---|
| \mathcal{A}_1 | τ_1 | 2 | 4 |
| | τ_2 | x | 3 |
| | τ_3 | 3 | 4 |
| \mathcal{A}_2 | τ_{11} | 2 | 3 |
| | τ_{12} | 3 | 5 |
| | τ_{13} | x | 4 |
| | τ_{14} | 2 | 3 |

WCET and mapping restrictions

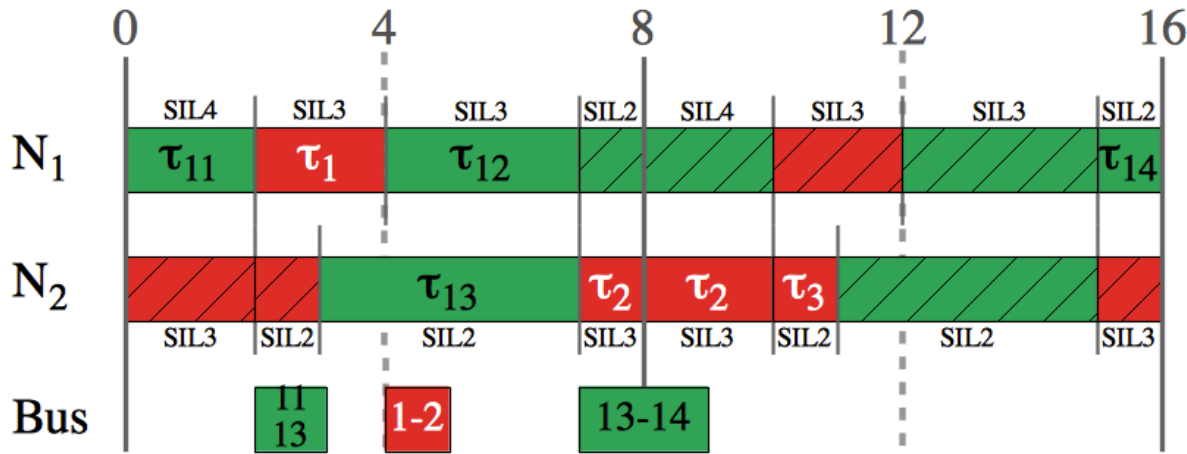
Motivational Example 1



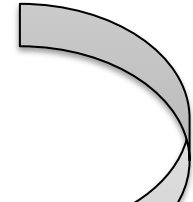
Optimal mapping,
without considering
partitions.



Motivational Example 1

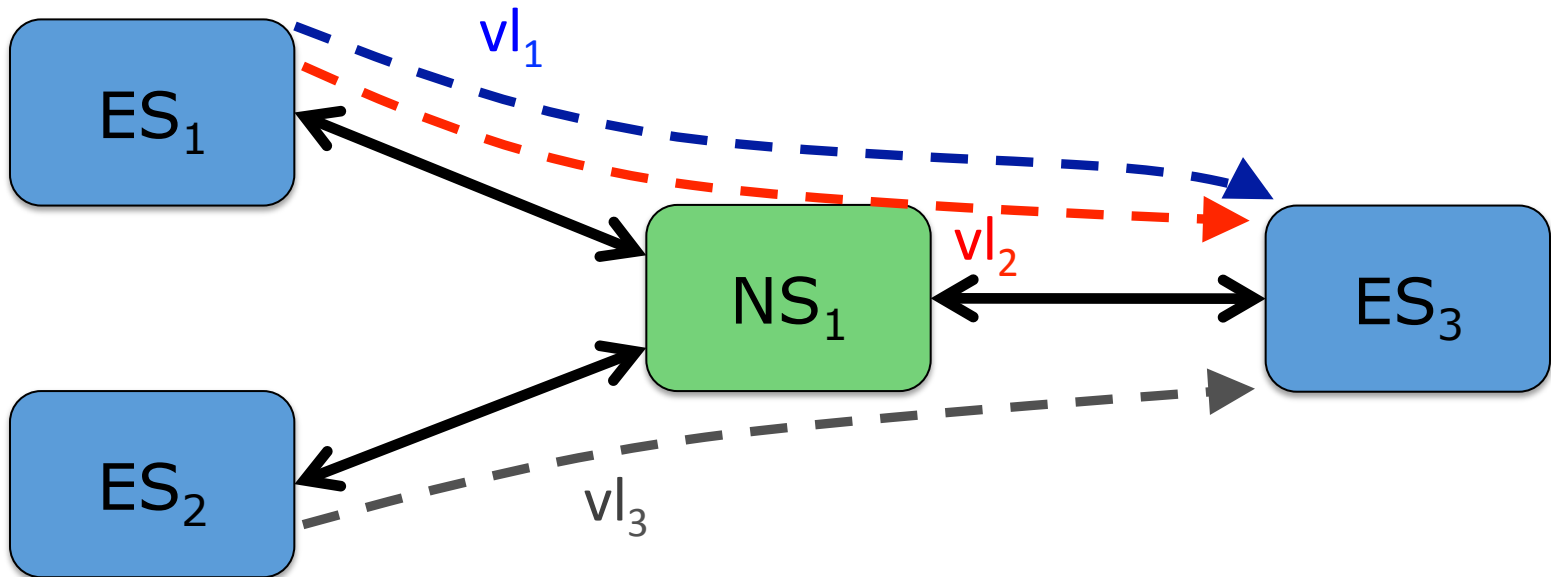


Partitioning, using the previously obtained mapping. τ_3 and τ_{14} miss their deadline.



Motivational Example 2

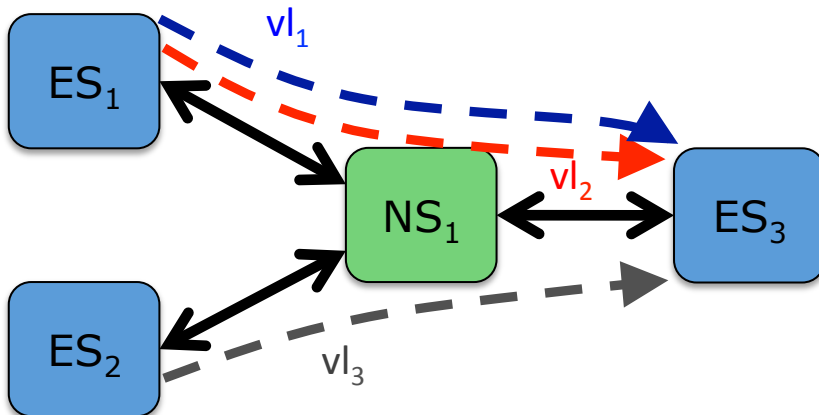
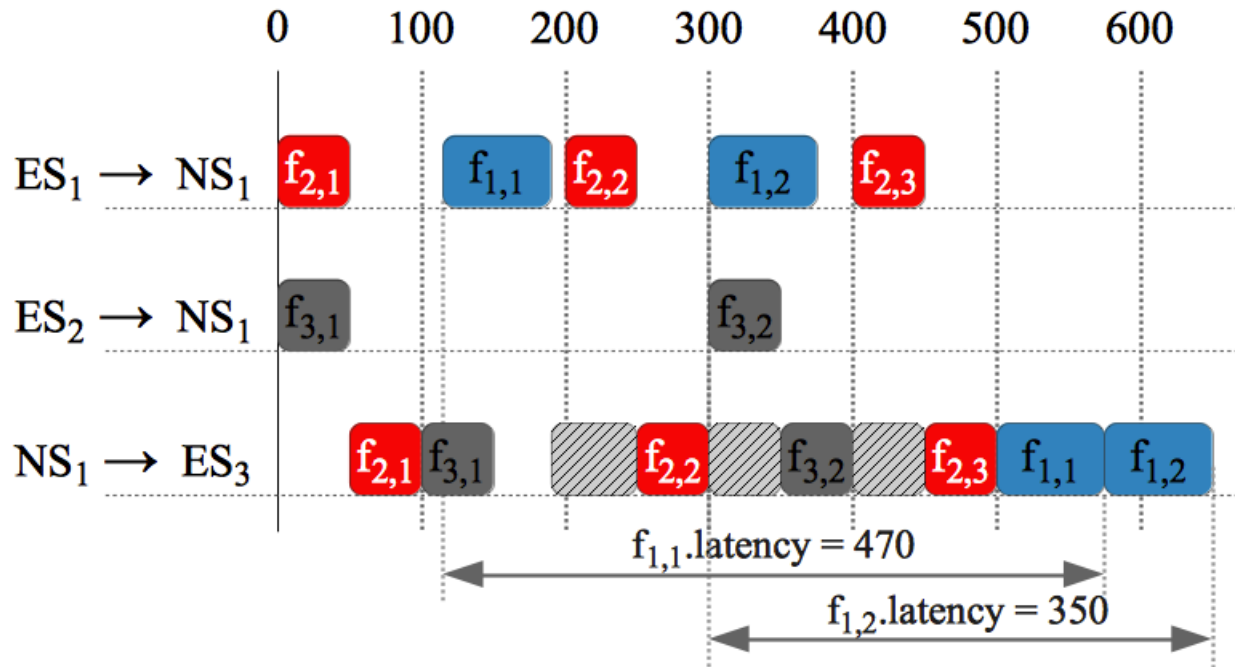
- Optimization of TT message schedules



| | period (us) | deadline (us) | C_i (us) | \mathcal{M} |
|---------------------------|-------------|---------------|------------|---------------|
| $f1 \in \mathcal{F}^{RC}$ | 300 | 300 | 75 | vl_1 |
| $f2 \in \mathcal{F}^{TT}$ | 200 | 200 | 50 | vl_2 |
| $f3 \in \mathcal{F}^{TT}$ | 300 | 300 | 50 | vl_3 |

Motivational Example 2

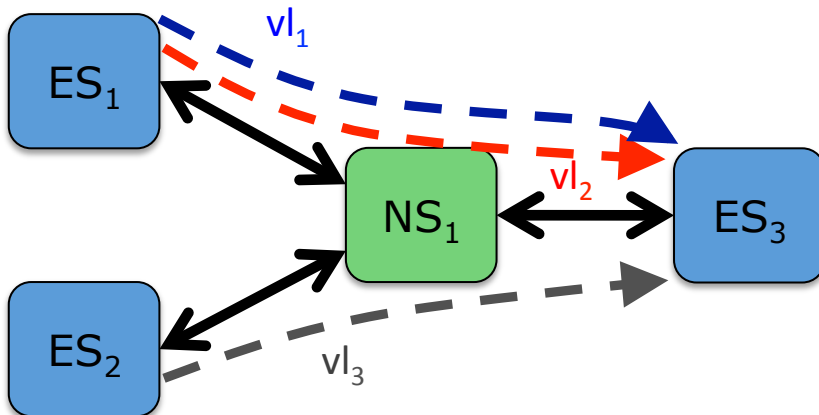
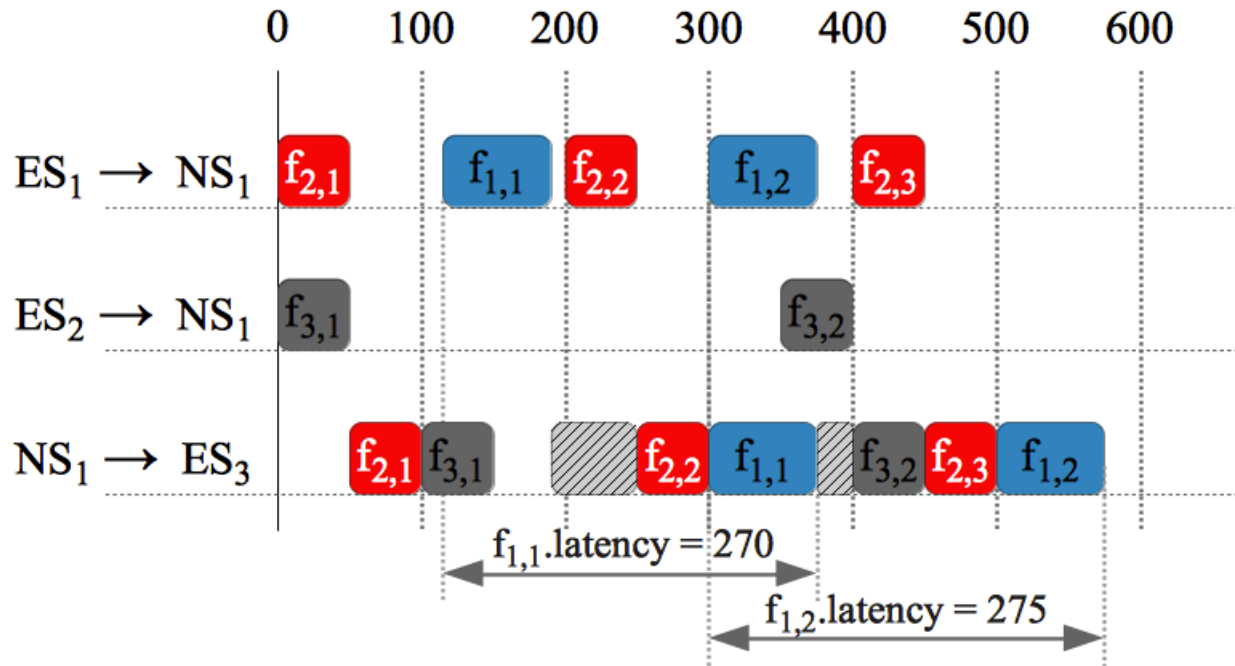
- Initial TT schedule



| | period (us) | deadline (us) | C_i (us) | \mathcal{M} |
|----------------------------|-------------|---------------|------------|---------------|
| $f_1 \in \mathcal{F}^{RC}$ | 300 | 300 | 75 | vl_1 |
| $f_2 \in \mathcal{F}^{TT}$ | 200 | 200 | 50 | vl_2 |
| $f_3 \in \mathcal{F}^{TT}$ | 300 | 300 | 50 | vl_3 |

Motivational Example 2

- Optimized TT schedule



| | period (us) | deadline (us) | C_i (us) | \mathcal{M} |
|----------------------------|-------------|---------------|------------|---------------|
| $f_1 \in \mathcal{F}^{RC}$ | 300 | 300 | 75 | vl_1 |
| $f_2 \in \mathcal{F}^{TT}$ | 200 | 200 | 50 | vl_2 |
| $f_3 \in \mathcal{F}^{TT}$ | 300 | 300 | 50 | vl_3 |

Optimization Strategy

- Tabu Search meta-heuristic
 - Task mapping and partition slice optimization (TO)
 - Considering TT frame schedules fixed
 - TT frame schedules optimization (TM)
 - Considering the task mapping and partition slices fixed
- Tabu Search
 - Minimizes the cost function
 - Explores the solution space using design transformations

Optimization Strategy

- Degree of schedulability
 - Captures the difference between the worst-case response time and the deadline

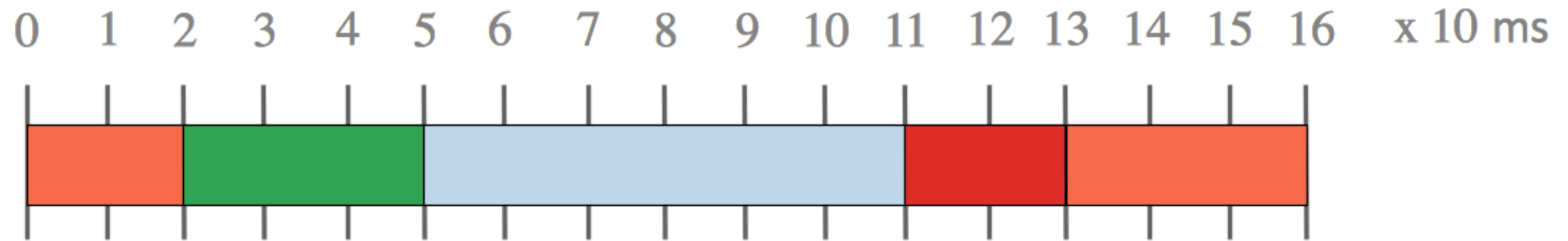
- Cost Function

$$Cost(\Psi) = \begin{cases} c_1 = \sum_{\mathcal{A}_i \in \Gamma} \max(0, R_i - D_i) & \text{if } c_1 > 0 \\ c_2 = \sum_{\mathcal{A}_i \in \Gamma} (R_i - D_i) & \text{if } c_1 = 0 \end{cases}$$

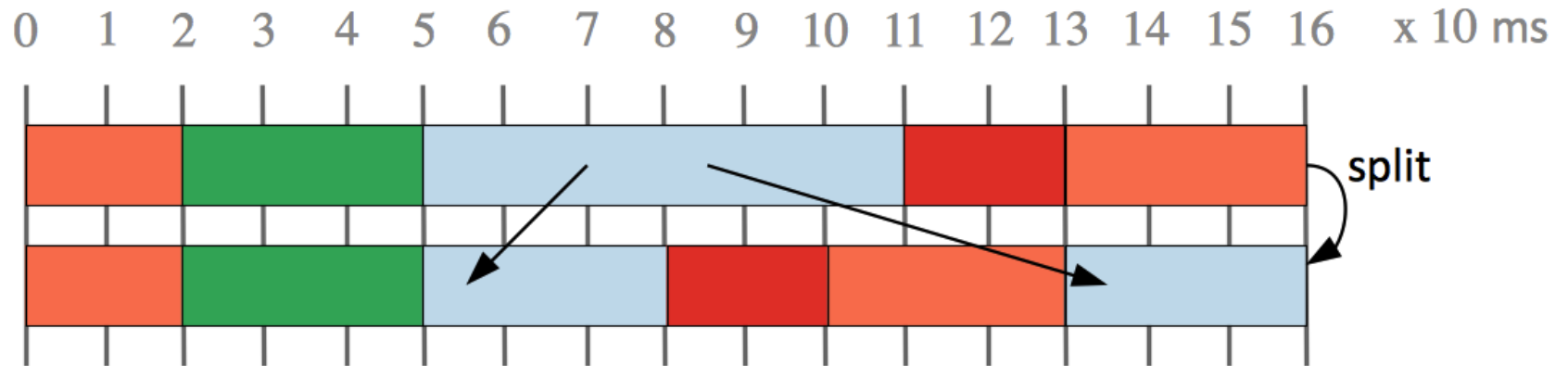
Optimization Strategy: Design Transformations

- Partition slice moves
 - resize partition slice
 - swap two partition slices
 - join two partition slices
 - split partition slice into two
- Task moves
 - re-assign task to another partition

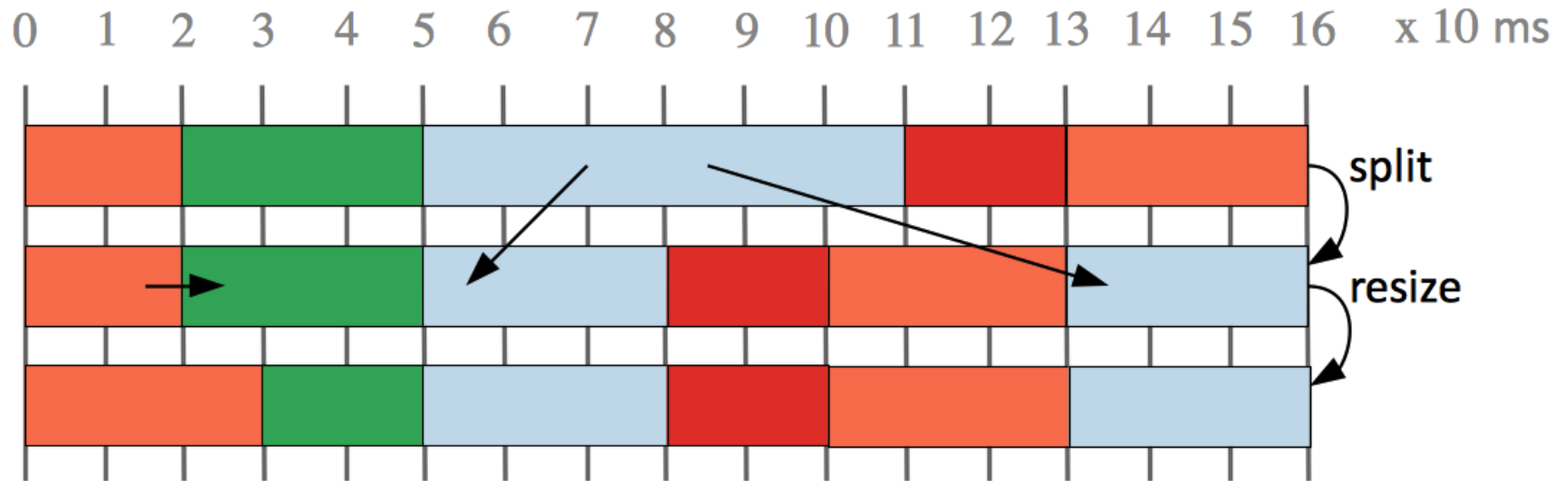
Optimization Strategy: Design Transformations



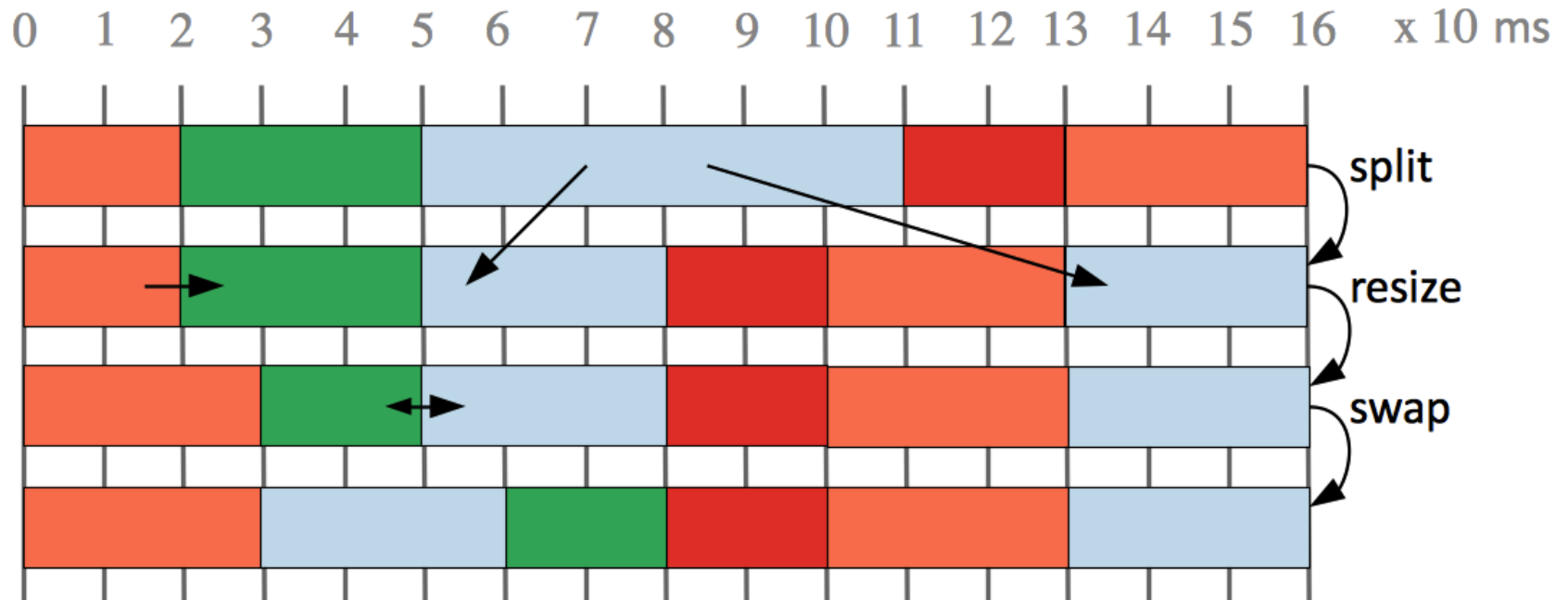
Optimization Strategy: Design Transformations



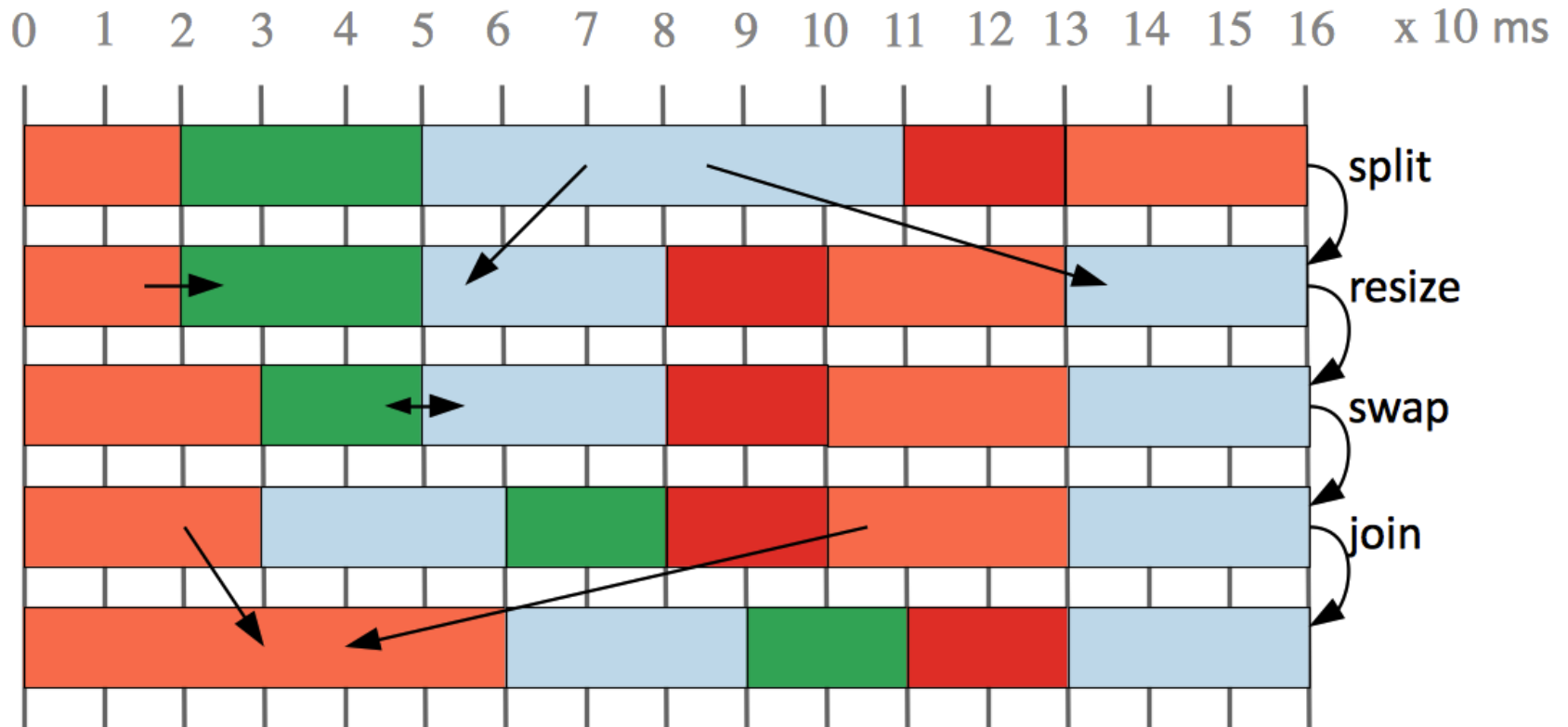
Optimization Strategy: Design Transformations



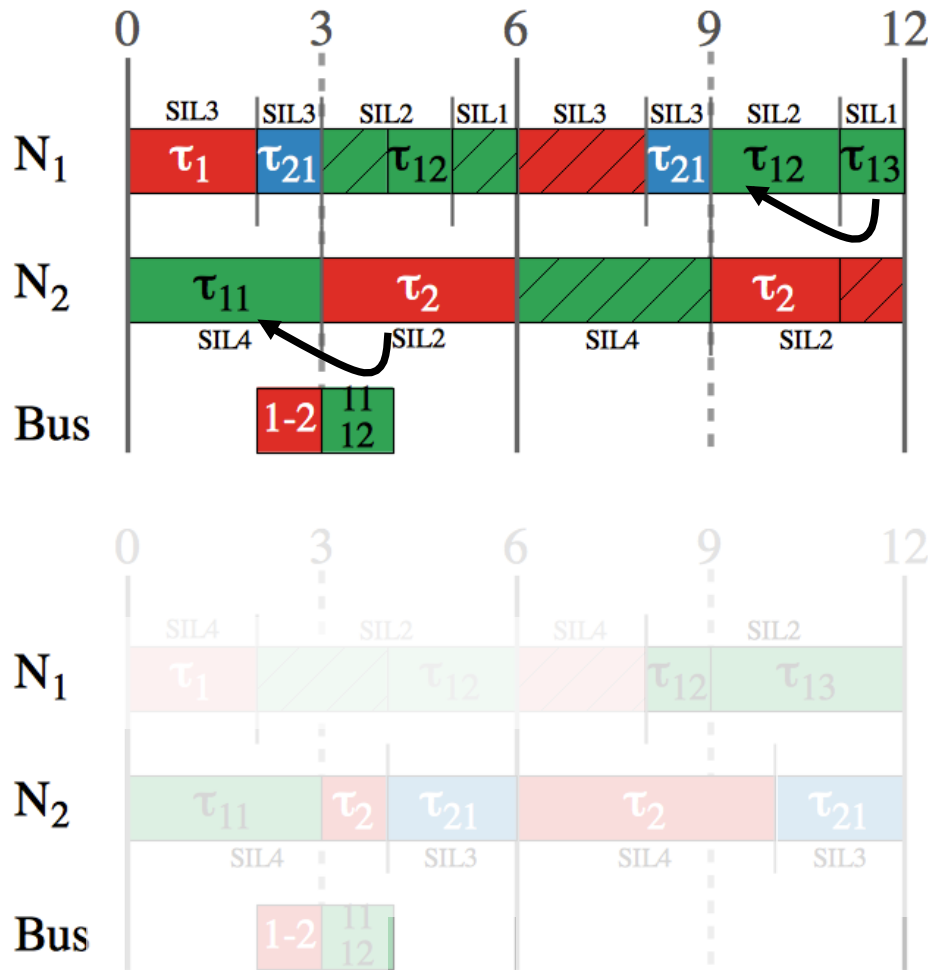
Optimization Strategy: Design Transformations



Optimization Strategy: Design Transformations



Optimization Strategy: Design Transformation

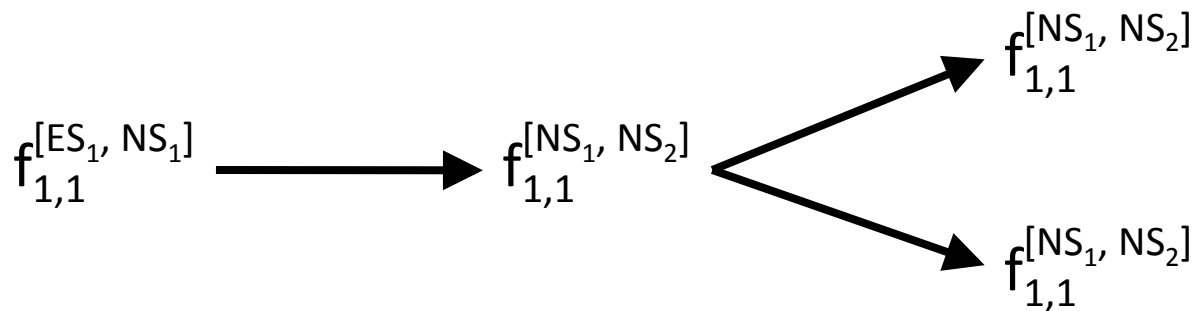
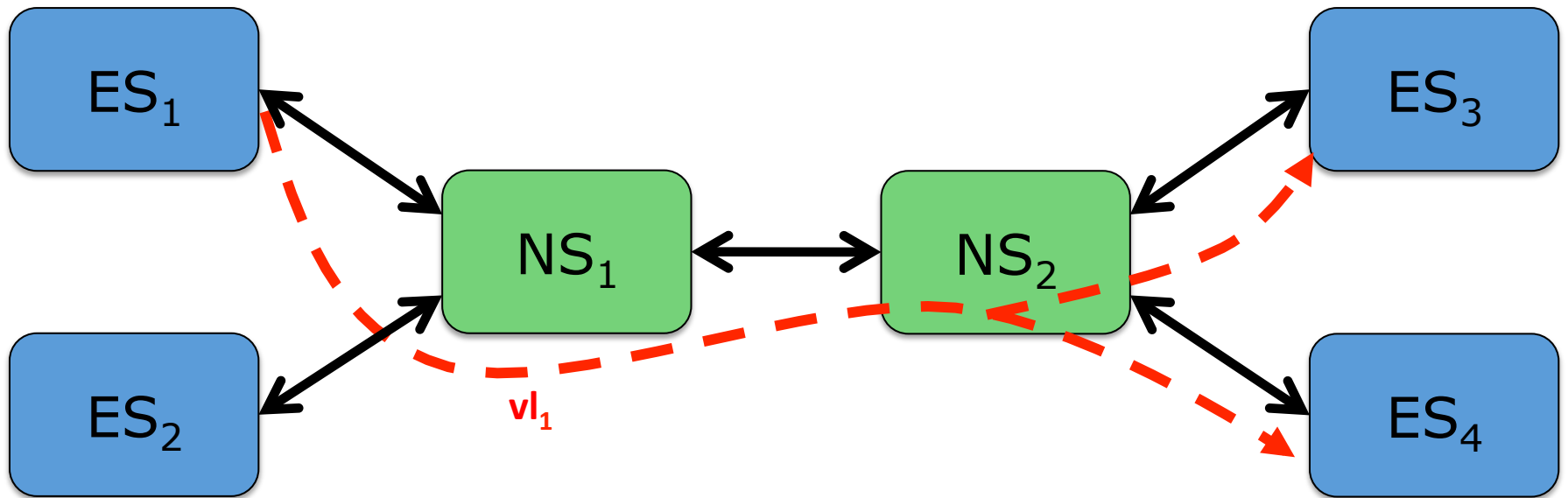


- **Task re-assignment move**
 - To another partition of the same application
 - To a partition of another application
 - To a newly created partition
- Empty partitions are deleted

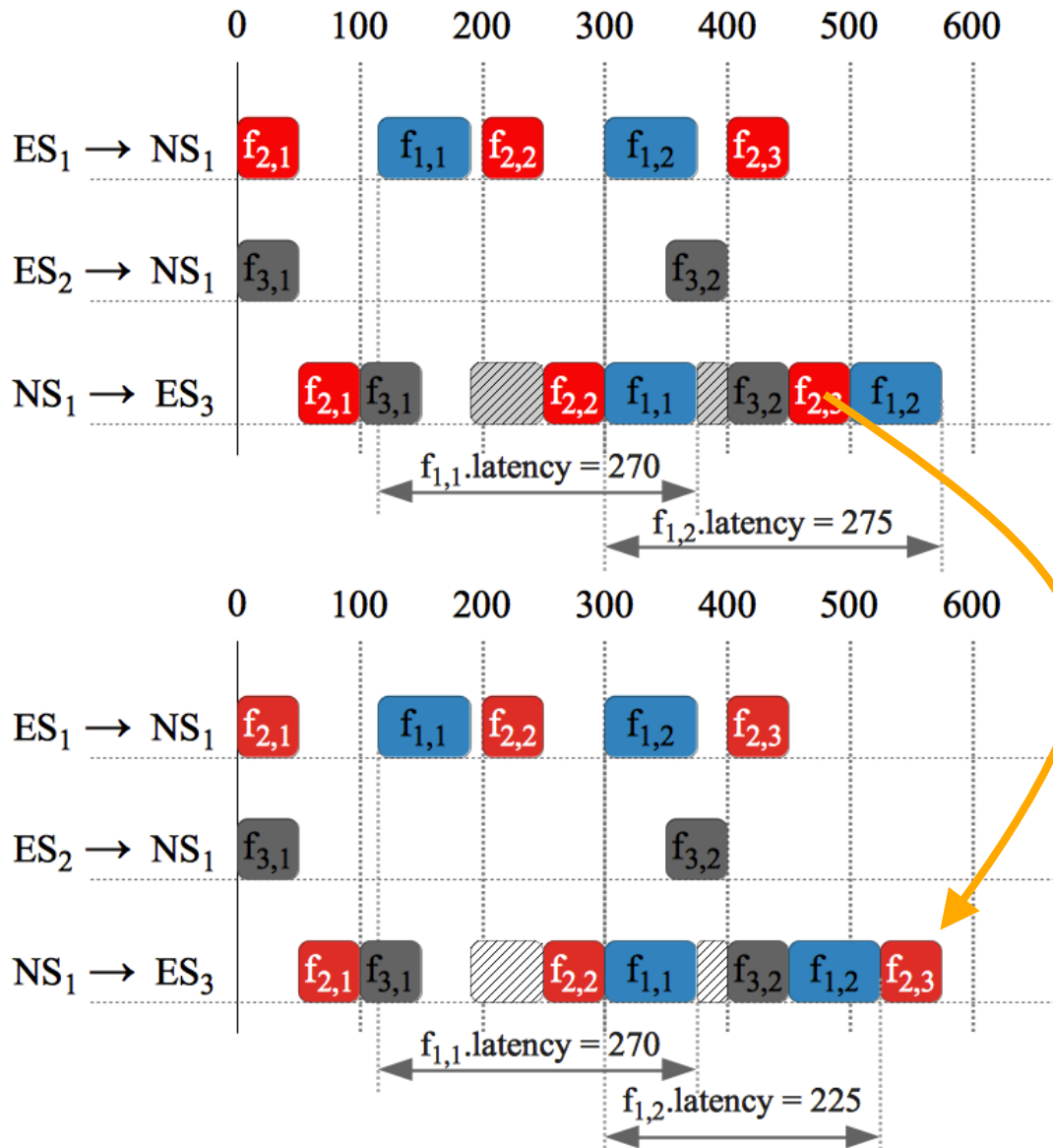
Optimization Strategy: Design Transformations

- TT frame moves
 - advance frame transmission time
 - advance frame predecessors transmission time
 - postpone frame transmission time
 - postpone frame successors transmission time
- RC frame moves
 - reserve space for RC frame
 - resize reserved space for RC frame
 - remove reserved space for RC frame

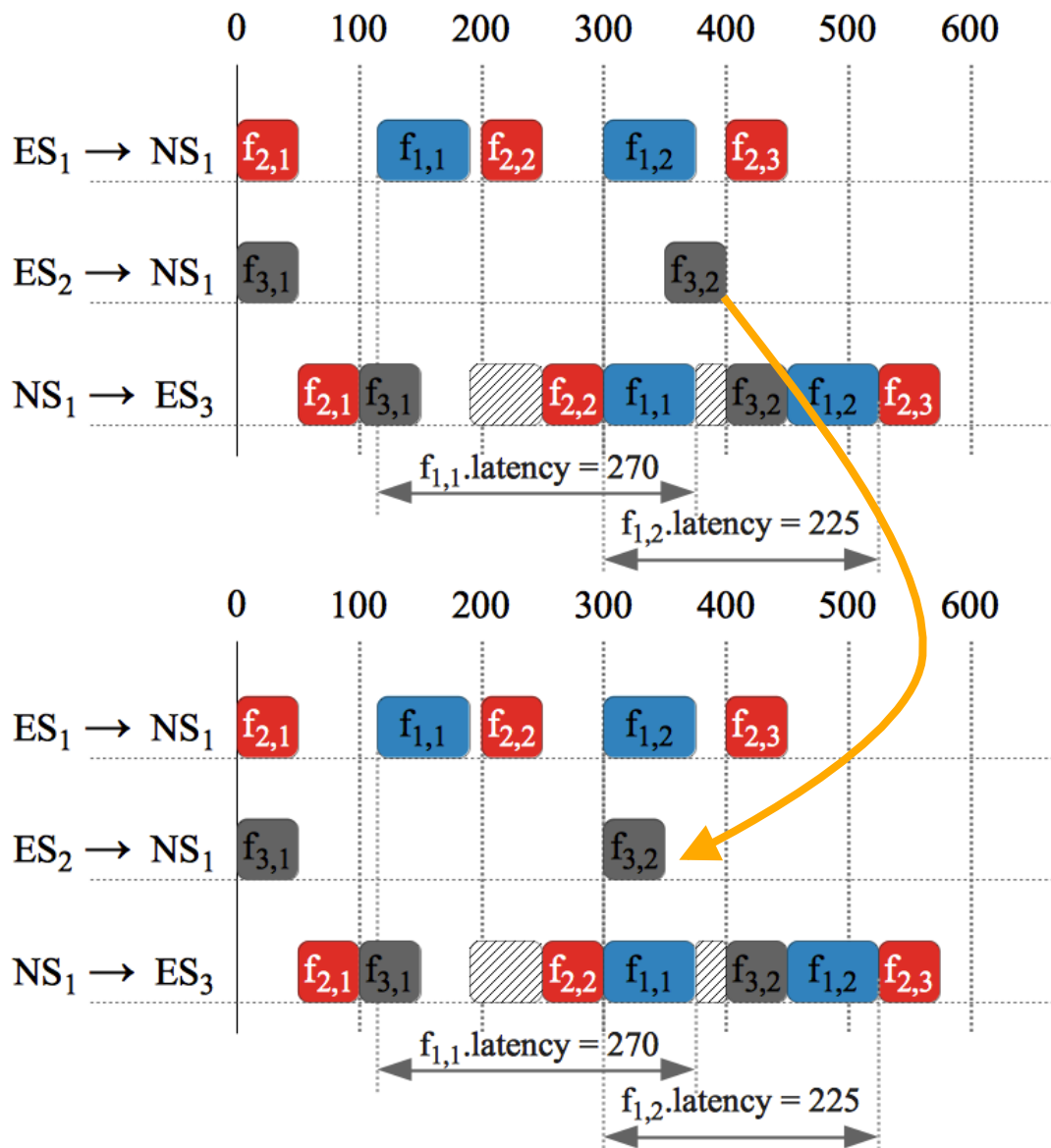
Frame Representation for Moves



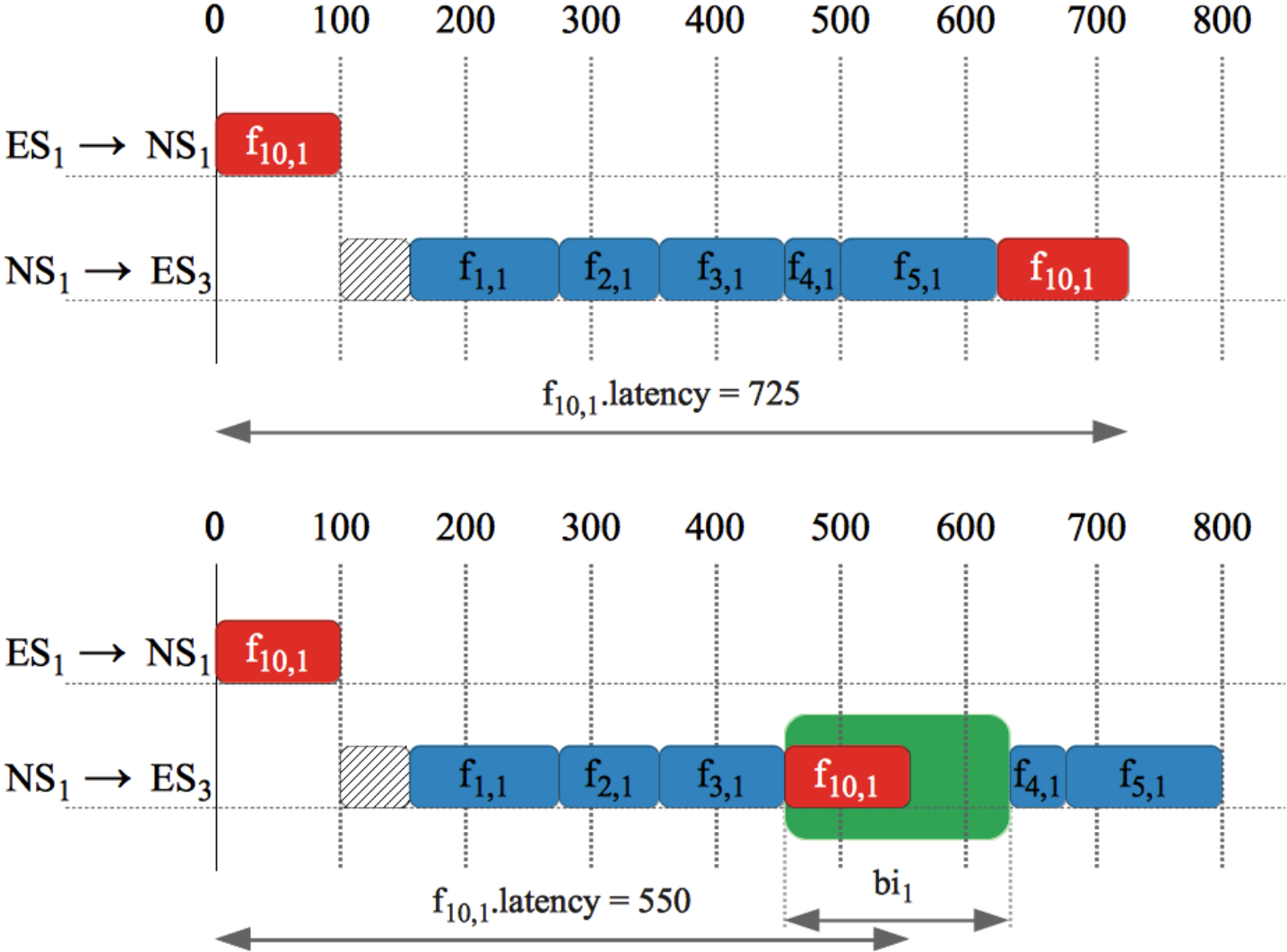
Design transformations: Postpone move



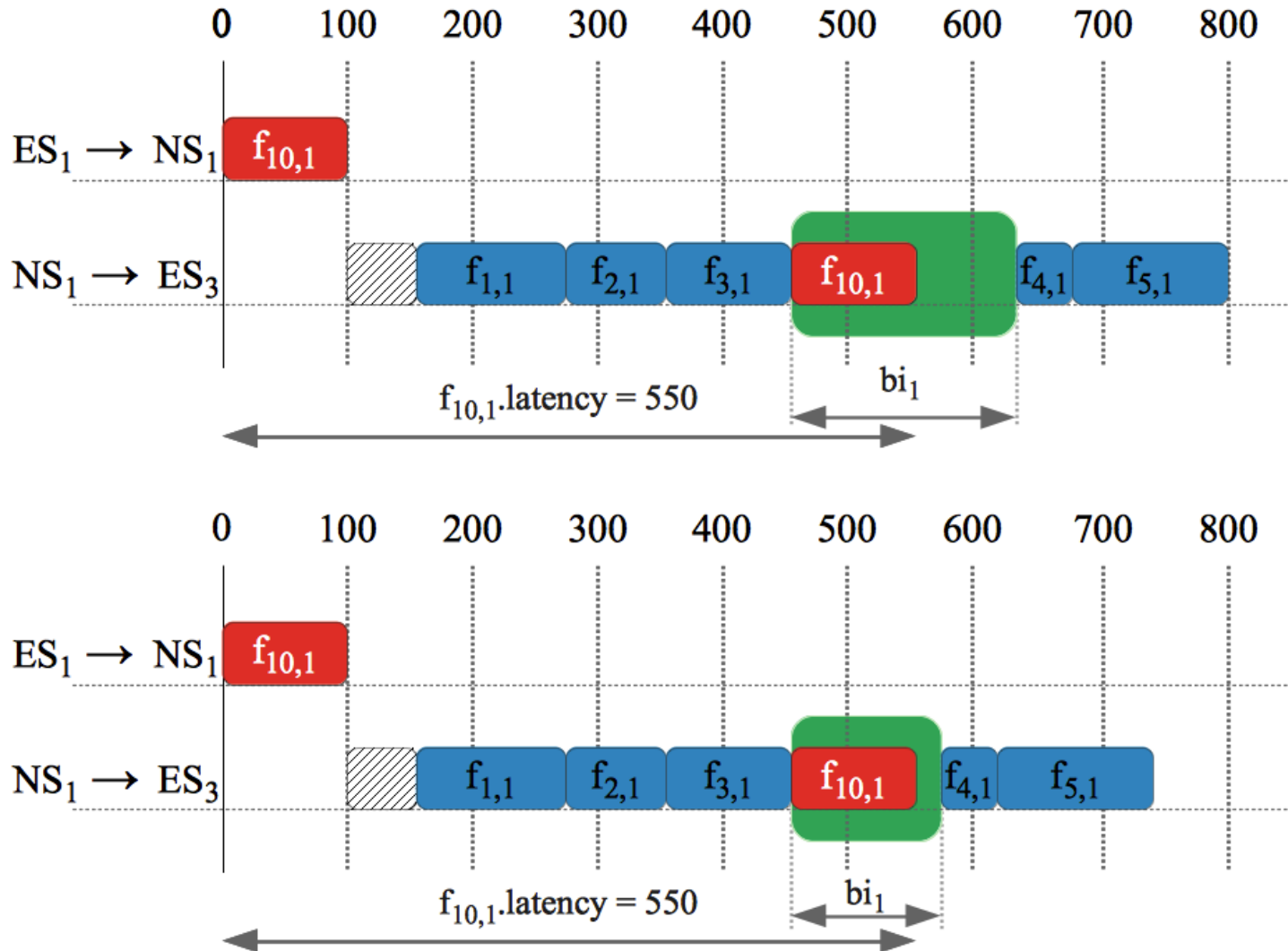
Design transformations: Advance move



Design transformations: Reserve space for RC



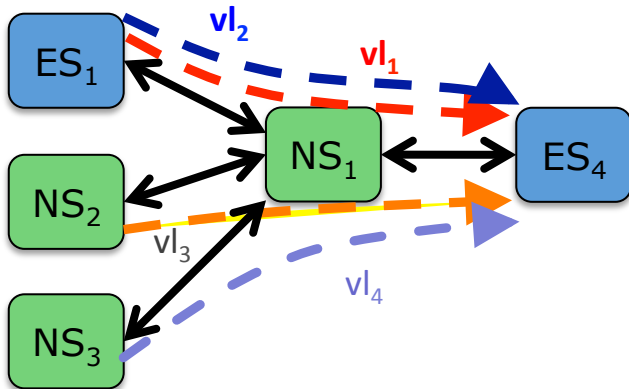
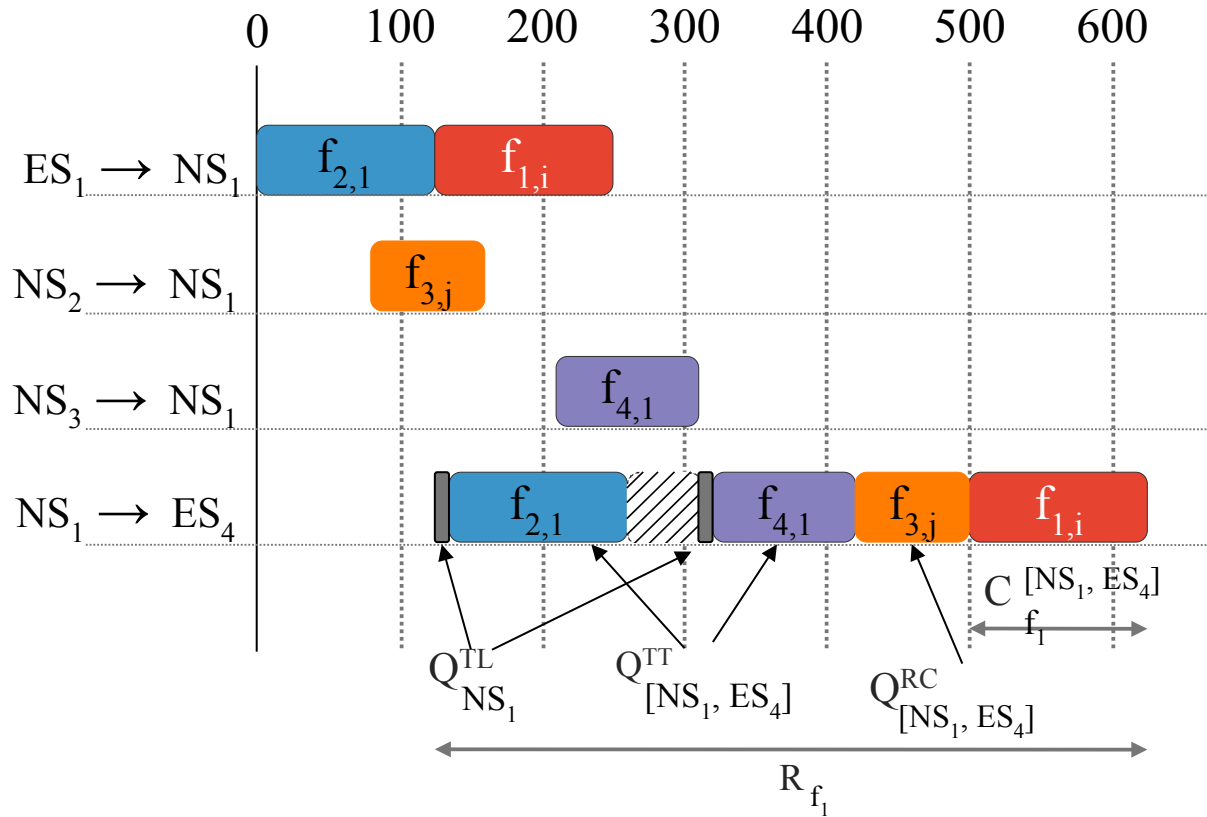
Design transformations: Resize RC reserved space



RC Frame End-to-End Analysis

- On a dataflow link, a RC frame can be delayed by:
 - scheduled TT frames
 - queued RC frames
 - technical latency
 - policy specific:
 - timely block
 - pre-emption

RC Frame End-to-End Analysis



$$Q_{f_i}^{[v_j, v_k]} = Q_{f_i, [v_j, v_k]}^{TT} + Q_{f_i, [v_j, v_k]}^{RC} + Q_{v_j}^{TL}$$

$$R_{f_i} = \sum_{\substack{v_j, v_k \in \mathcal{V} \\ [v_j, v_k] \in vl_i}} (Q_{f_i}^{[v_j, v_k]} + C_{f_i}^{[v_j, v_k]})$$

RC Frame End-to-End Analysis

- Approaches for analysis of ARINC 644p7 network traffic:
 - Network Calculus, (Boyer, 2008)
 - Finite State Machine, (Saha, 2007)
 - Timed Automata, (Adnan, 2010)
 - Trajectory Approach, (Bauer, 2009)
- We use the method proposed in (Steiner, 2011)
 - it takes into account also the TT traffic
 - it is pessimistic:
 - does not ignore frames that already delayed a RC frame on a previous link
 - assumes uniformly distributed intervals of equal length reserved for RC traffic

Experimental Results: TO

- Benchmarks
 - 5 synthetic
 - 2 real life test cases from E3S
- TO compared to:
 - Straightforward Solution for Tasks (SST)
 - Simple partitioning scheme, each application \mathcal{A}_i is allocated a total time proportional to the utilization of tasks of \mathcal{A}_i on the processor they are mapped to

Experimental Results: TO

| Set | Tasks | PEs | SST Sched. Tasks | TO Sched. Tasks | avg. % increase in δ |
|-----|-------|-----|---------------------|--------------------|--------------------------------|
| 1 | 20 | 2 | 10 | All | 832.88 |
| | 26 | 3 | 13 | All | 27.36 |
| | 40 | 4 | 6 | All | 88.41 |
| | 50 | 5 | 10 | All | 73.57 |
| | 62 | 6 | 26 | All | 278.72 |

Experimental Results: TO

| Set | Tasks | PEs | SST Sched. Tasks | TO Sched. Tasks | avg. % increase in δ |
|-----|-------|-----|---------------------|--------------------|--------------------------------|
| 1 | 20 | 2 | 10 | All | 832.88 |
| | 26 | 3 | 13 | All | 27.36 |
| | 40 | 4 | 6 | All | 88.41 |
| | 50 | 5 | 10 | All | 73.57 |
| | 62 | 6 | 26 | All | 278.72 |
| 2 | 24 | 3 | 5 | All | 113.95 |
| | 25 | 3 | All | All | 61.87 |

Experimental Results: TM

- Benchmarks
 - 7 synthetic
 - 1 real life test case based on the SAE Automotive benchmark
- TM compared to:
 - Straightforward Solution for Messages (SSM)
 - Builds TT schedules with the goal to optimize the end-to-end response time of the TT frames without considering the RC traffic

Experimental Results: TM

| Set | Test case | ES | NS | Messages | Frame instances | Δ_{cost} [%] |
|-----|-----------|----|----|----------|-----------------|---------------------|
| 1 | 11 | 13 | 4 | 80 | 12593 | 2.58 |
| | 12 | 25 | 6 | 88 | 1787 | 24.44 |
| | 13 | 35 | 8 | 103 | 2285 | 20.06 |
| | 14 | 45 | 10 | 165 | 3299 | 11.90 |

Experimental Results: TM

| Set | Test case | ES | NS | Messages | Frame instances | Δ_{cost} [%] |
|-----|-----------|----|----|----------|-----------------|---------------------|
| 1 | 11 | 13 | 4 | 80 | 12593 | 2.58 |
| | 12 | 25 | 6 | 88 | 1787 | 24.44 |
| | 13 | 35 | 8 | 103 | 2285 | 20.06 |
| | 14 | 45 | 10 | 165 | 3299 | 11.90 |
| 2 | 21 | 11 | 4 | 115 | 16904 | 9.17 |
| | 22 | 25 | 6 | 179 | 2523 | 20.61 |
| | 23 | 35 | 8 | 154 | 3698 | 39.34 |

Experimental Results: TM

| Set | Test case | ES | NS | Messages | Frame instances | Δ_{cost} [%] |
|-----|------------|----|----|----------|-----------------|---------------------|
| 1 | 11 | 13 | 4 | 80 | 12593 | 2.58 |
| | 12 | 25 | 6 | 88 | 1787 | 24.44 |
| | 13 | 35 | 8 | 103 | 2285 | 20.06 |
| | 14 | 45 | 10 | 165 | 3299 | 11.90 |
| 2 | 21 | 11 | 4 | 115 | 16904 | 9.17 |
| | 22 | 25 | 6 | 179 | 2523 | 20.61 |
| | 23 | 35 | 8 | 154 | 3698 | 39.34 |
| 3 | automotive | 15 | 3 | 170 | 38305 | 50.88 |

Conclusions

- Applications of different criticality levels can be integrated onto the same architecture only if there is enough separation:
 - Separation at PE-level achieved with IMA.
 - Separation at network-level using TTEthernet.
- We proposed a Tabu Search based optimization of task mapping and allocation to partitions, and of time partitions.
- Only by optimizing the implementation of the applications, taking into account the particularities of IMA and TTEthernet, are we able to support the designer in obtaining schedulable implementations.

