

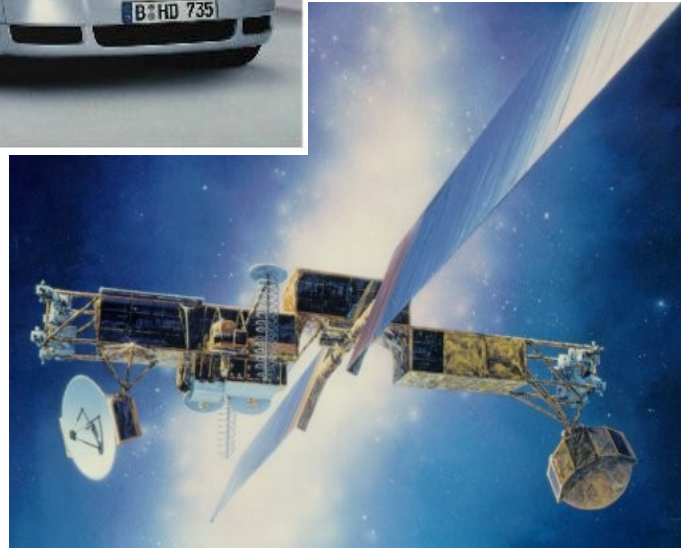
Scheduling and Voltage Scaling for Energy/Reliability Trade-offs in Fault-Tolerant Time-Triggered Embedded Systems

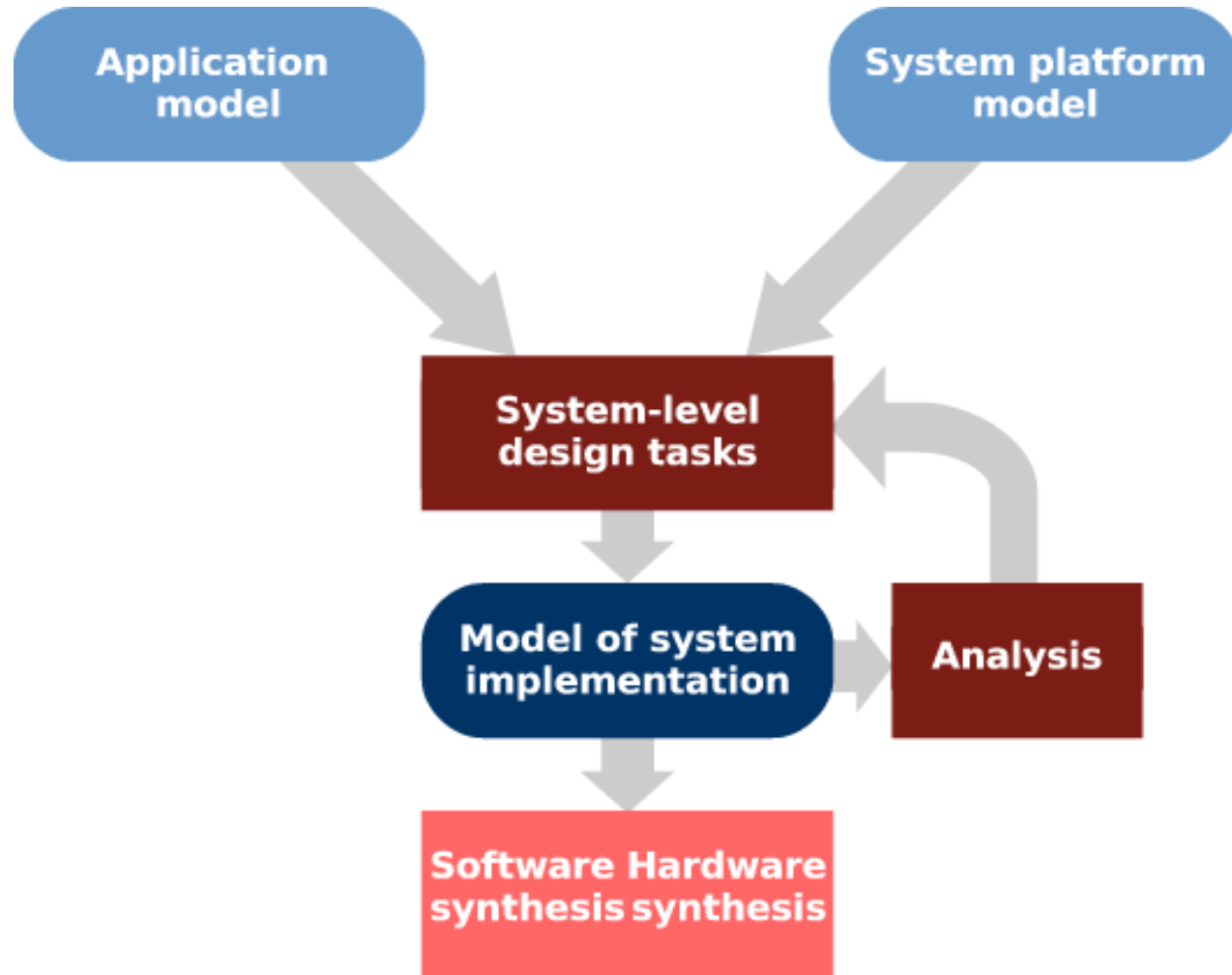
Kåre Harbo Poulsen,

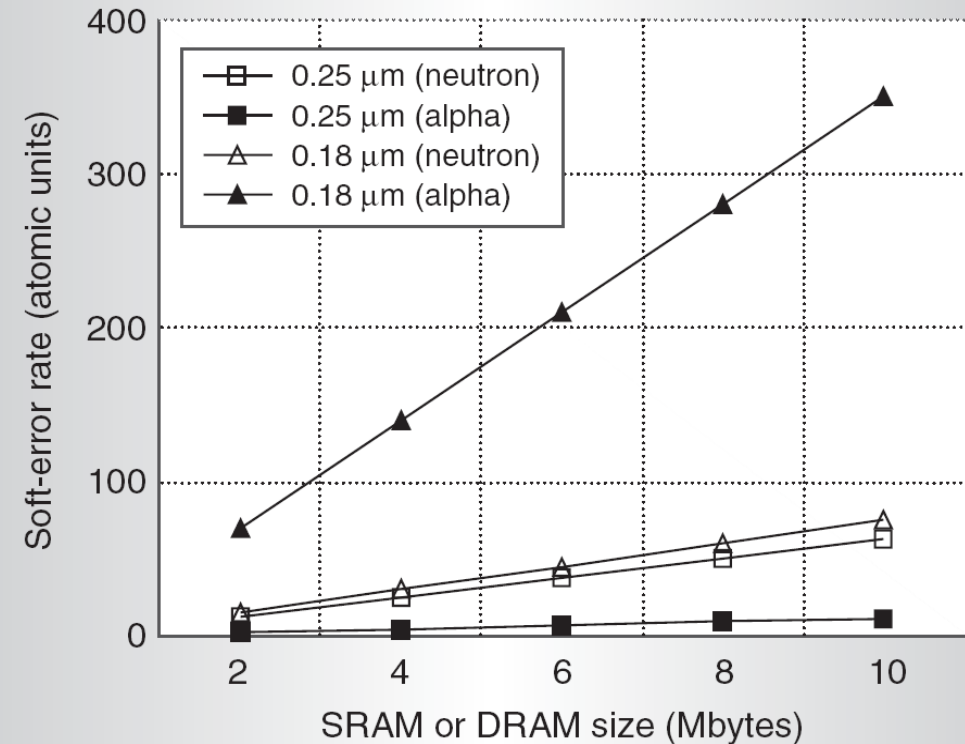
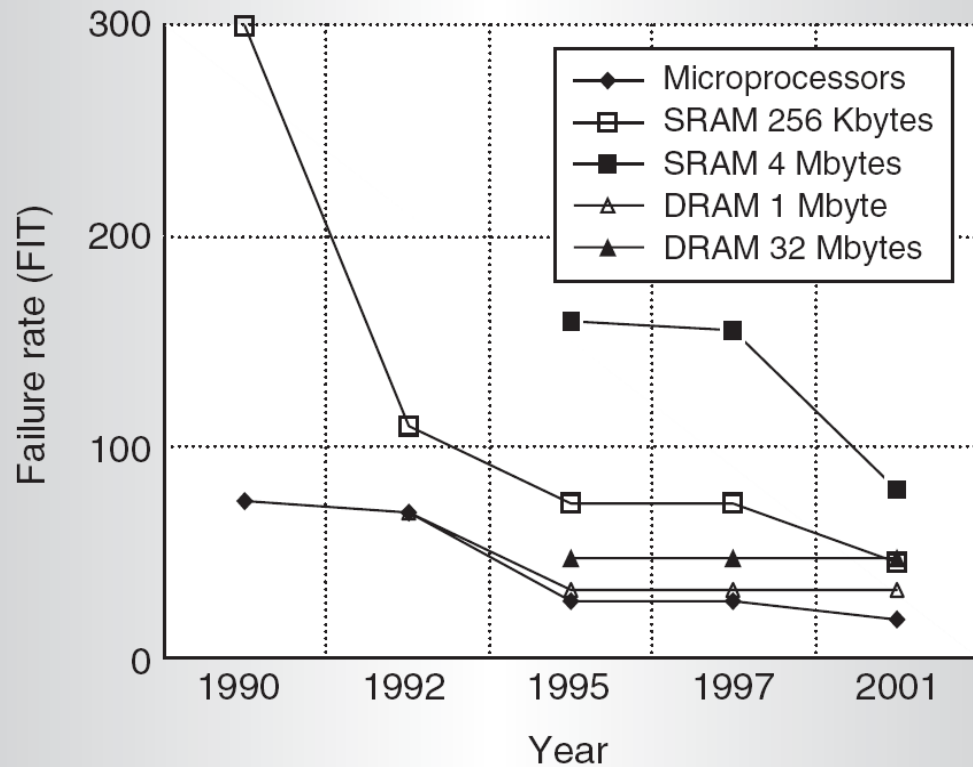
Paul Pop, Viacheslav Izosimov

August 23, 2007

Embedded Systems

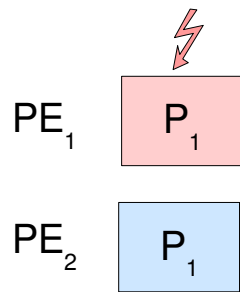




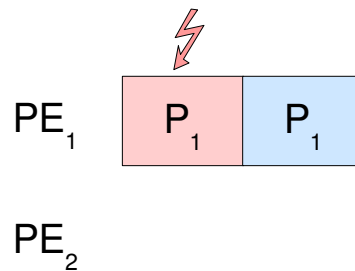


- Permanent faults are decreasing
- Transient faults are increasing

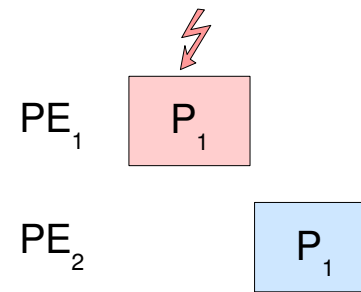
- Tolerate faults gracefully
- Expressions for reliability for fault-tolerance



Replication



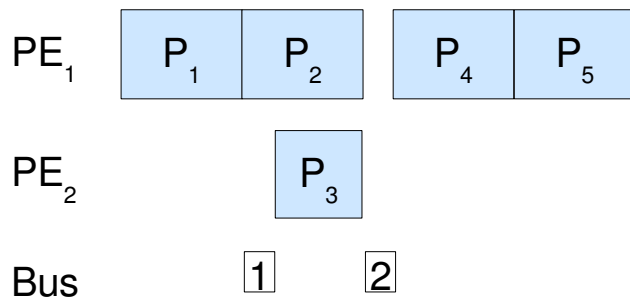
Re-execution



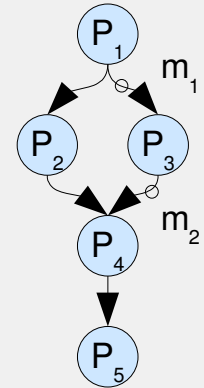
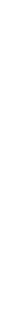
Passive Replication

- Input
 - Application
 - Architecture
 - Reliability goal: 0.999 999 999

$$R_0 = 0.999\ 981$$

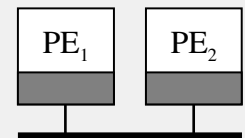


Deadline



PE₁ PE₂

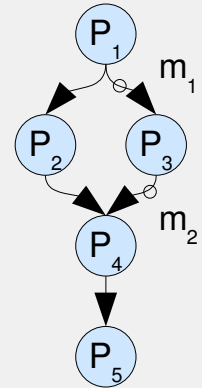
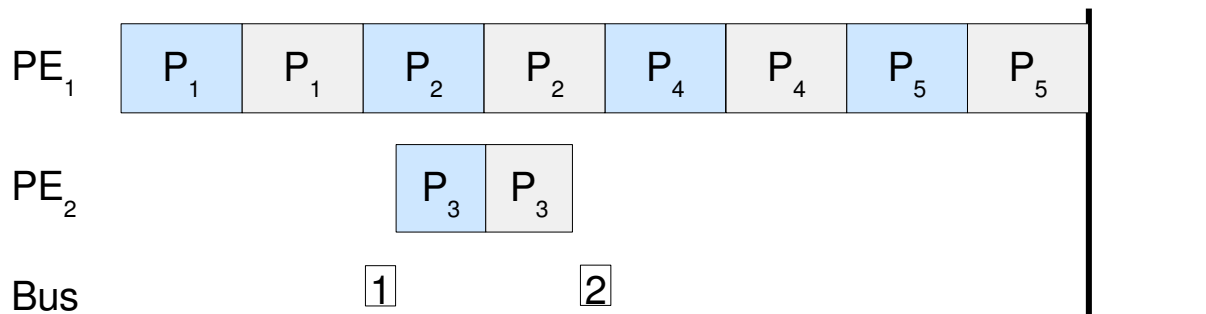
P ₁	4	4
P ₂	4	4
P ₃	3	3
P ₄	4	4
P ₅	4	4



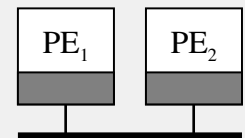
k=1

- Input
 - Application
 - Architecture
 - Reliability goal: 0.999 999 999
- Fault-tolerance for $k=1$ faults

$$R_0 = 0.999\ 999\ 999\ 927$$

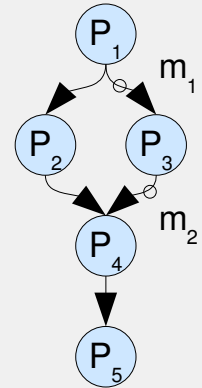
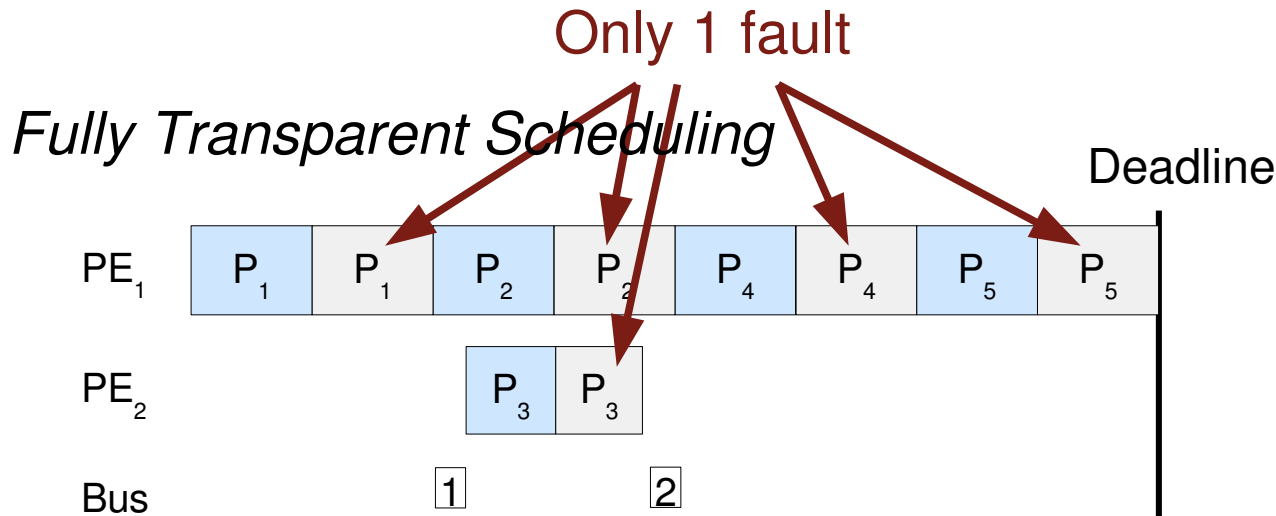


	PE ₁	PE ₂
P ₁	4	4
P ₂	4	4
P ₃	3	3
P ₄	4	4
P ₅	4	4

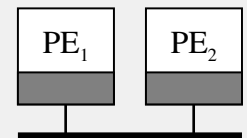


$k=1$

- Fault tolerant scheduler
 - Full transparency
 - Good debugability
 - Little memory

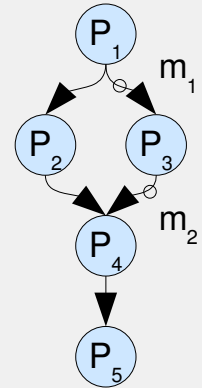
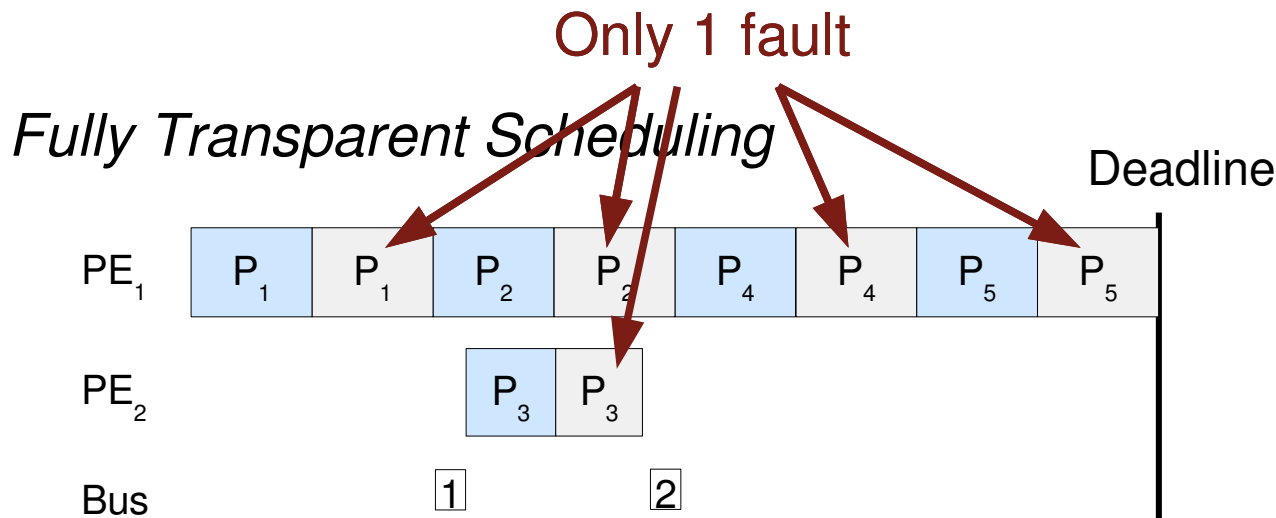


	PE ₁	PE ₂
P ₁	4	4
P ₂	4	4
P ₃	3	3
P ₄	4	4
P ₅	4	4

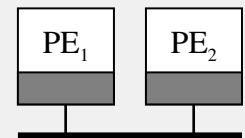


⚡
k=1

- Can be done faster
 - Sacrifice local transparency

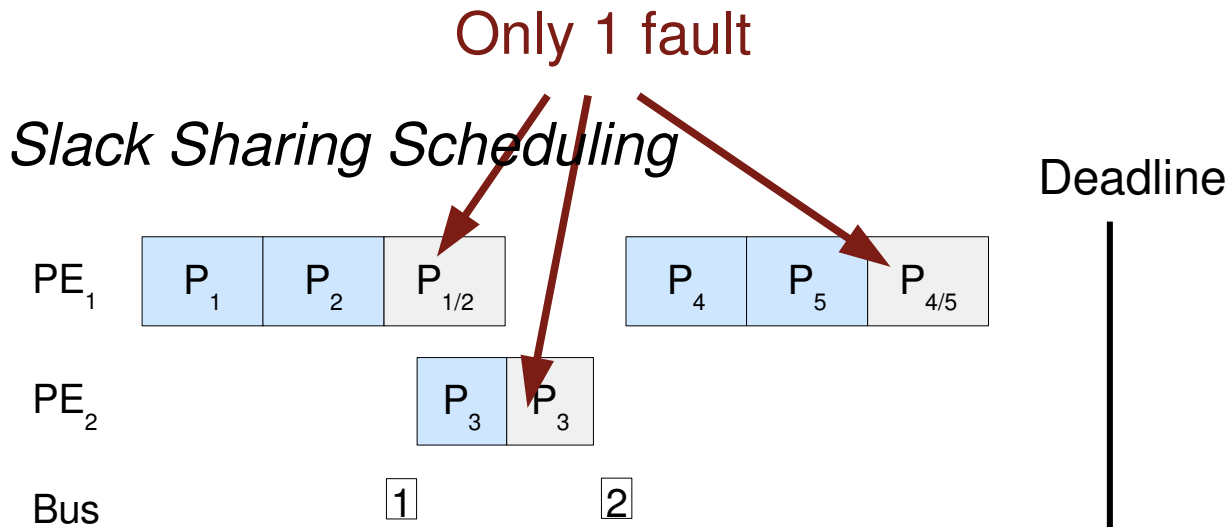
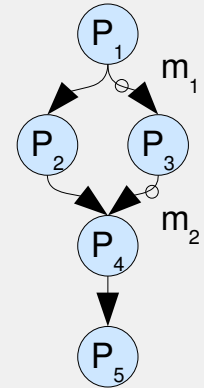


	PE ₁	PE ₂
P ₁	4	4
P ₂	4	4
P ₃	3	3
P ₄	4	4
P ₅	4	4

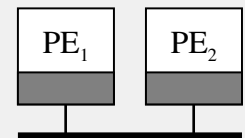



$k=1$

- Can be done faster
 - Sacrifice local transparency
 - More complex online scheduler



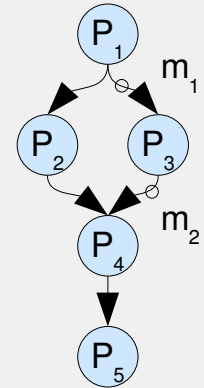
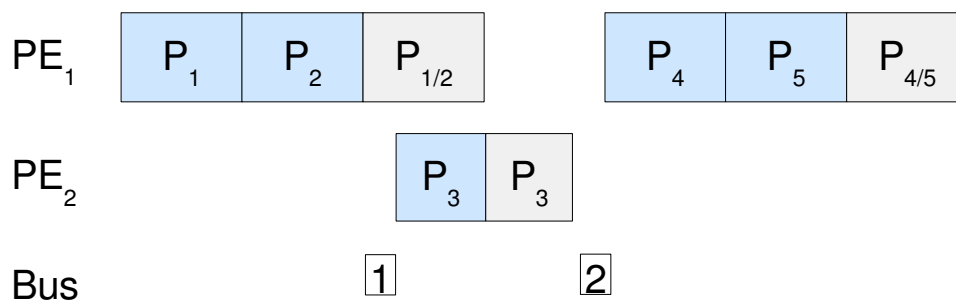
	PE ₁	PE ₂
P ₁	4	4
P ₂	4	4
P ₃	3	3
P ₄	4	4
P ₅	4	4



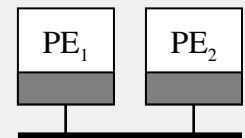
 $k=1$

- Even faster
 - Sacrifice all transparency
 - Schedule for each fault scenario

Slack Sharing Scheduling

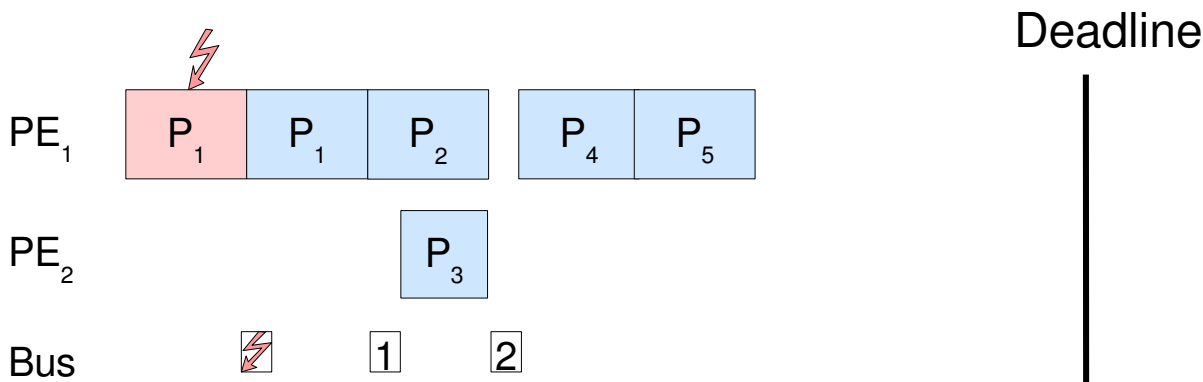
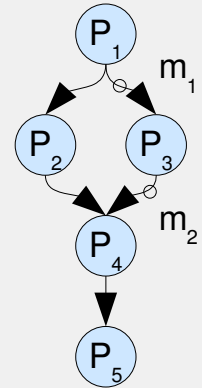


	PE ₁	PE ₂
P ₁	4	4
P ₂	4	4
P ₃	3	3
P ₄	4	4
P ₅	4	4

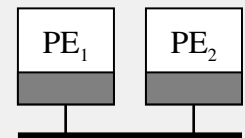


⚡
k=1

- Even faster
 - Sacrifice all transparency
 - Schedule for each fault scenario
 - At most k re-executions

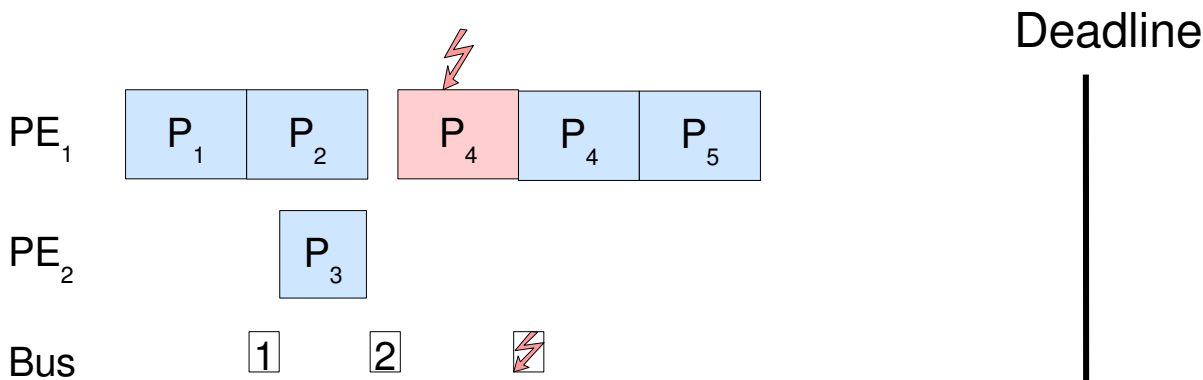
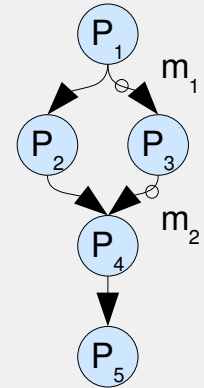


	PE ₁	PE ₂
P ₁	4	4
P ₂	4	4
P ₃	3	3
P ₄	4	4
P ₅	4	4

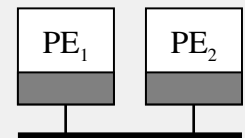


$k=1$

- Even faster
 - Sacrifice all transparency
 - Schedule for each fault scenario
 - At most k re-executions



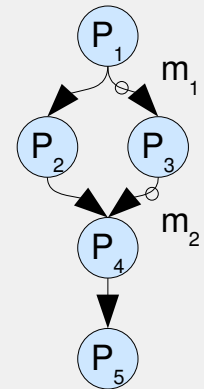
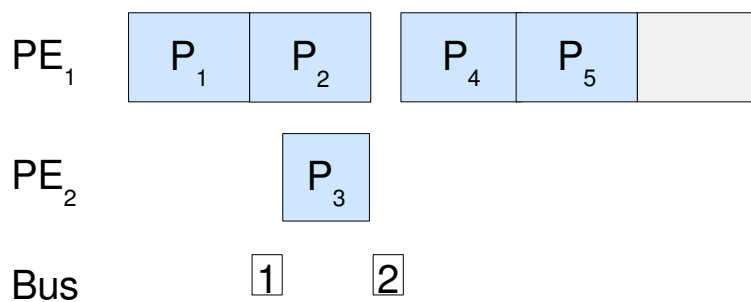
	PE ₁	PE ₂
P ₁	4	4
P ₂	4	4
P ₃	3	3
P ₄	4	4
P ₅	4	4



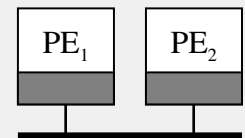
⚡
 $k=1$

- Even faster
 - Sacrifice all transparency
 - Schedule for each fault scenario
 - At most k re-executions
 - All faults information is shared

Conditional Scheduling



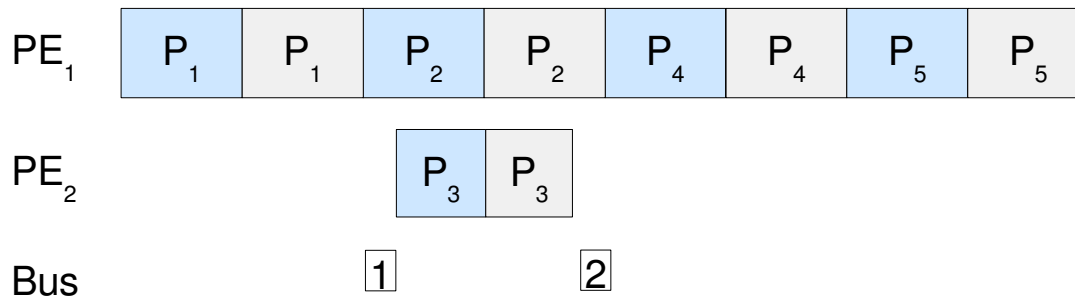
	PE ₁	PE ₂
P ₁	4	4
P ₂	4	4
P ₃	3	3
P ₄	4	4
P ₅	4	4



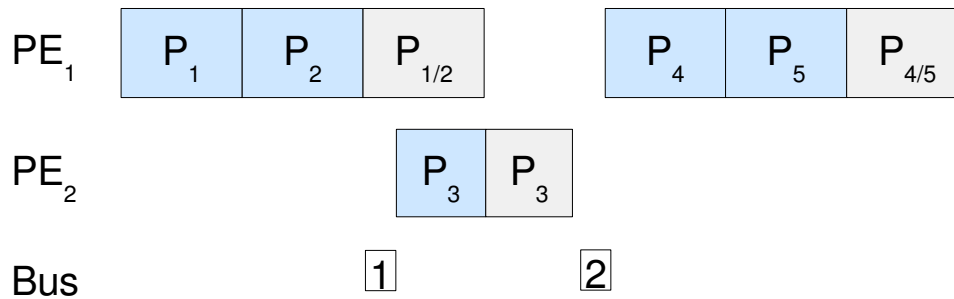
$k=1$

Fully Transparent Scheduling

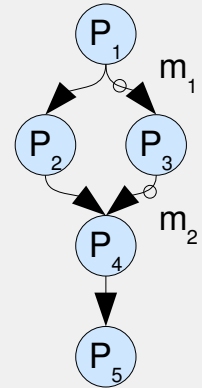
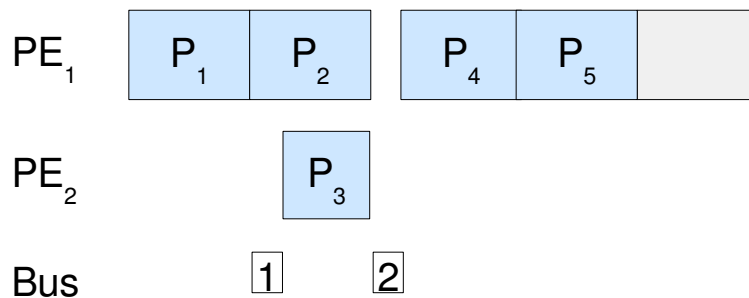
Deadline



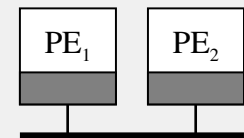
Slack Sharing Scheduling



Conditional Scheduling

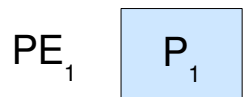


	PE ₁	PE ₂
P ₁	4	4
P ₂	4	4
P ₃	3	3
P ₄	4	4
P ₅	4	4



k=1

- Goal: minimise energy consumption
 - Dynamic voltage scaling



PE₂

100% V_{ss}

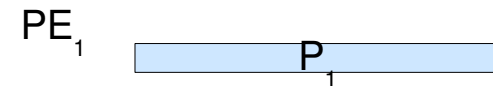
100% E_0



PE₂

66% V_{ss}

44% E_0



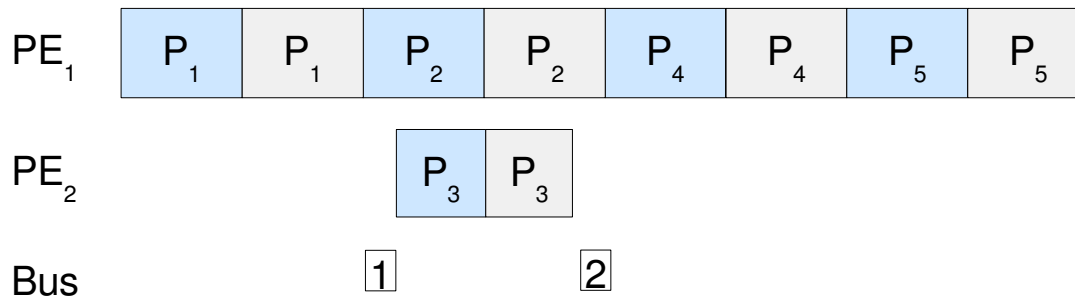
PE₂

33% V_{ss}

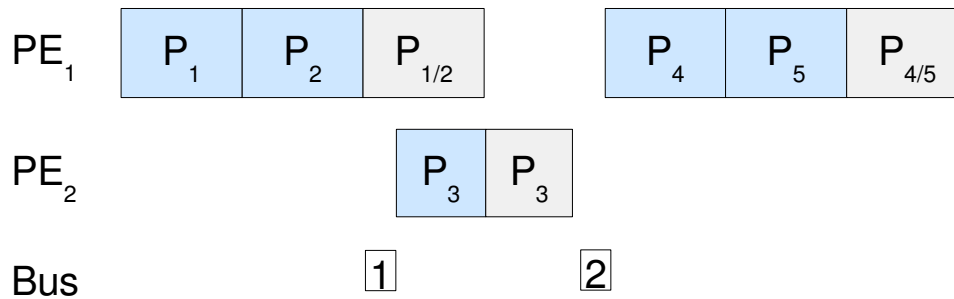
11% E_0

Fully Transparent Scheduling

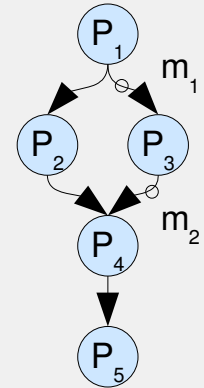
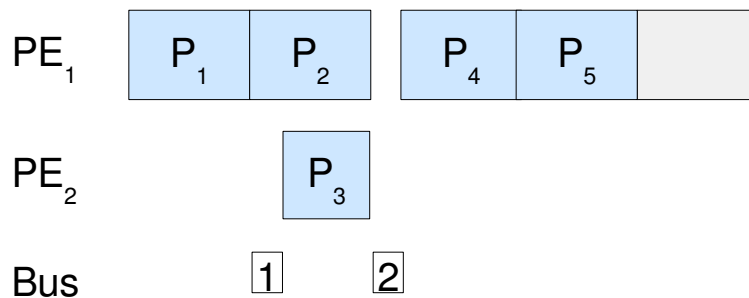
Deadline



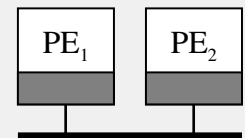
Slack Sharing Scheduling



Conditional Scheduling

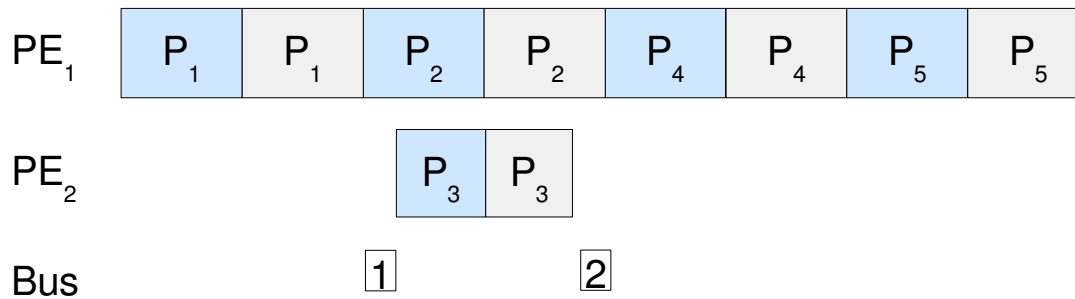


	PE ₁	PE ₂
P ₁	4	4
P ₂	4	4
P ₃	3	3
P ₄	4	4
P ₅	4	4



k=1

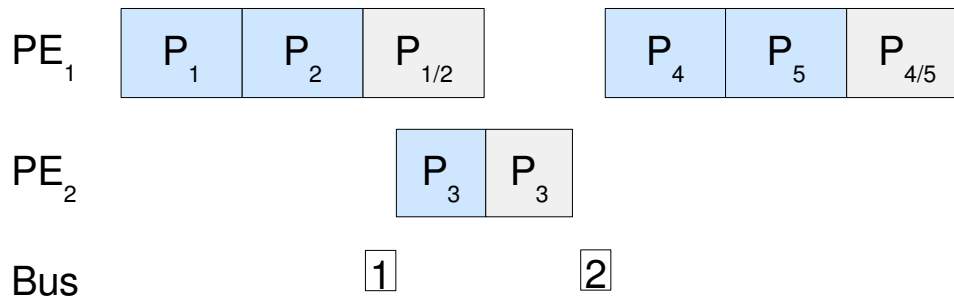
Fully Transparent Scheduling



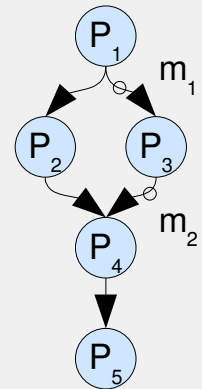
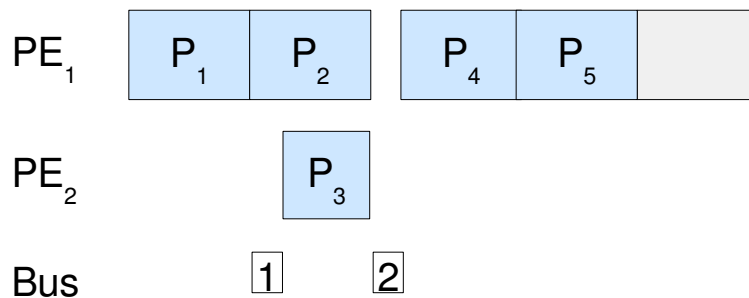
Deadline

100% E₀

Slack Sharing Scheduling

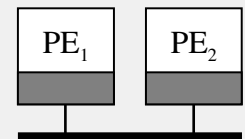


Conditional Scheduling



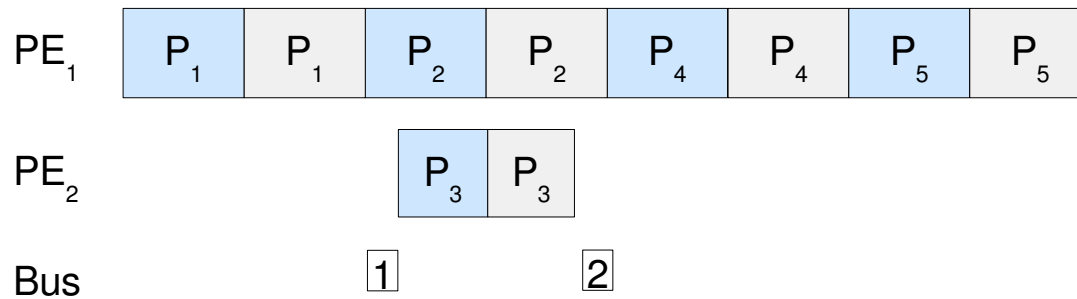
PE₁ PE₂

P ₁	4	4
P ₂	4	4
P ₃	3	3
P ₄	4	4
P ₅	4	4



k=1

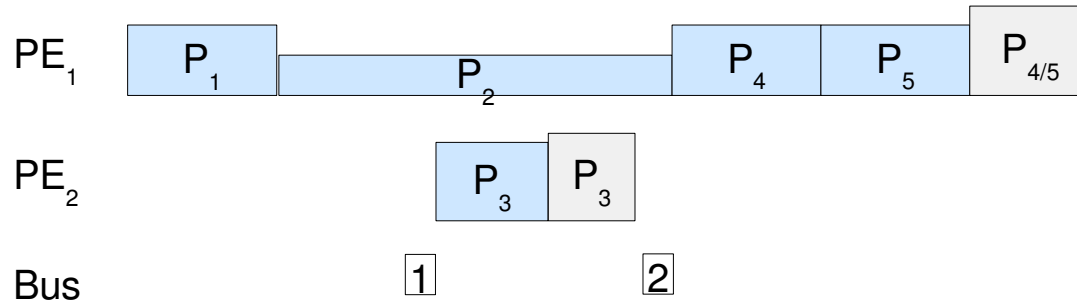
Fully Transparent Scheduling



Deadline

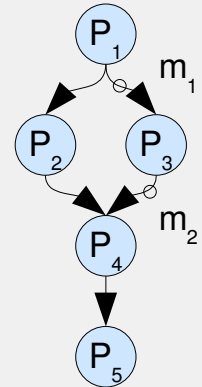
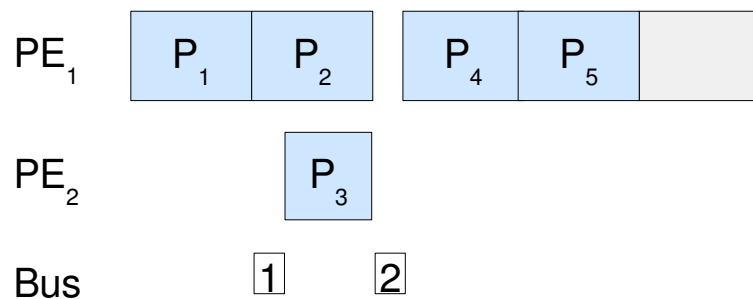
100% E_0

Slack Sharing Scheduling



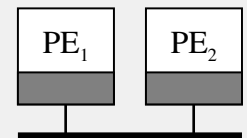
63% E_0

Conditional Scheduling



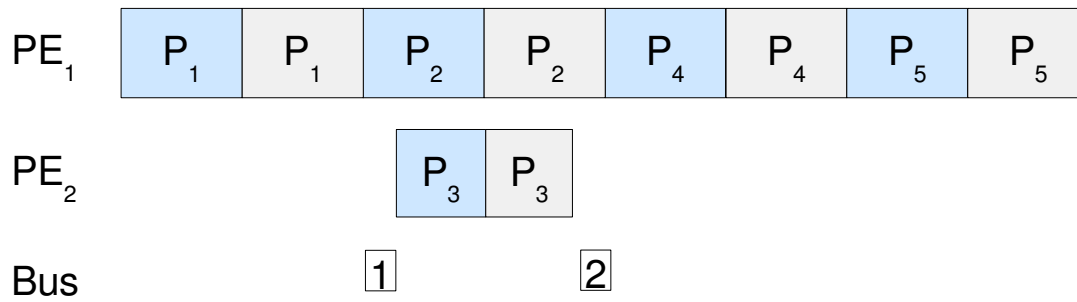
PE₁ PE₂

P ₁	4	4
P ₂	4	4
P ₃	3	3
P ₄	4	4
P ₅	4	4



$k=1$

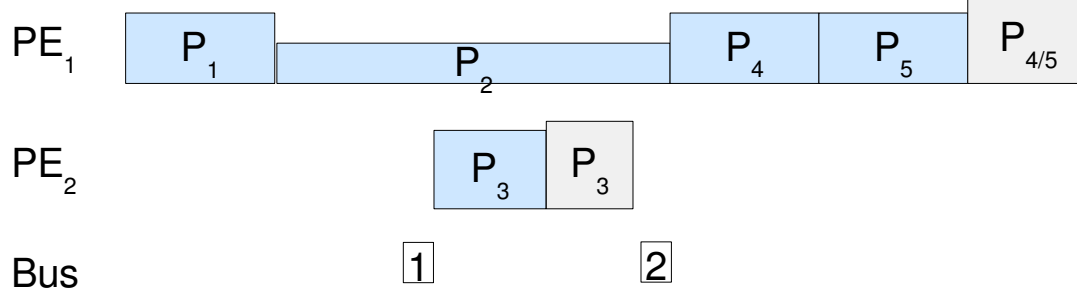
Fully Transparent Scheduling



Deadline

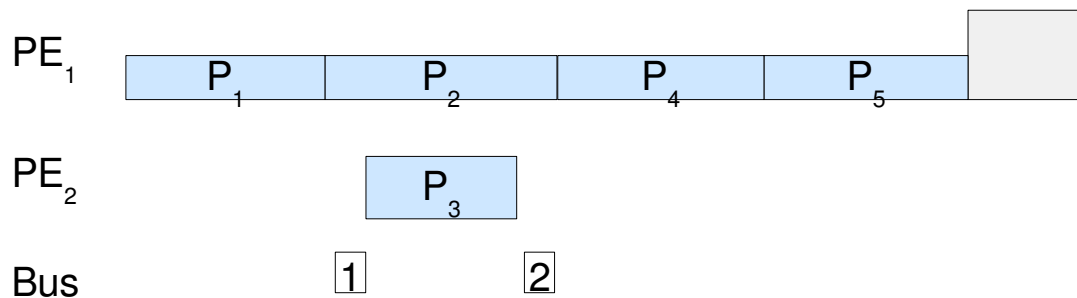
100% E_0

Slack Sharing Scheduling

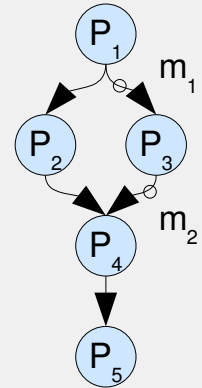


63% E_0

Conditional Scheduling

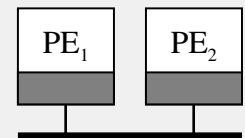


38% E_0



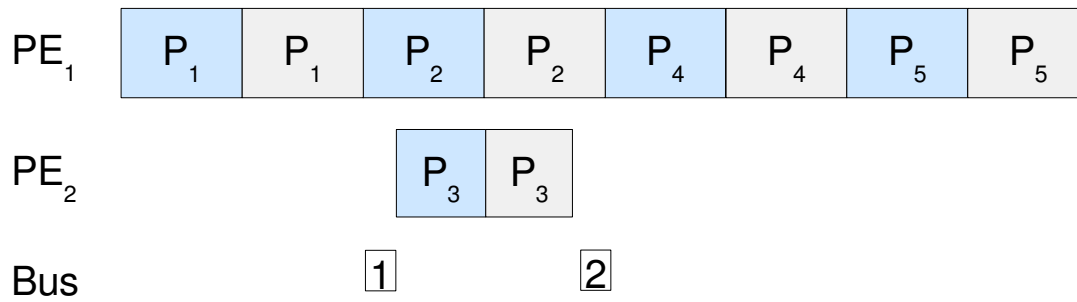
PE₁ PE₂

P ₁	4	4
P ₂	4	4
P ₃	3	3
P ₄	4	4
P ₅	4	4



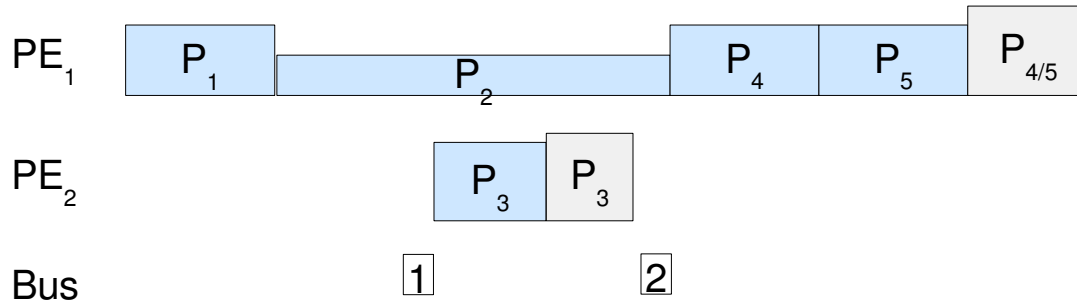
$k=1$

Fully Transparent Scheduling



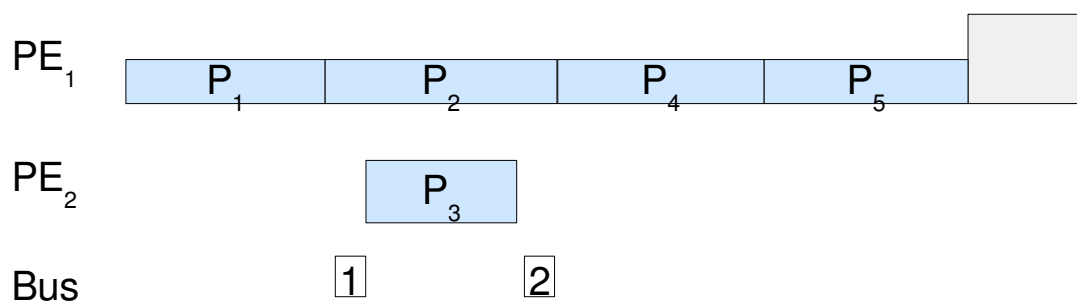
100% E_0

Slack Sharing Scheduling

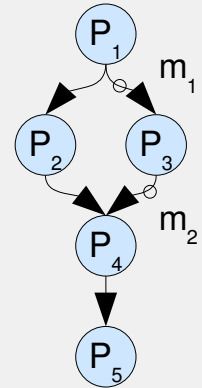


63% E_0

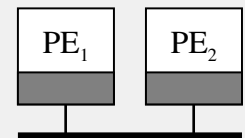
Conditional Scheduling



38% E_0



	PE ₁	PE ₂
P ₁	4	4
P ₂	4	4
P ₃	3	3
P ₄	4	4
P ₅	4	4



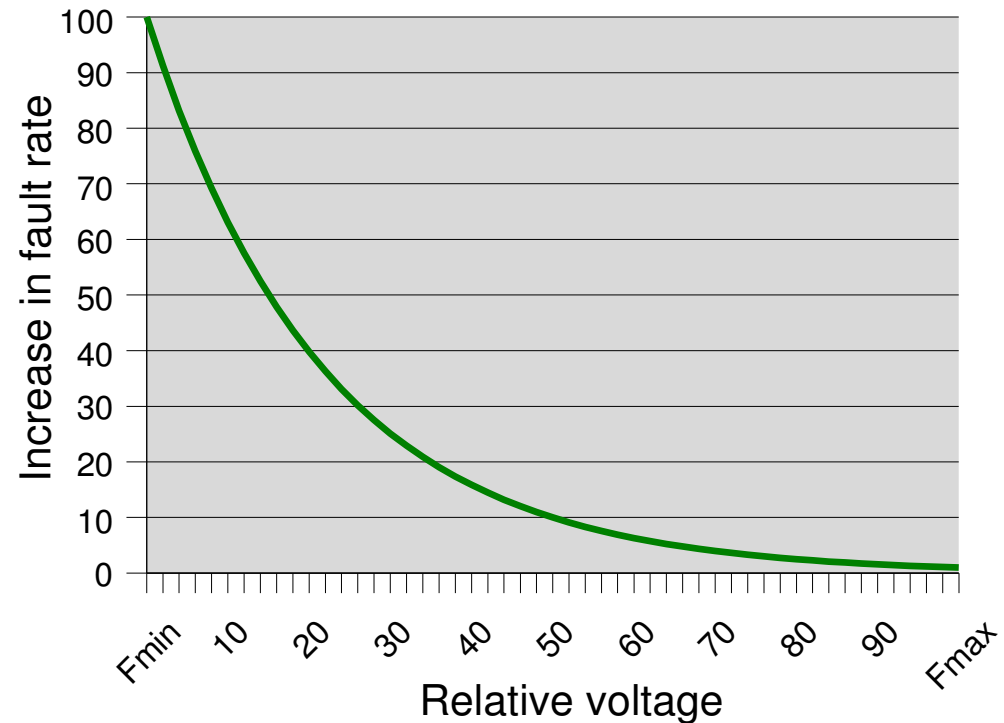
$k=1$

- Lower voltage
 - Critical energy is lowered
 - Probability of faults increases
 - Circuit operates slower
- Lower frequency
 - Longer execution time
 - Probability of faults increases

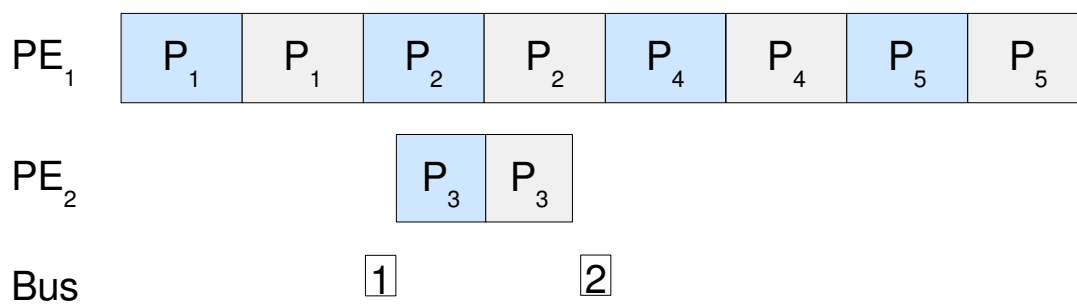
- Exponential model

$$\lambda(f) = \lambda_0 10^{\frac{d(1-f)}{1-f_{min}}}$$

Failure rate vs. Voltage



Fully Transparent Scheduling

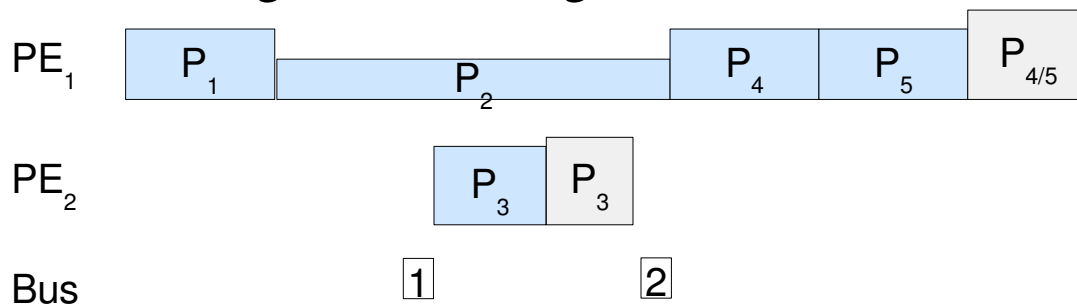


Deadline

R=0.999 999 999 93

100% E₀

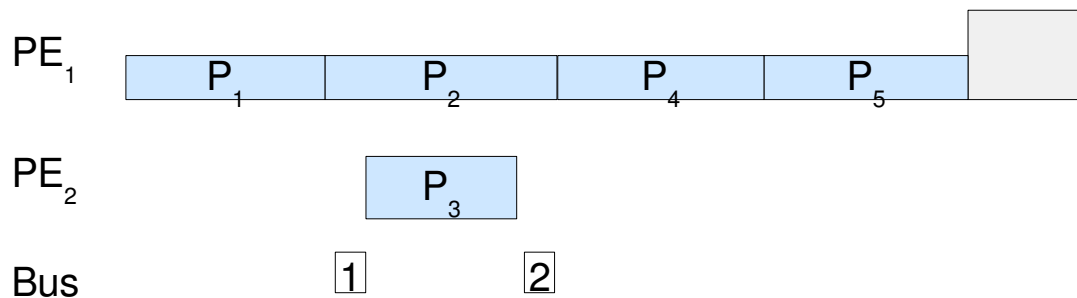
Slack Sharing Scheduling



R=0.999 999 999 25

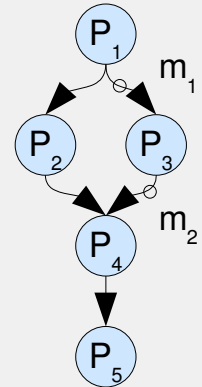
63% E₀

Conditional Scheduling

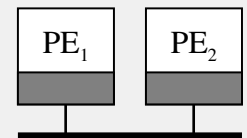


R=0.999 999 958 208

38% E₀

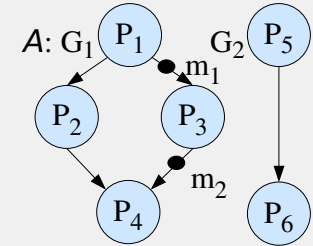


	PE ₁	PE ₂
P ₁	4	4
P ₂	4	4
P ₃	3	3
P ₄	4	4
P ₅	4	4

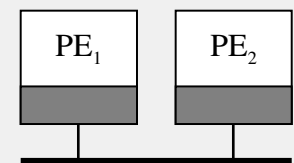


$k=1$

- Reliability goal: 0.999 999 9



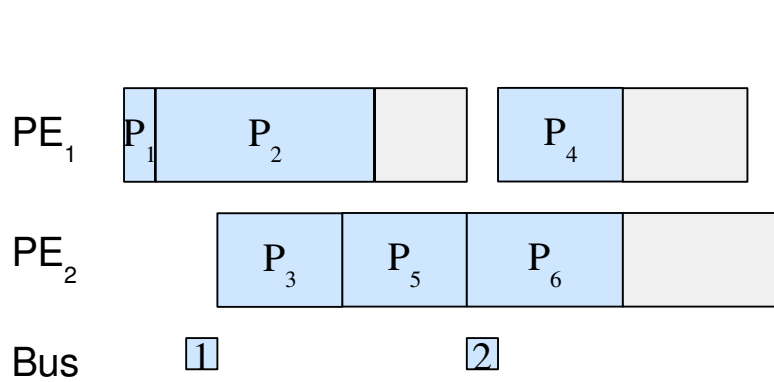
	N ₁	N ₂
P ₁	10	X
P ₂	70	X
P ₃	X	40
P ₄	40	X
P ₅	X	40
P ₆	X	50



Voltage levels

N ₁	100%	66%	33%
N ₂	100%	66%	33%

k = 1 ⚡

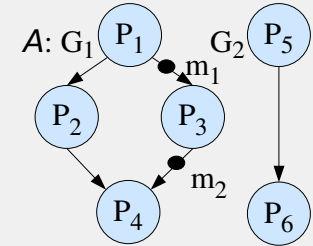


Deadline

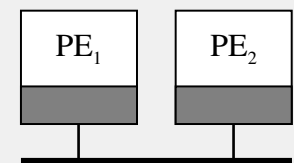
R=0.999 999 987

100% E₀

- Reliability goal: 0.999 999 9
- Set reliability as hard constraint



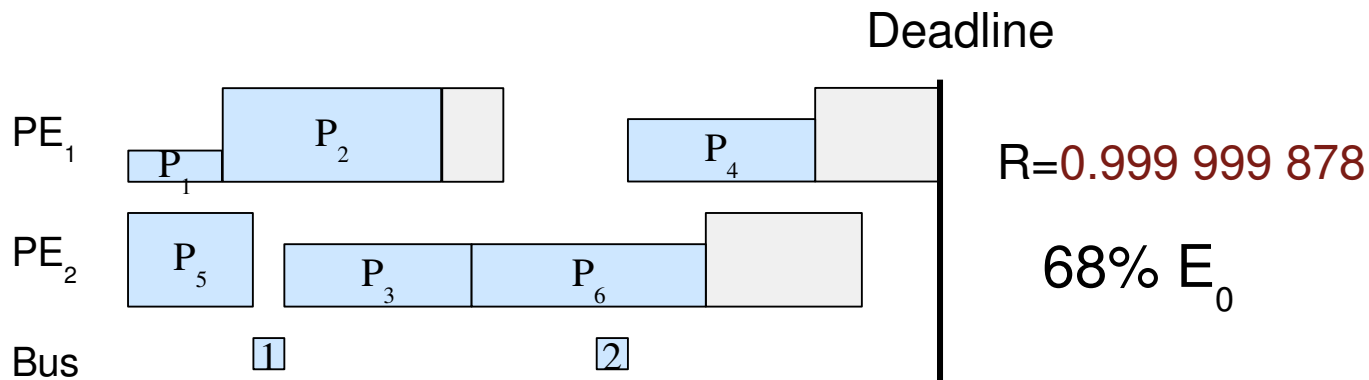
	N_1	N_2
P_1	10	X
P_2	70	X
P_3	X	40
P_4	40	X
P_5	X	40
P_6	X	50



Voltage levels

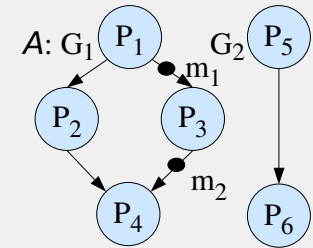
N_1	100%	66%	33%
N_2	100%	66%	33%

$k = 1$ ⚡

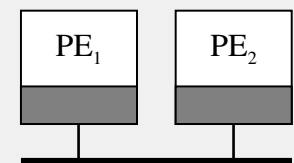


Energy/Reliability Trade-off

- Reliability goal: 0.999 999 9
- Set reliability as hard constraint
- Trade-off 5% energy
- Meets reliability goal



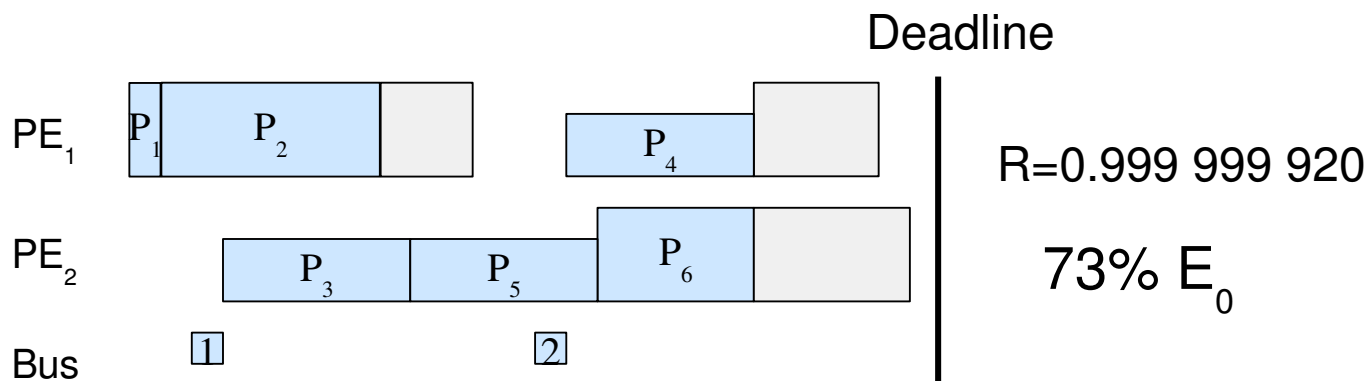
	N_1	N_2
P_1	10	X
P_2	70	X
P_3	X	40
P_4	40	X
P_5	X	40
P_6	X	50



Voltage levels

N_1	100%	66%	33%
N_2	100%	66%	33%

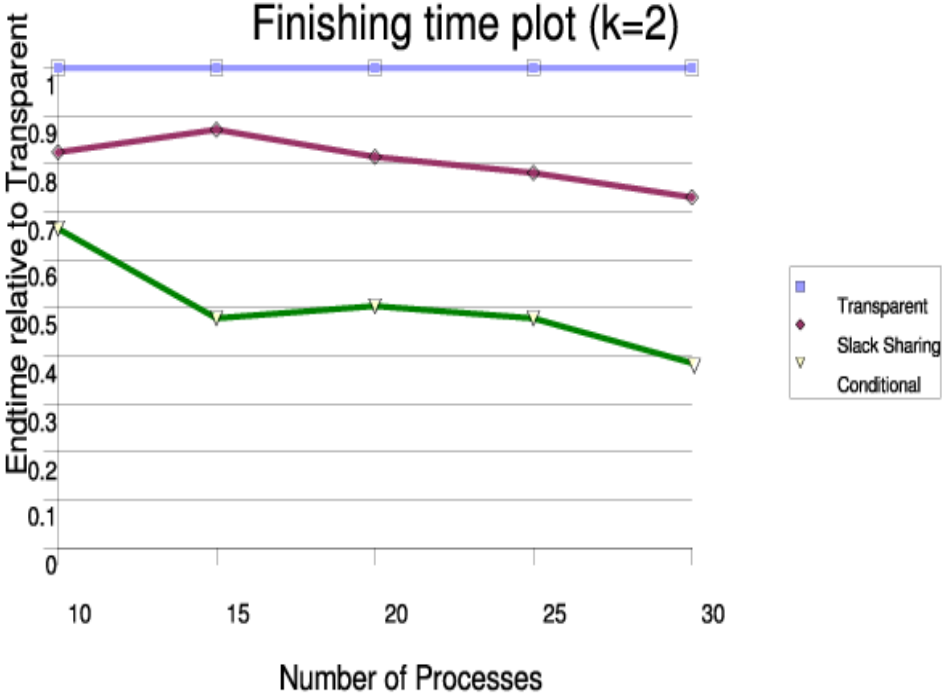
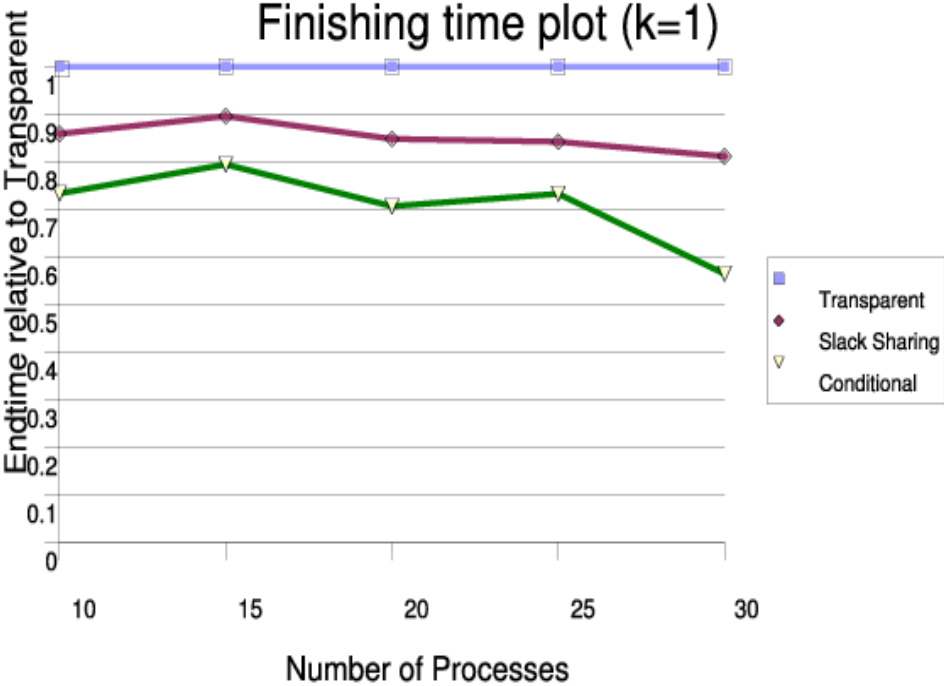
$k = 1$ ⚡



- Input
 - Application
 - Architecture
 - Reliability goal
- Decide
 - Fault-Tolerant Scheduling
 - Mapping
 - Fault-Tolerance Policy
- While optimising for
 - Energy
 - Under hard reliability goal

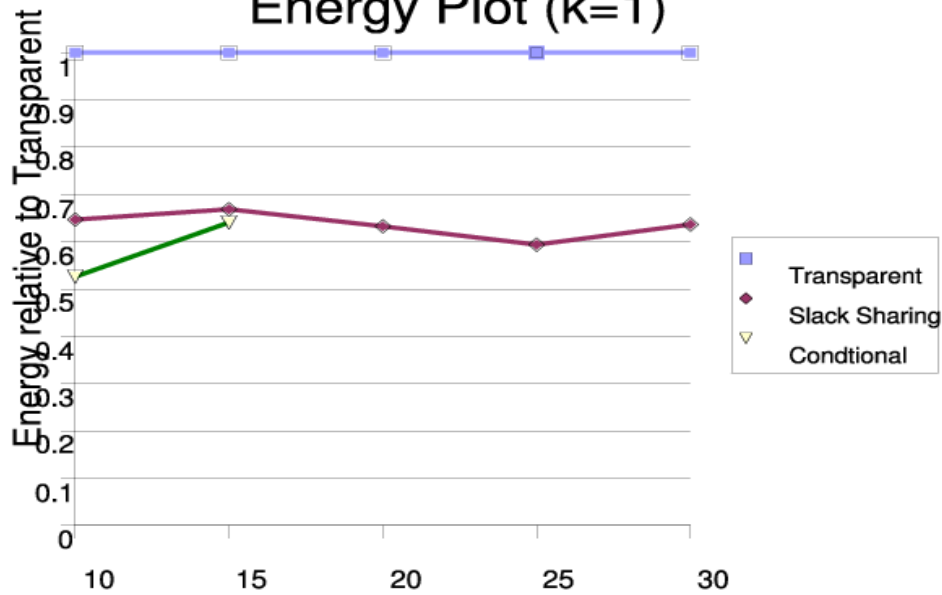
- Problem is NP-Complete
 - Normally solved using “best effort” heuristics
- Use constraint logic programming
 - Good performance with NP-completeness
 - Optimal solutions are feasible
 - Flexible model
 - ECLiPSe-CLP

Comparison of Schedulers

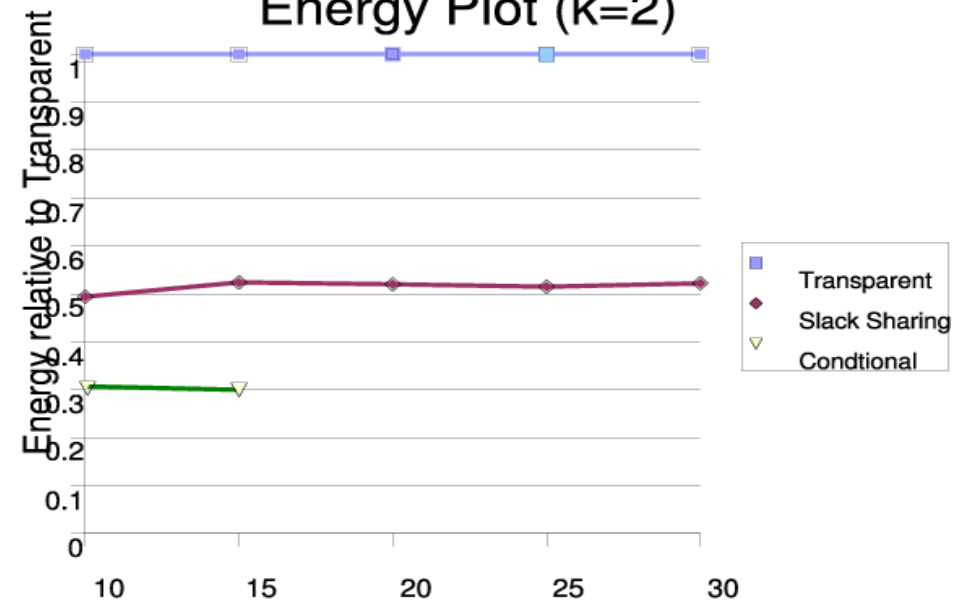


Comparison of Schedulers

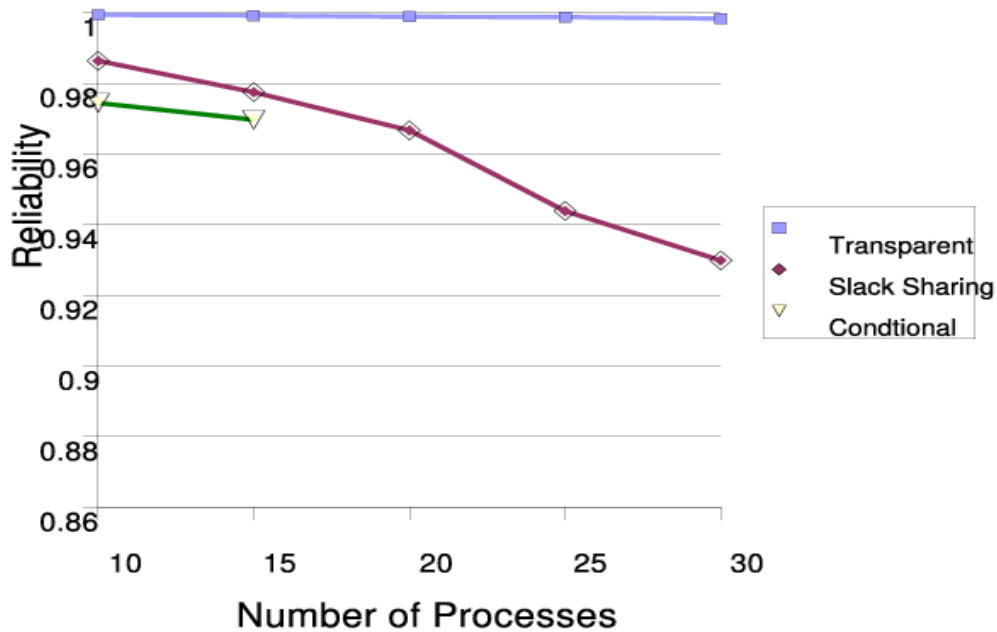
Energy Plot (k=1)



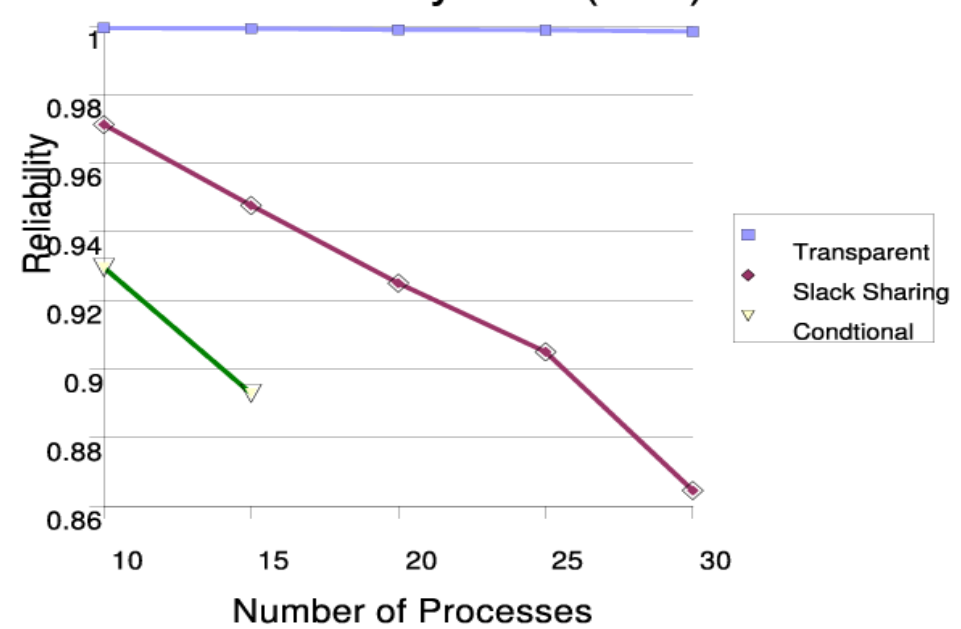
Energy Plot (k=2)



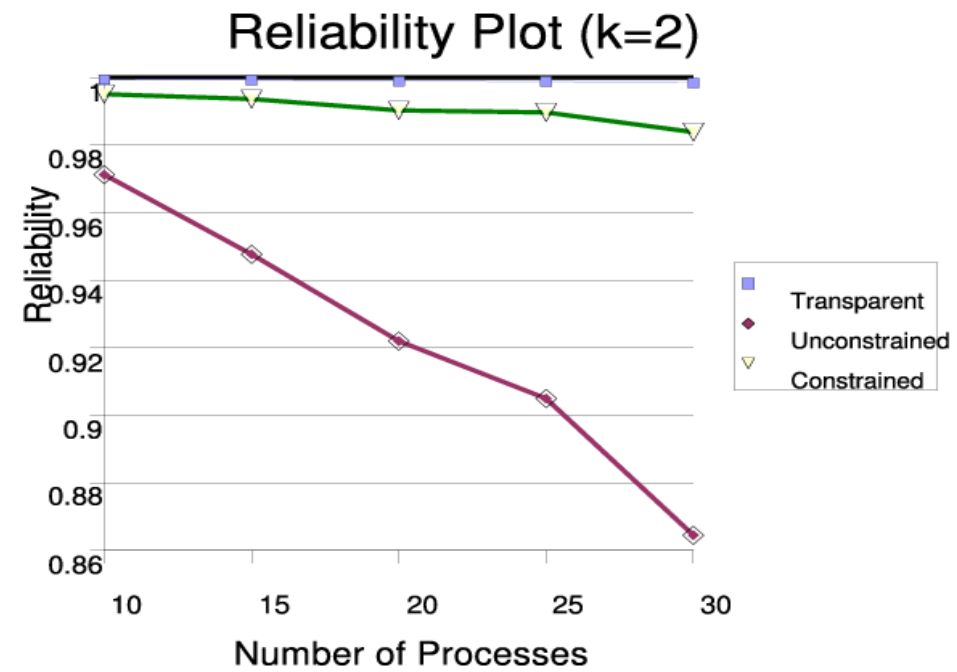
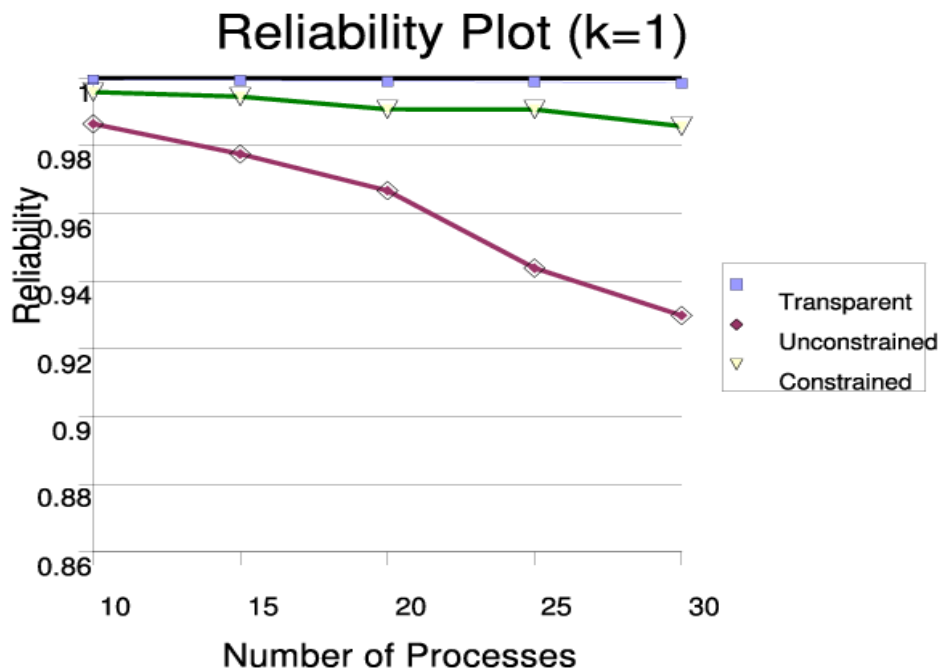
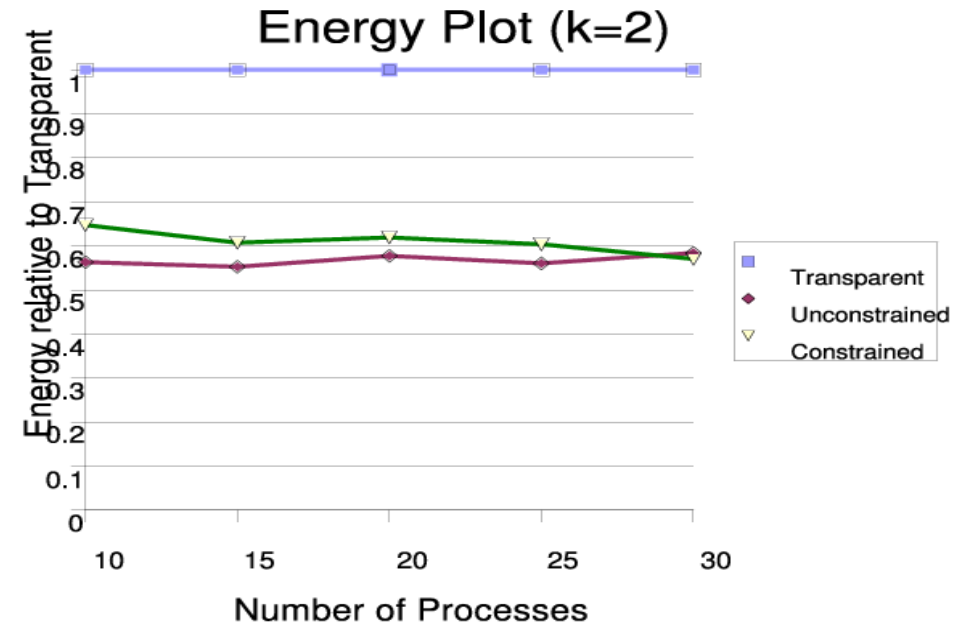
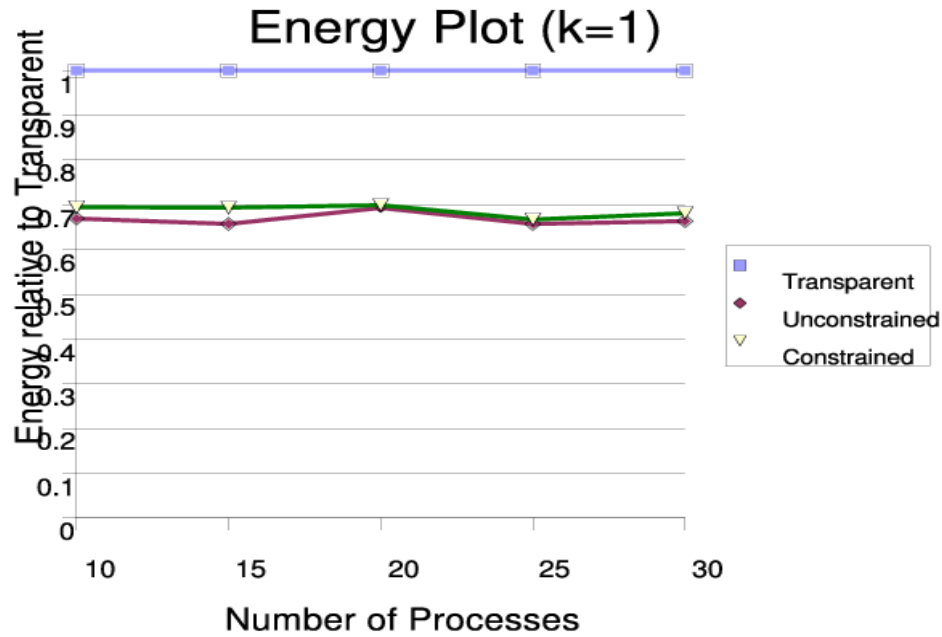
Reliability Plot (k=1)



Reliability Plot (k=2)



Reliability and Energy Trade-offs



- Design tool for doing
 - Fault tolerant scheduling
 - Mapping
 - Policy assignment
- Optimising for
 - Minimal energy
 - Hard constraints for timing and reliability
- Message:
 - Reliability can be met at little energy cost

Embedded Systems

