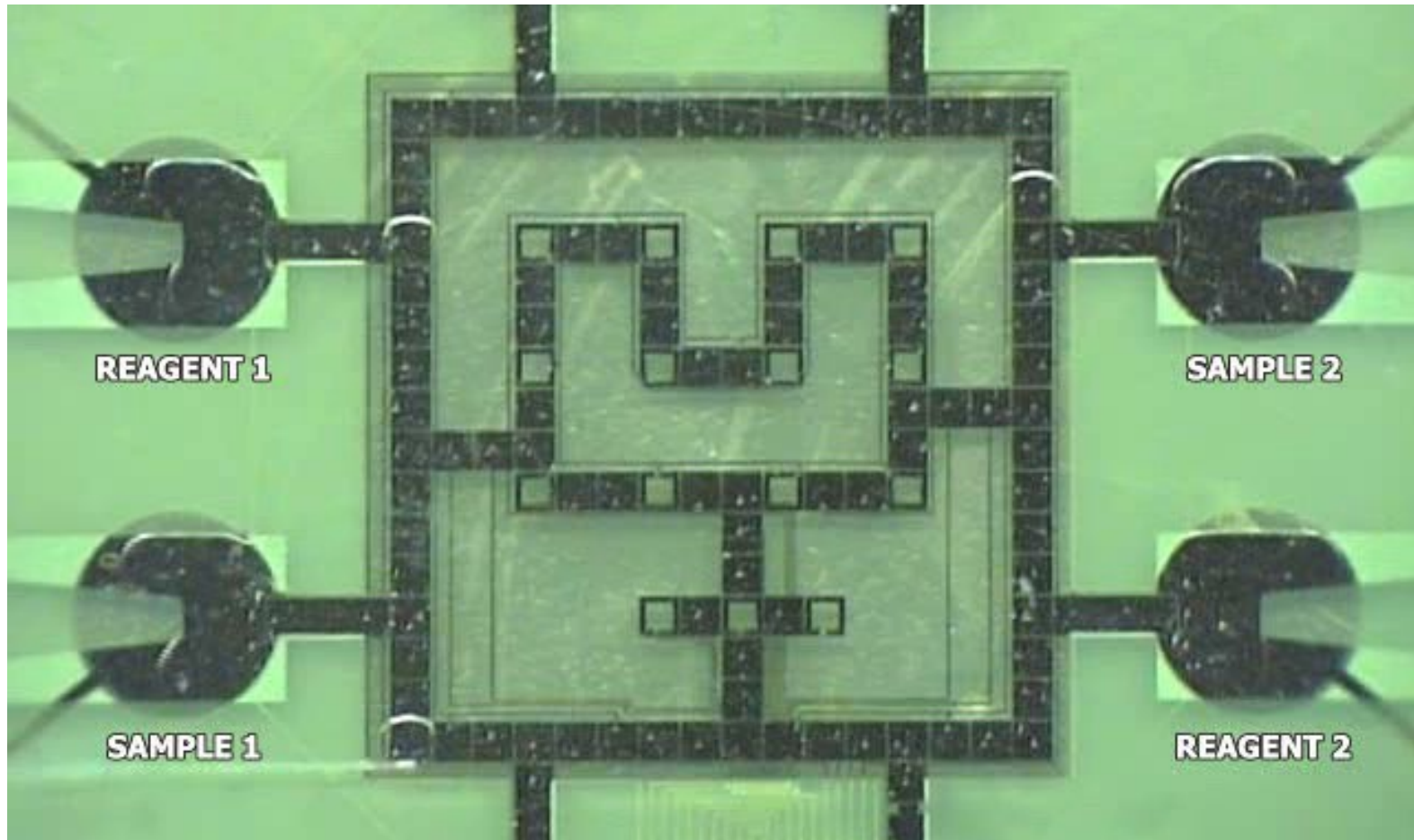


# Synthesis of Digital Microfluidic Biochips with Reconfigurable Operation Execution

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Technical University of Denmark  
DTU Informatics



# Digital Microfluidic Biochip



Duke University

# Applications

- Sampling and real time testing of air/water for biochemical toxins
- Food testing
- DNA analysis and sequencing
- Clinical diagnosis
- Point of care devices
- Drug development



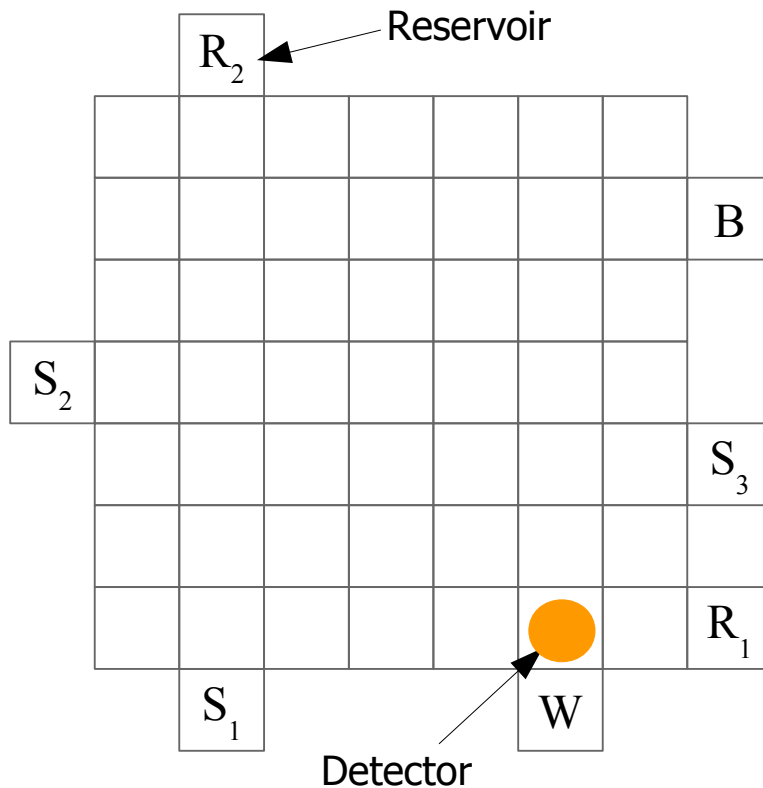
# Advantages & Challenges

- Advantages:
  - High throughput (reduced sample / reagent consumption)
  - Space (miniaturization)
  - Time (parallelism)
  - Automation (minimal human intervention)
- Challenges:
  - Design complexity
  - Radically different design and test methods required
  - Integration with microelectronic components in future SoCs

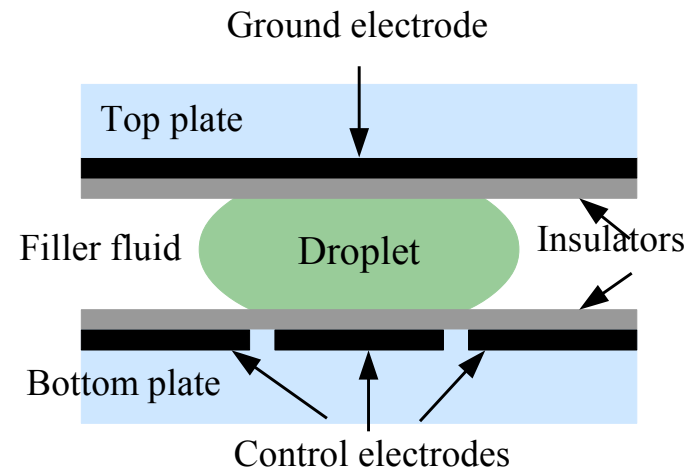
- Motivation
- Architecture
- Operation Execution
- Contribution I
  - Module-Based Synthesis with Dynamic Virtual Devices
- Contribution II
  - Routing-Based Synthesis
- Contribution III
  - Droplet-Aware Module-Based Synthesis
- Conclusions & Future Directions

# Architecture and Working Principles

## Biochip architecture

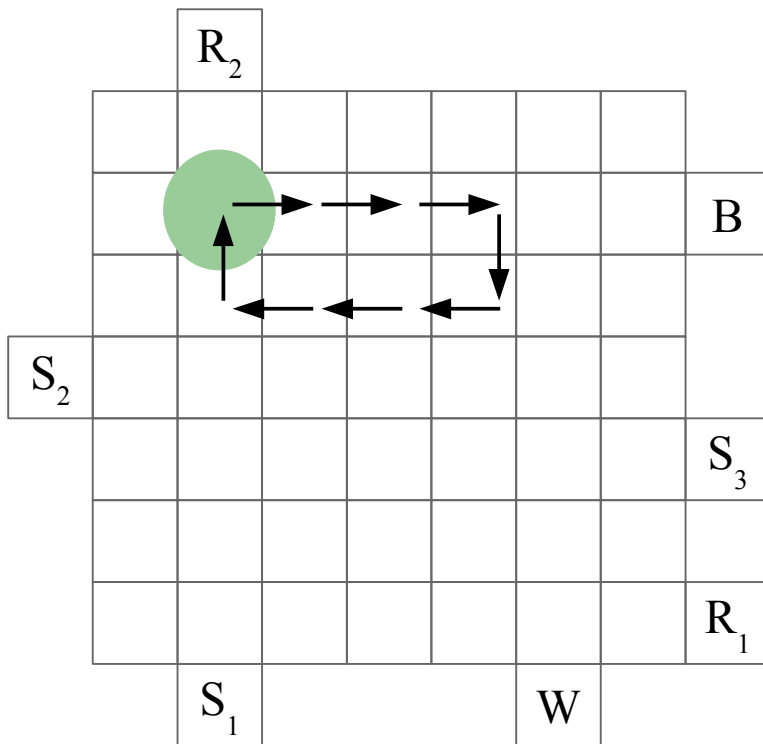


## Cell architecture



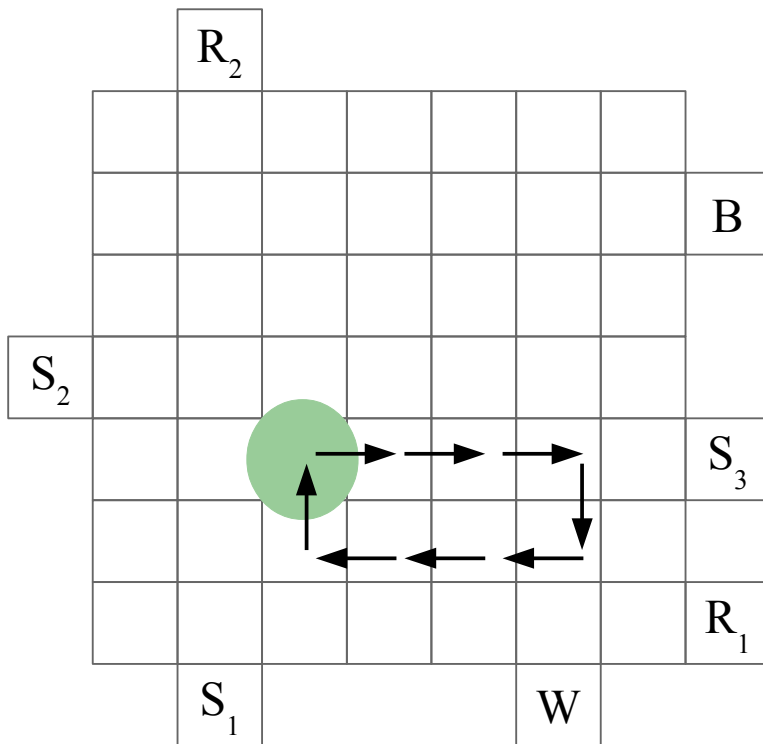
- Electrowetting-on-dielectric

# Microfluidic Operations



- Dispensing
- Detection
- Splitting/Merging
- Storage
- Mixing/Dilution

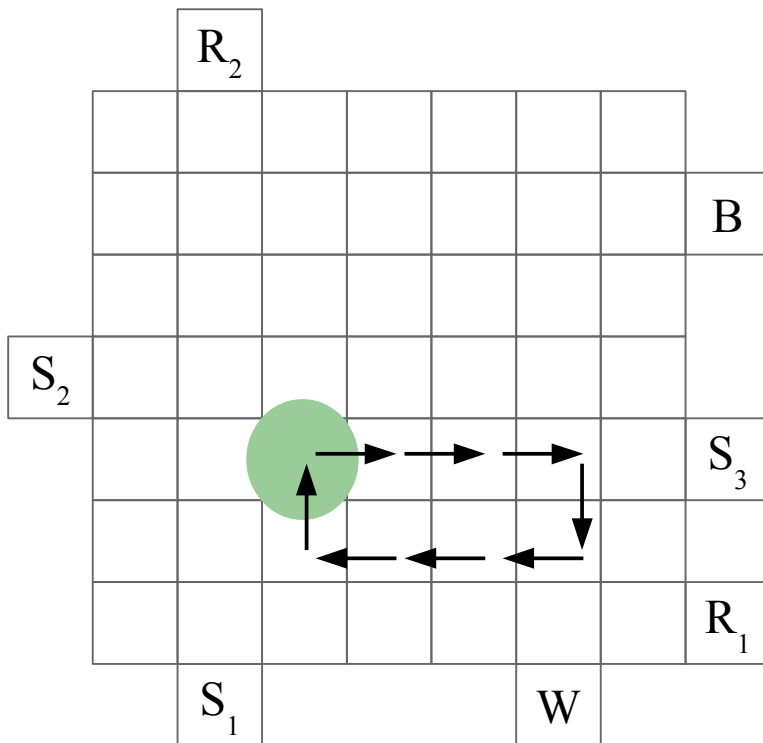
# Reconfigurability



- Dispensing
- Detection
- Splitting/Merging
- Storage
- Mixing/Dilution



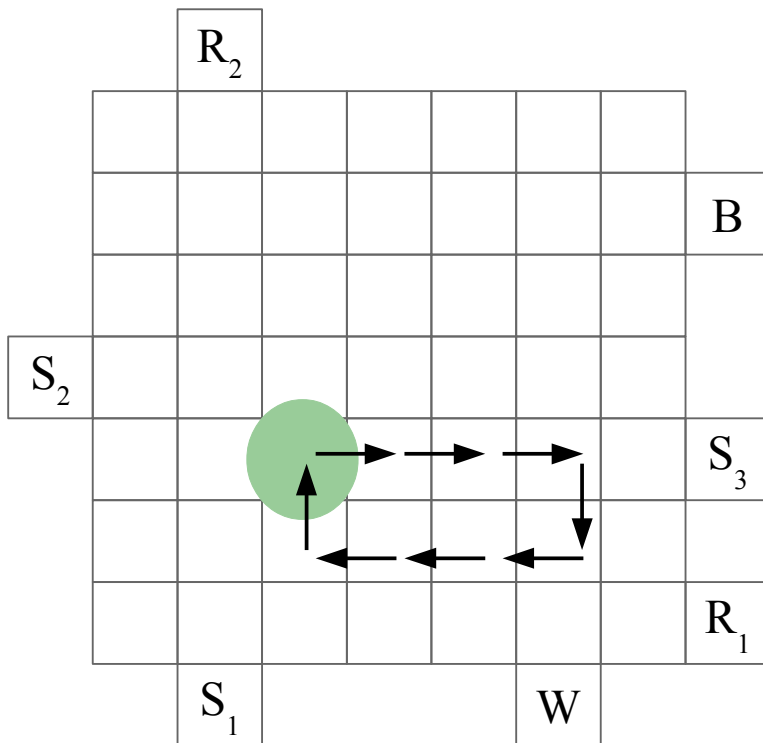
# Reconfigurability



## Non-reconfigurable

- Dispensing
- Detection
- Splitting/Merging
- Storage
- Mixing/Dilution

# Reconfigurability



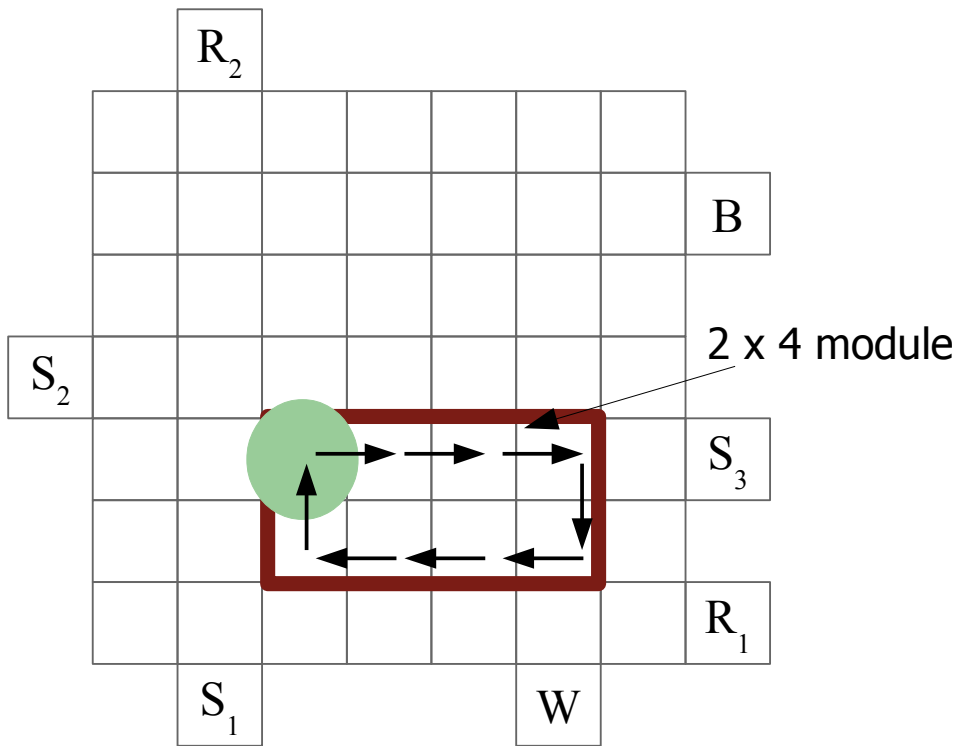
## Non-reconfigurable

- Dispensing
- Detection

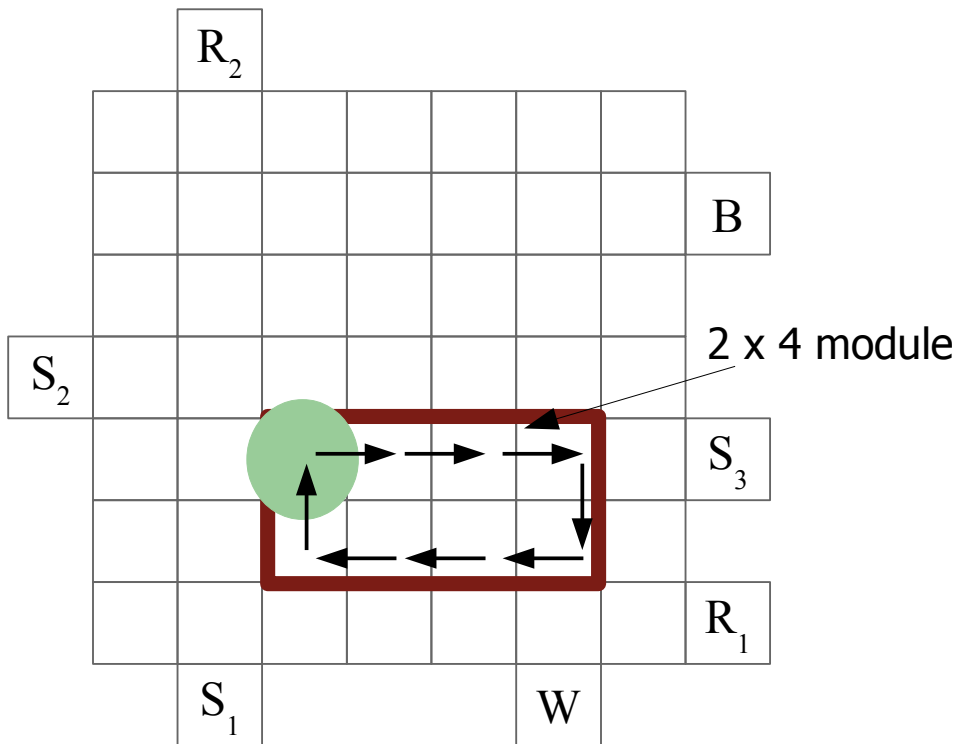
## Reconfigurable

- Splitting/Merging
- Storage
- Mixing/Dilution

# Module-Based Operation Execution



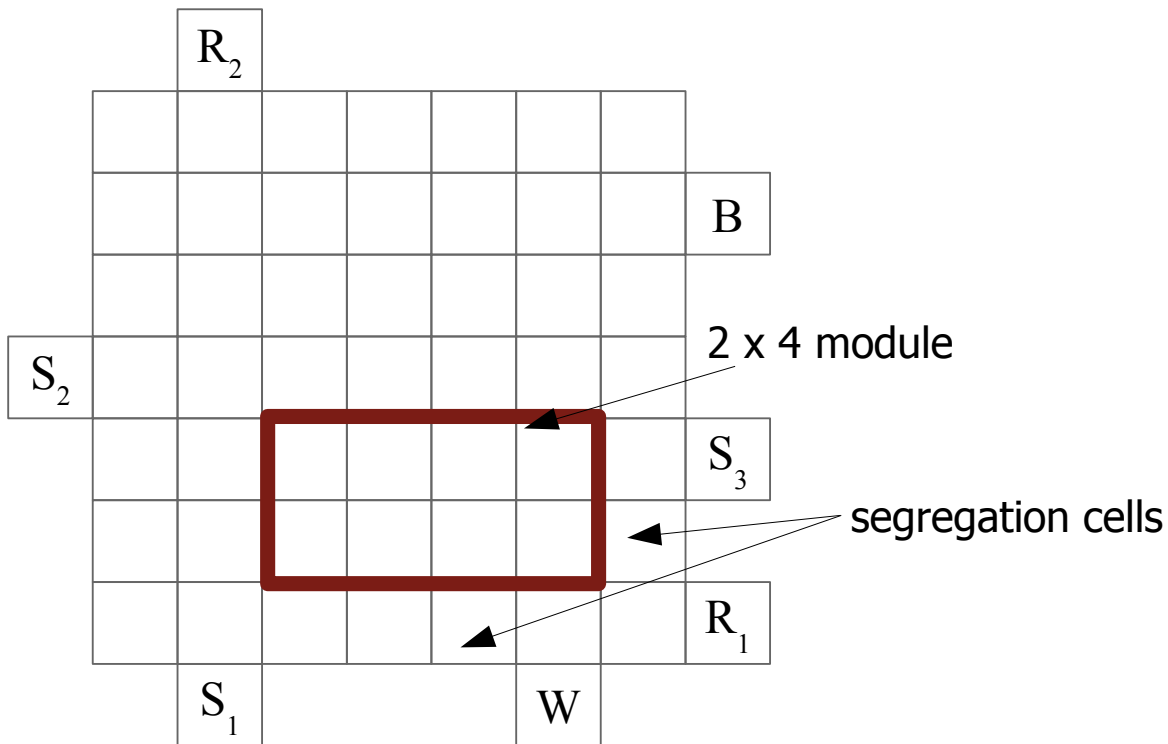
# Module-Based Operation Execution



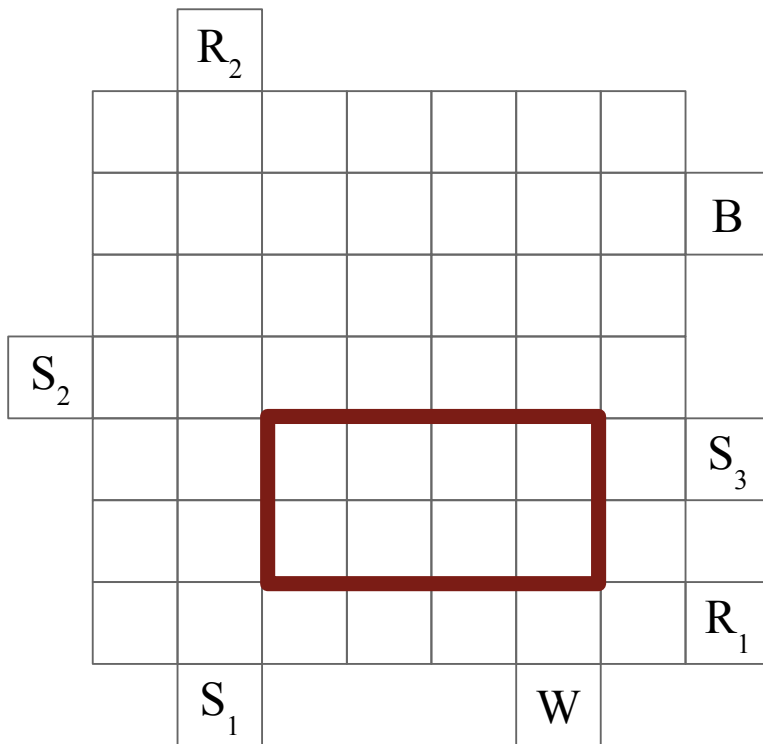
Operation	Area (cells)	Time (s)
Mix	2 x 4	3
Mix	2 x 2	4
Dilution	2 x 4	4
Dilution	2 x 2	5

Module library

# Module-Based Operation Execution



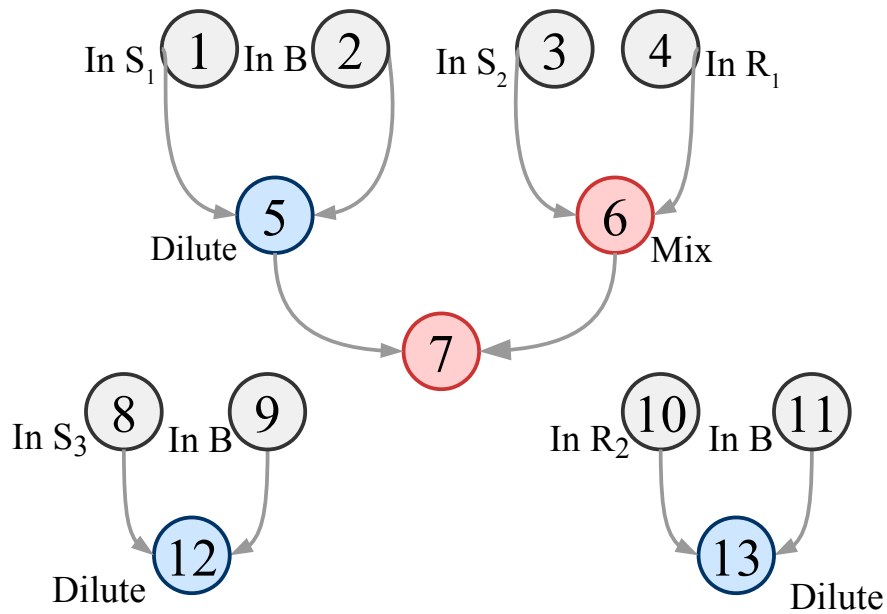
# Module-Based Operation Execution



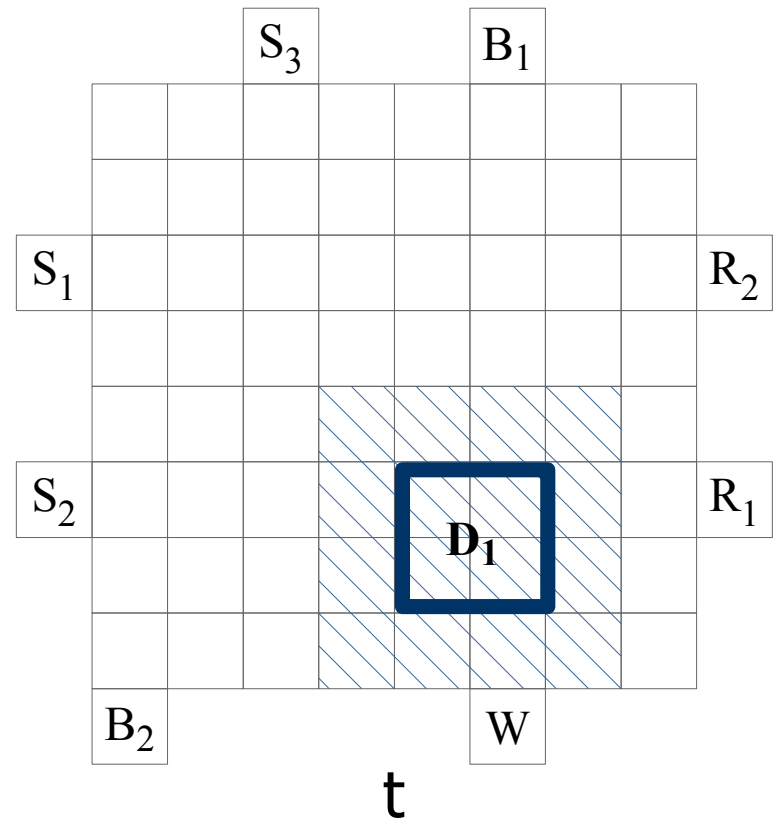
- Operations confined to rectangular, fixed modules
- Positions of droplets inside modules ignored
- Segregation cells

# Module-Based Synthesis with Dynamic Virtual Modules

# Example

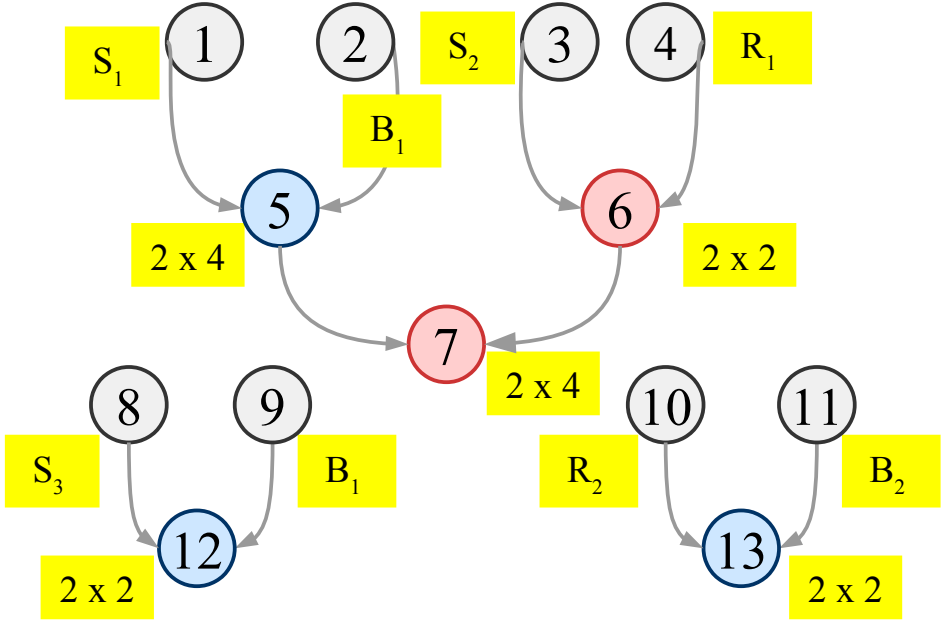


Application graph

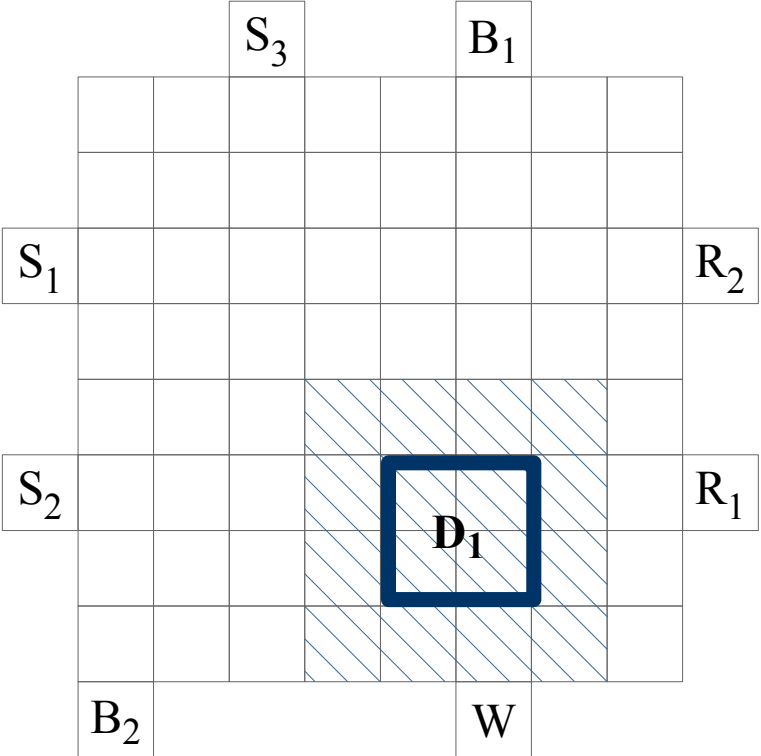




# Example

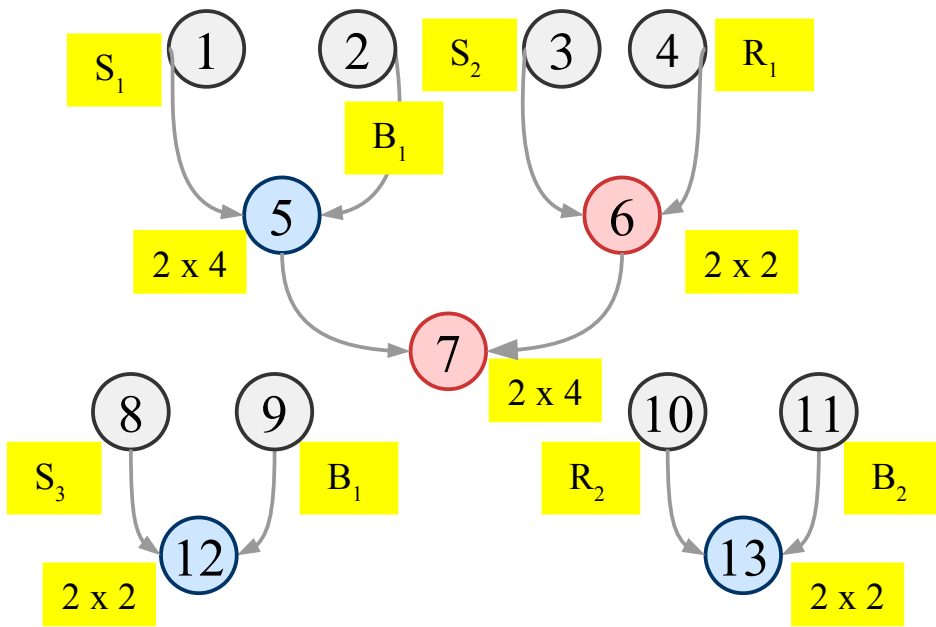


Application graph

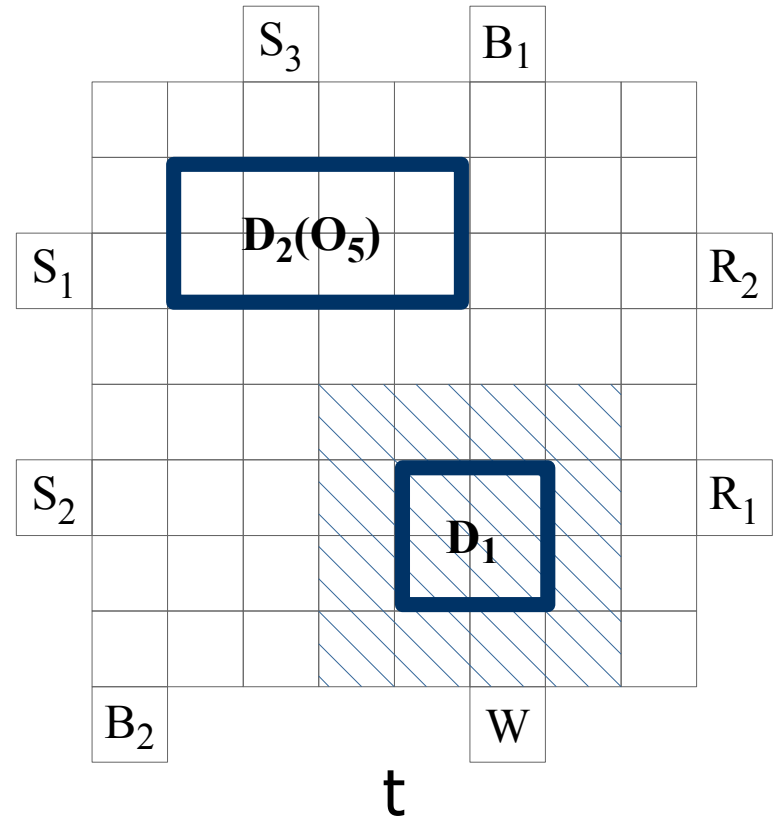


Biochip

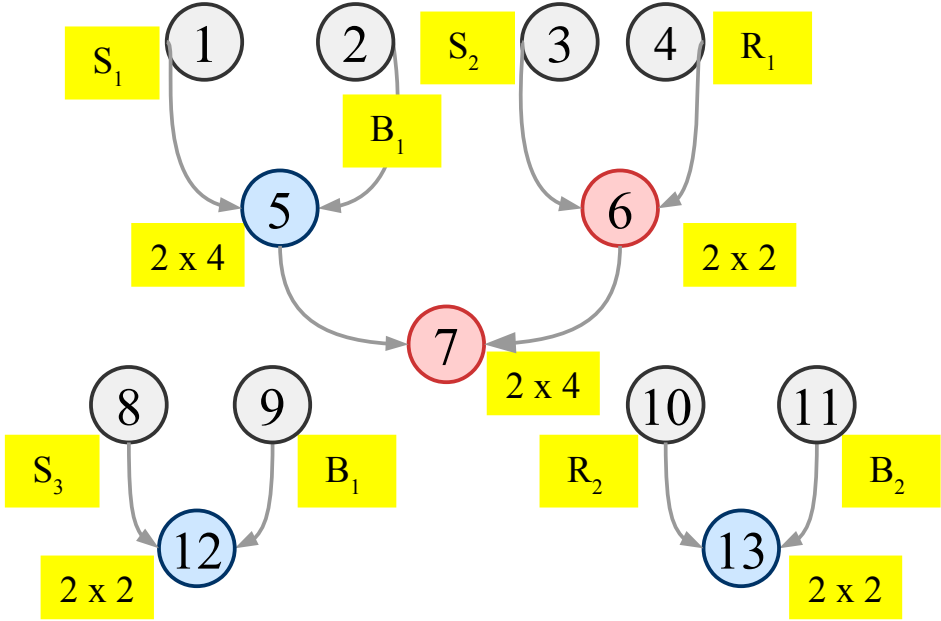
# Example



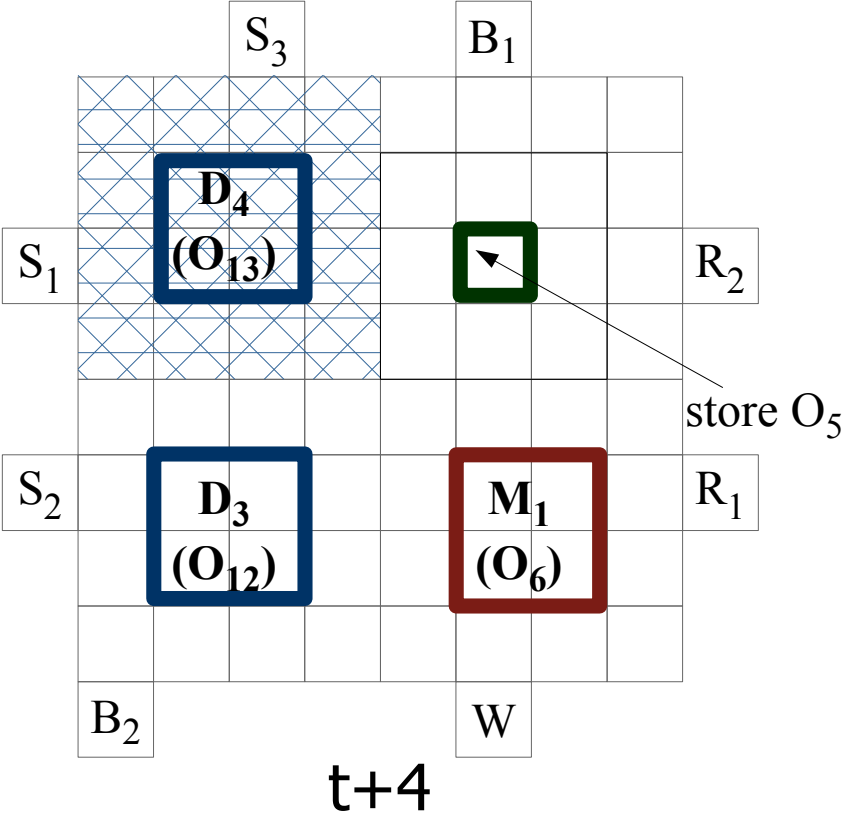
Application graph



# Example

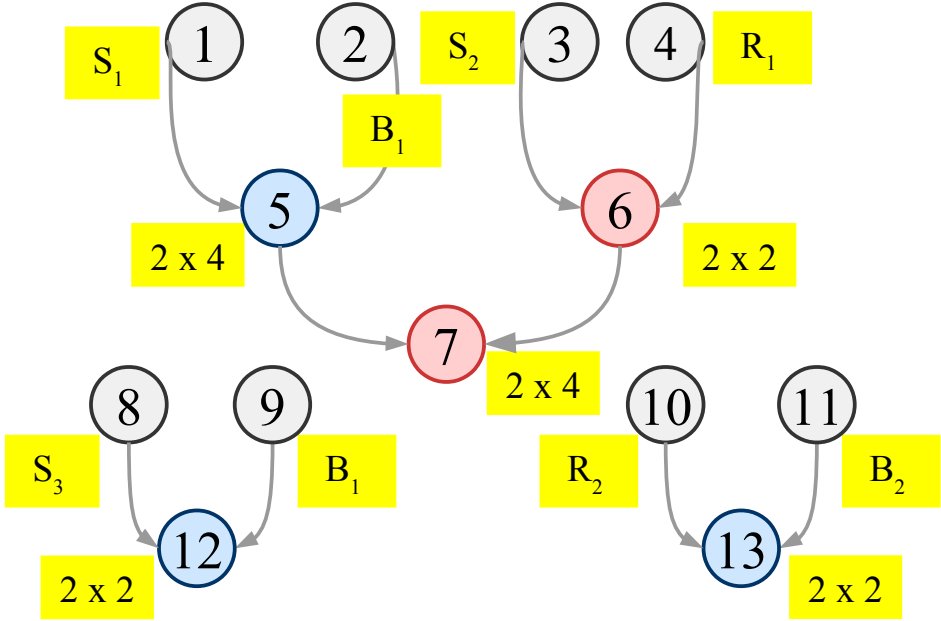


Application graph

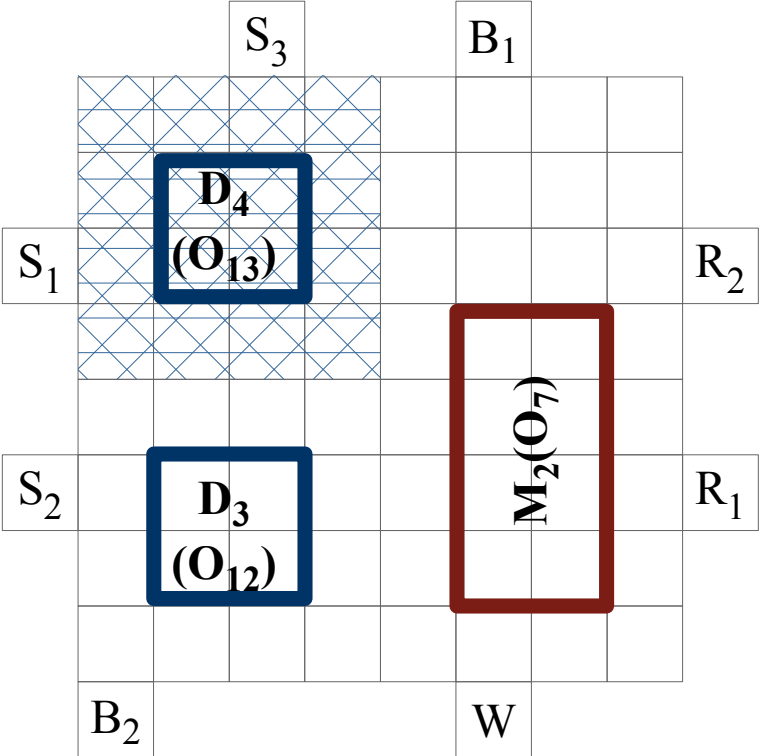


$t+4$

# Example

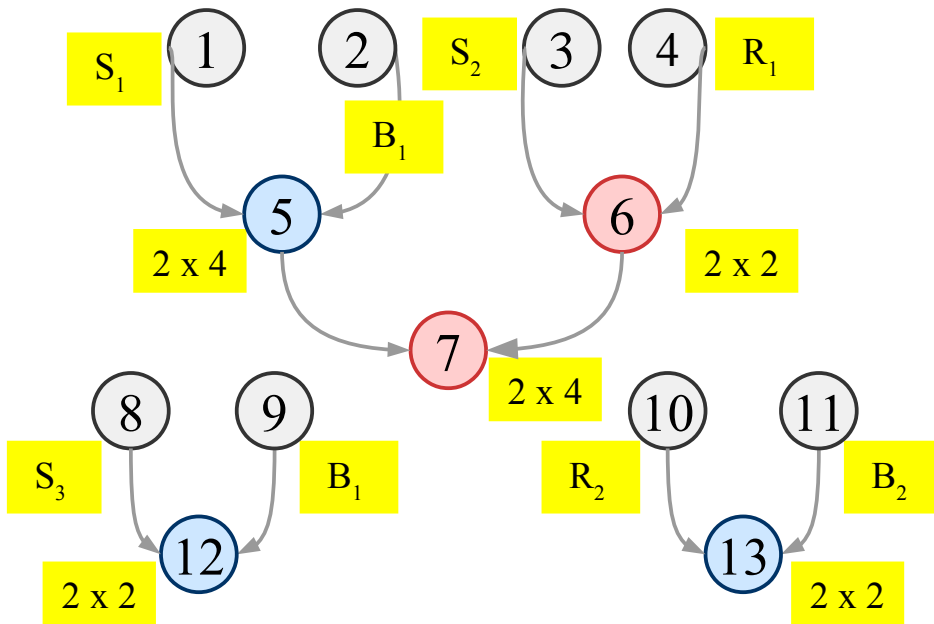


Application graph

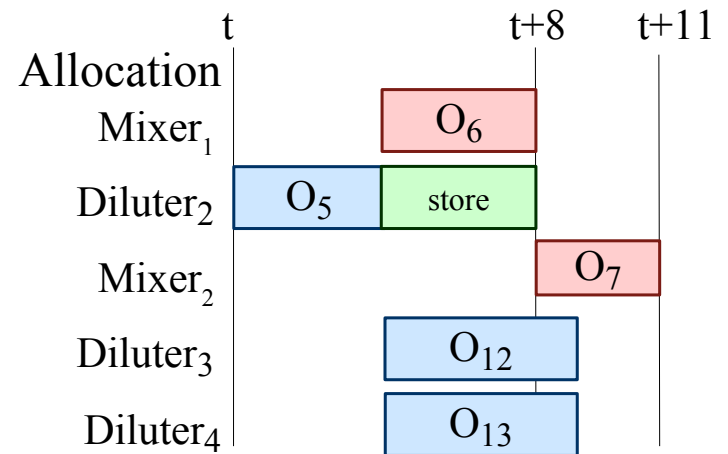


$t+8$

# Example

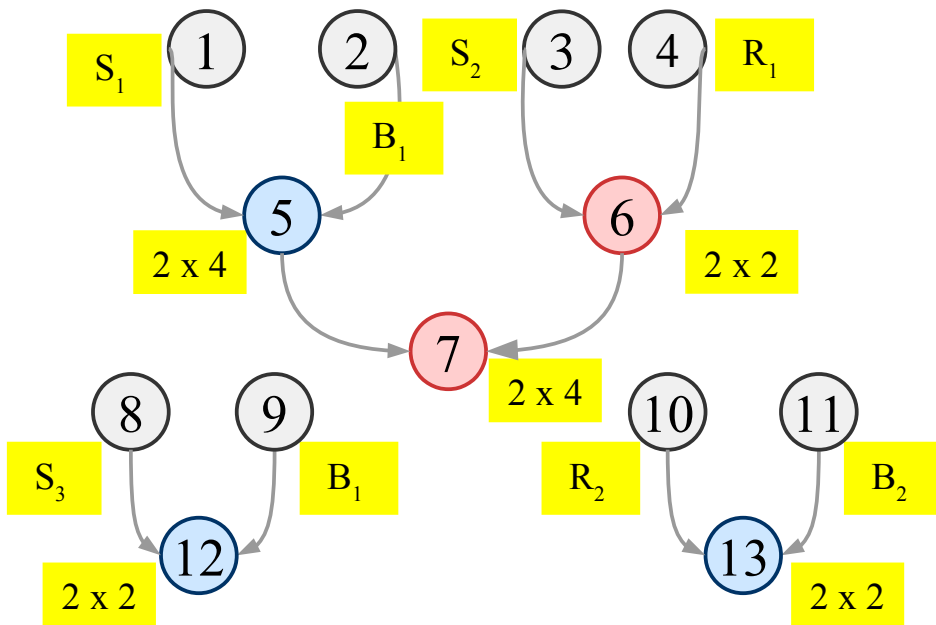


Application graph

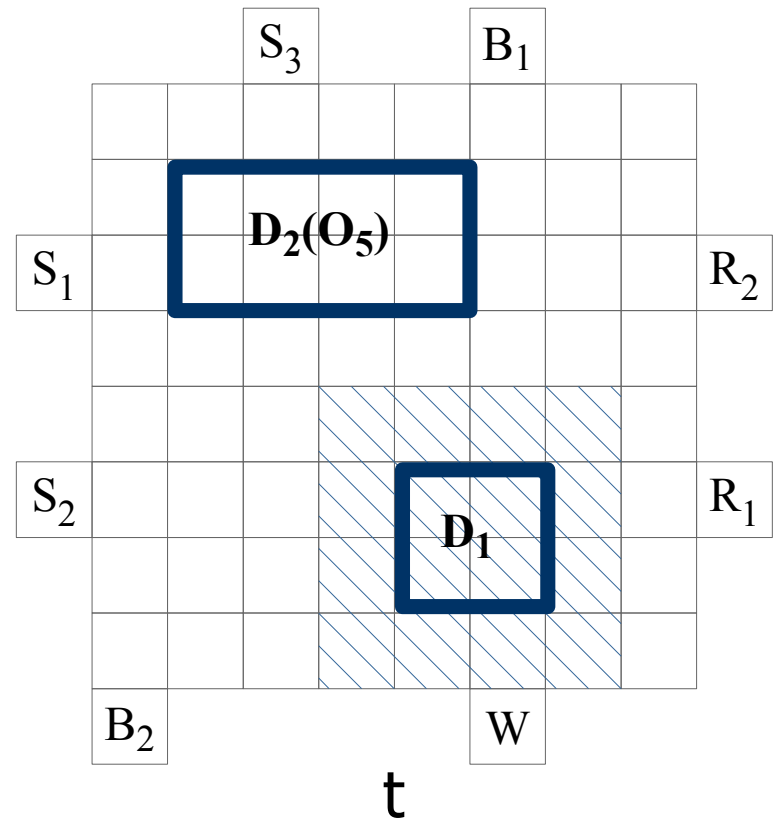


Schedule

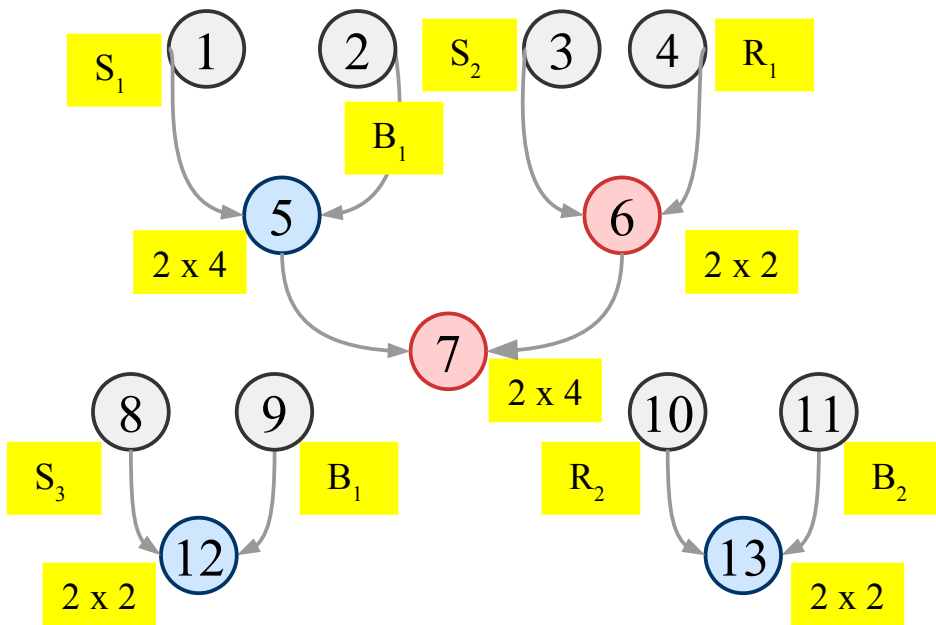
# Example



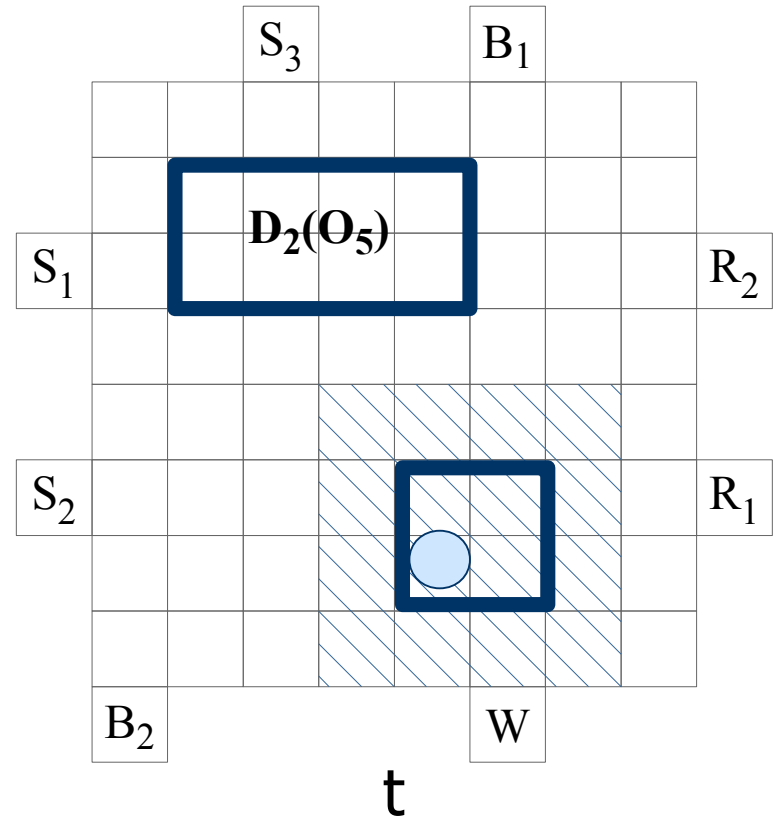
Application graph



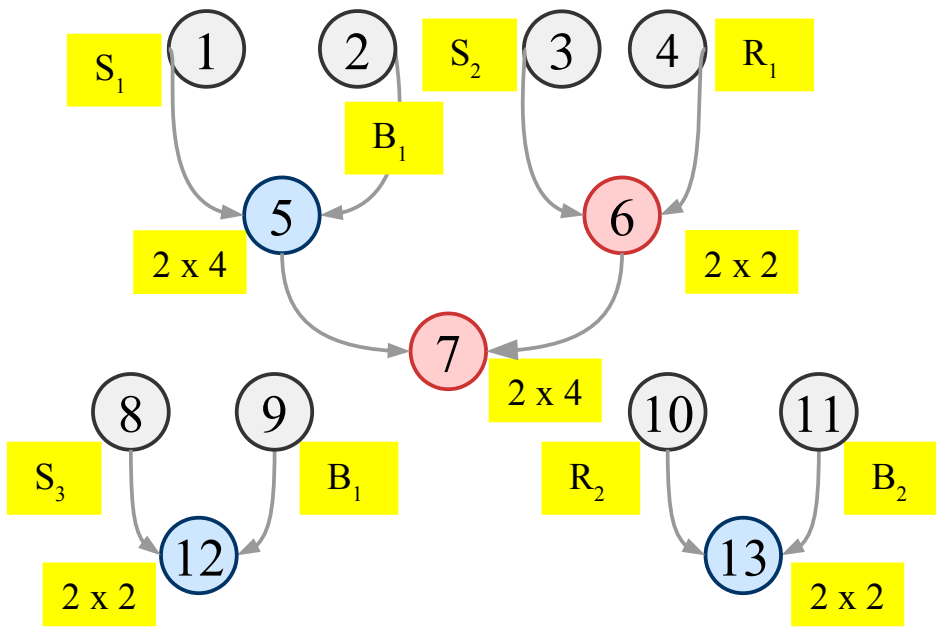
# Example



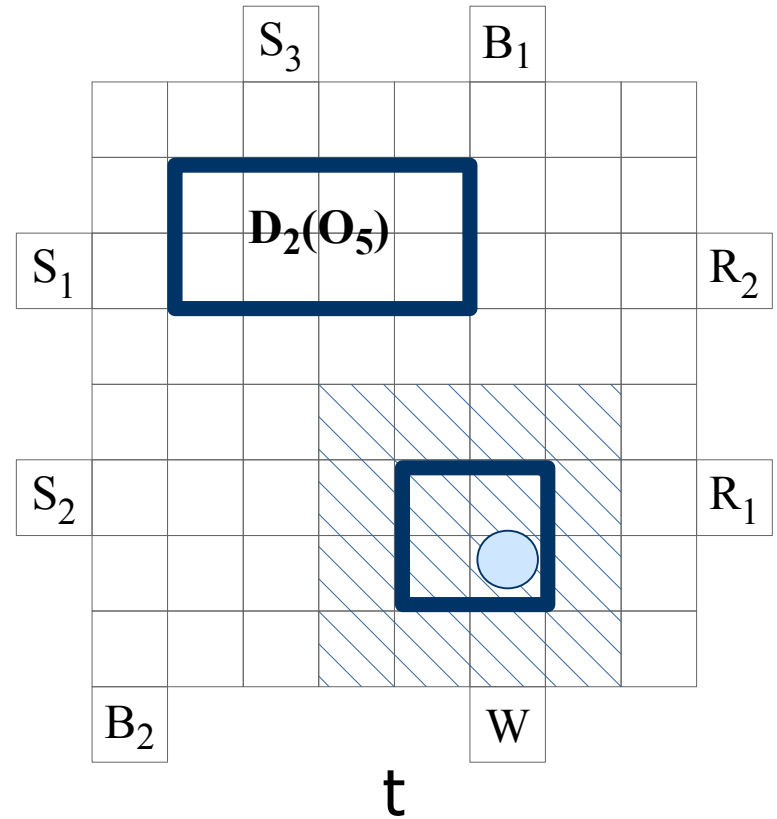
Application graph



# Example

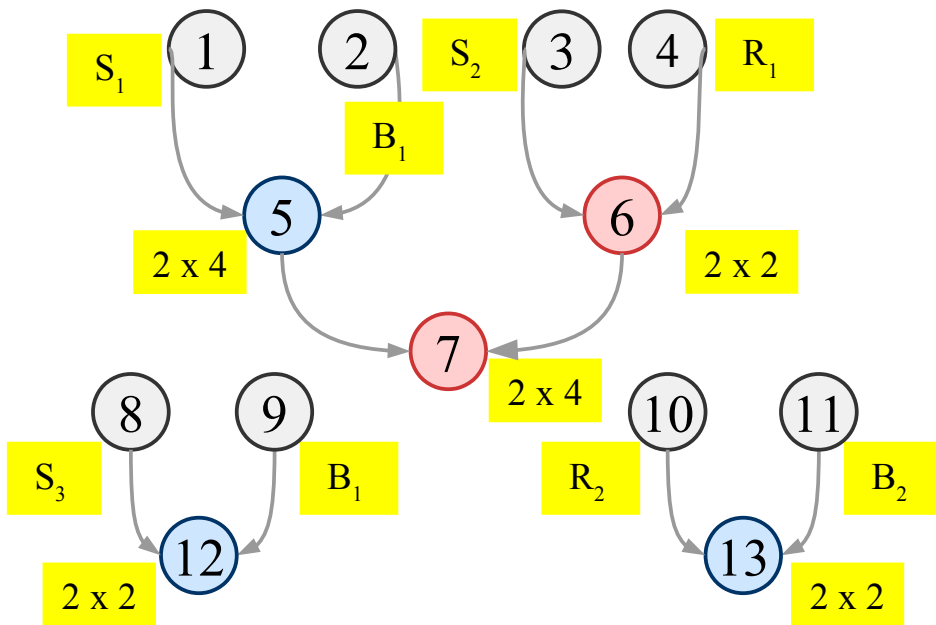


Application graph

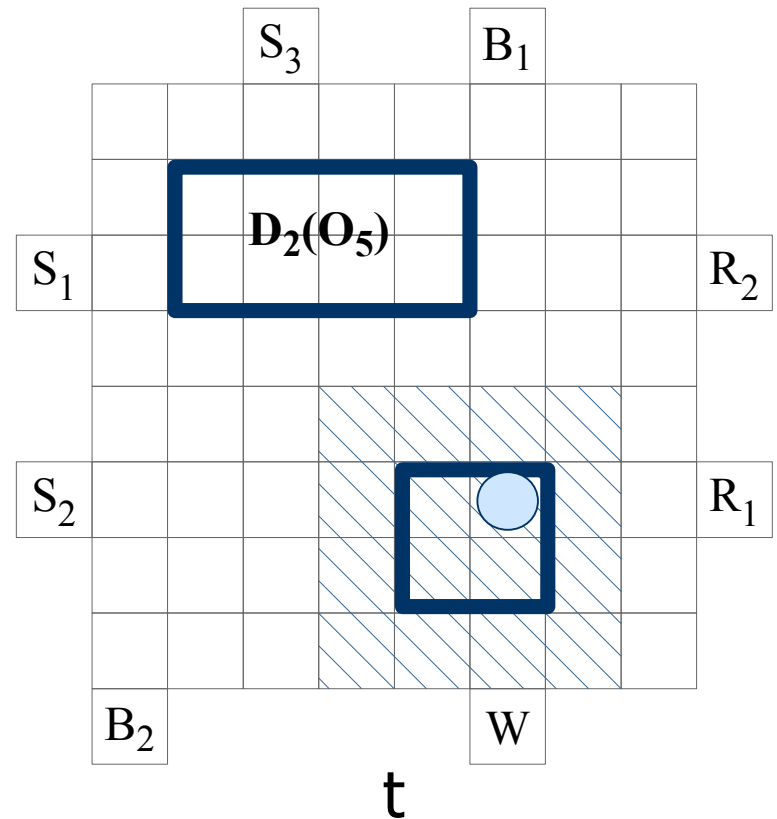




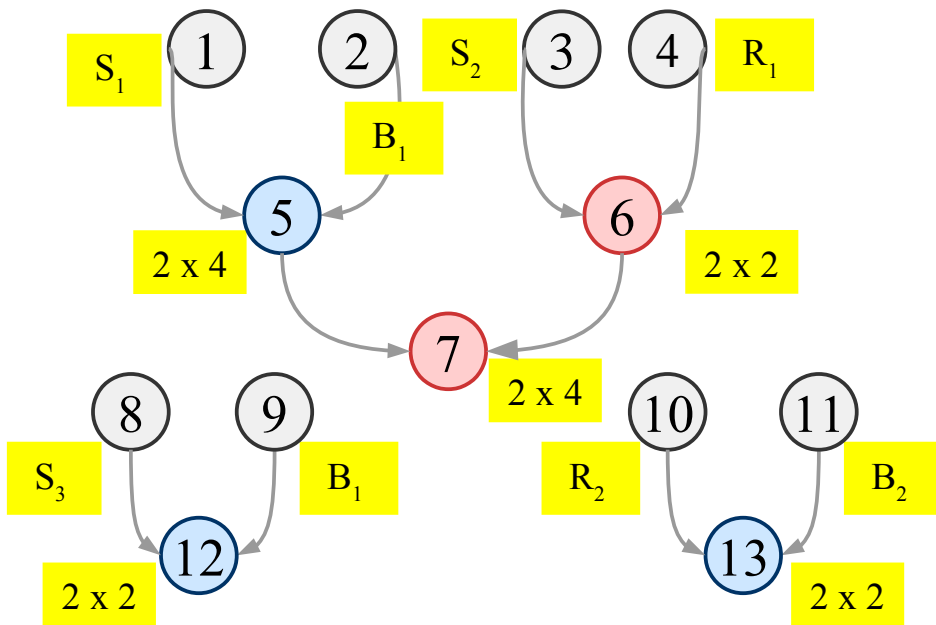
# Example



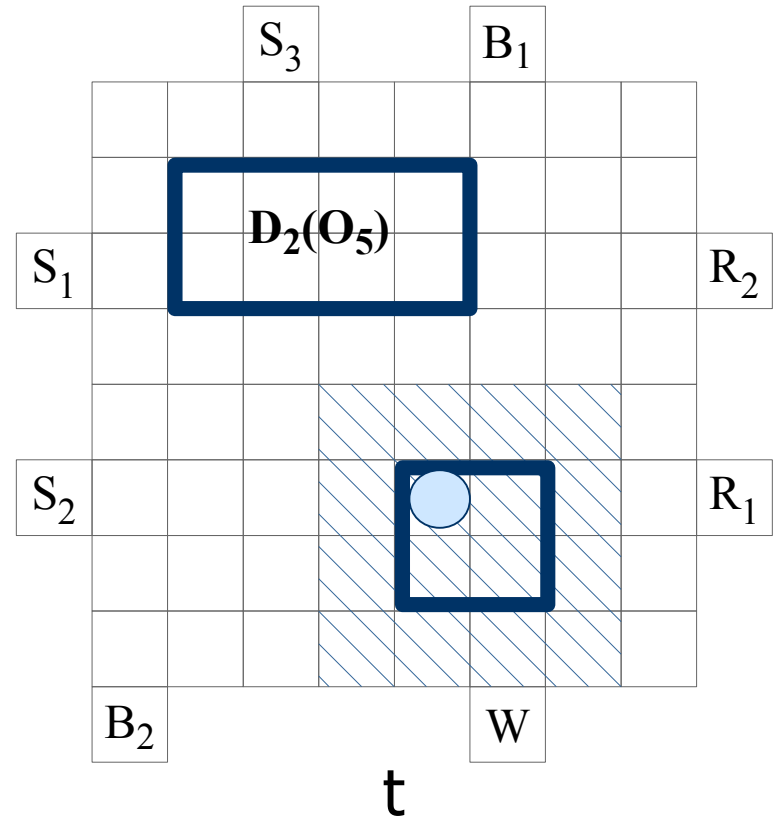
Application graph



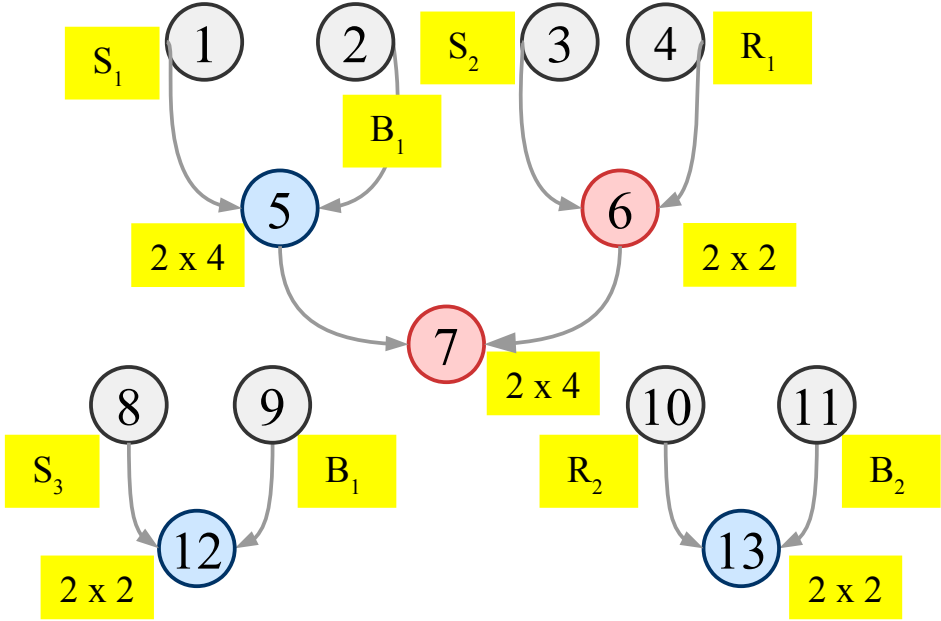
# Example



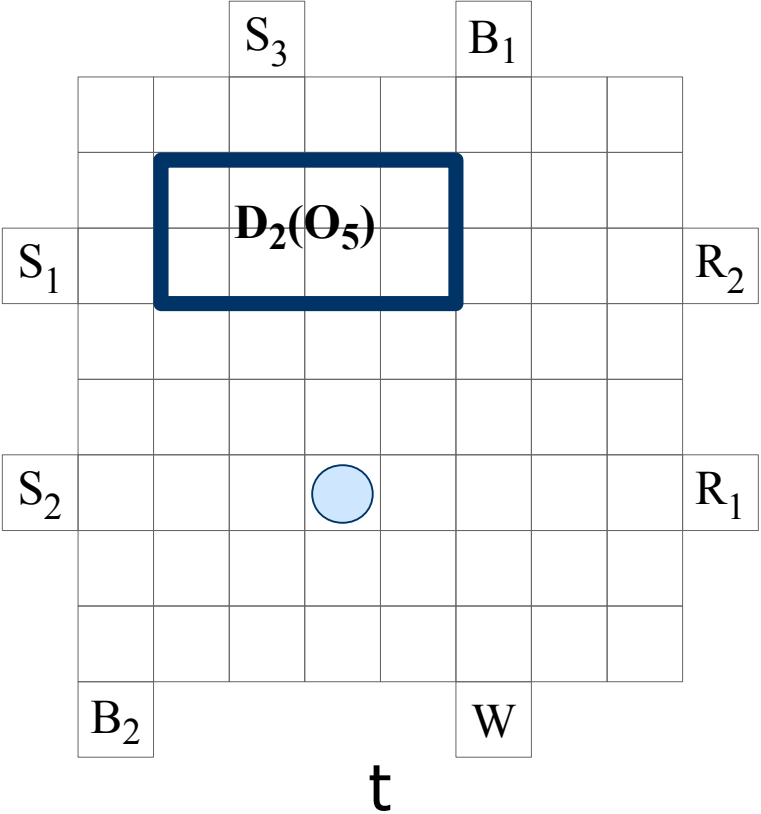
Application graph



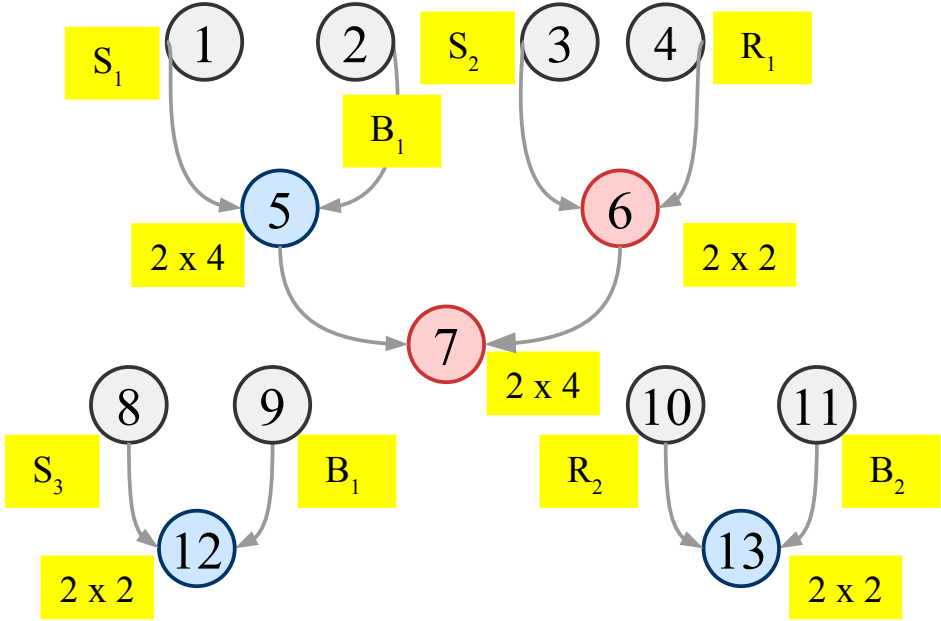
# Example



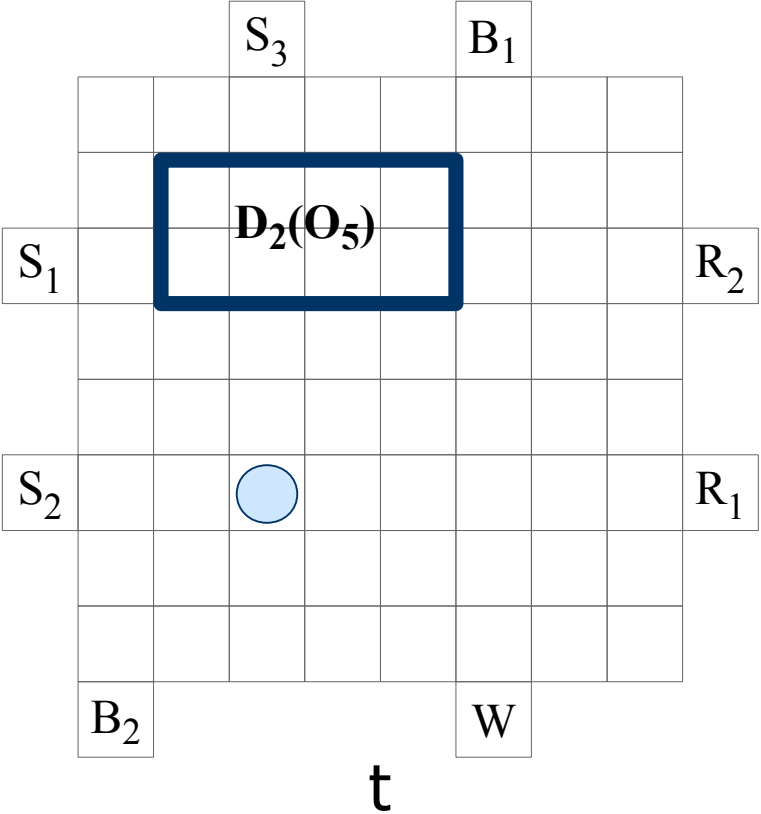
Application graph



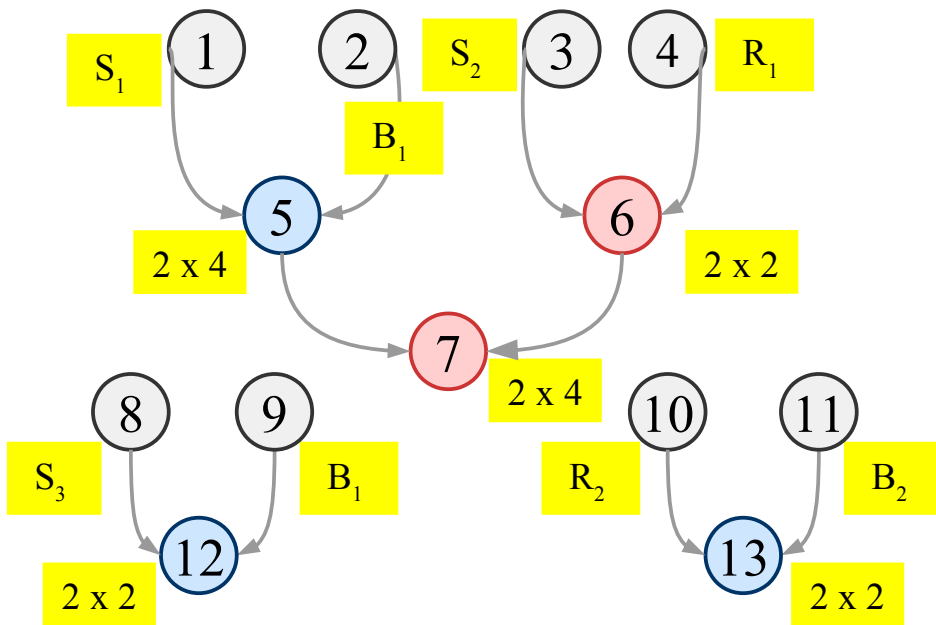
# Example



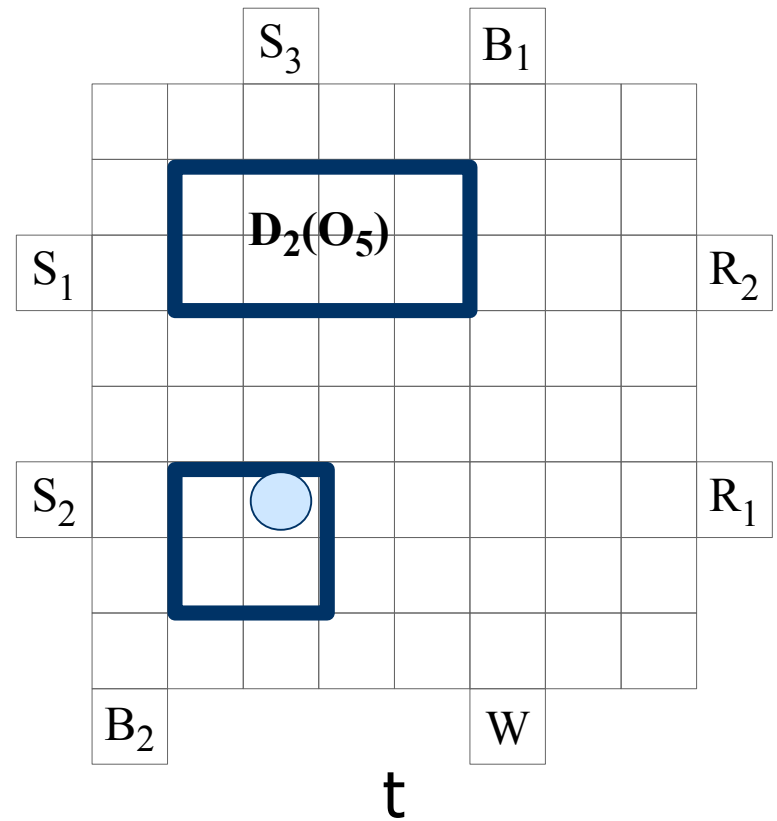
Application graph



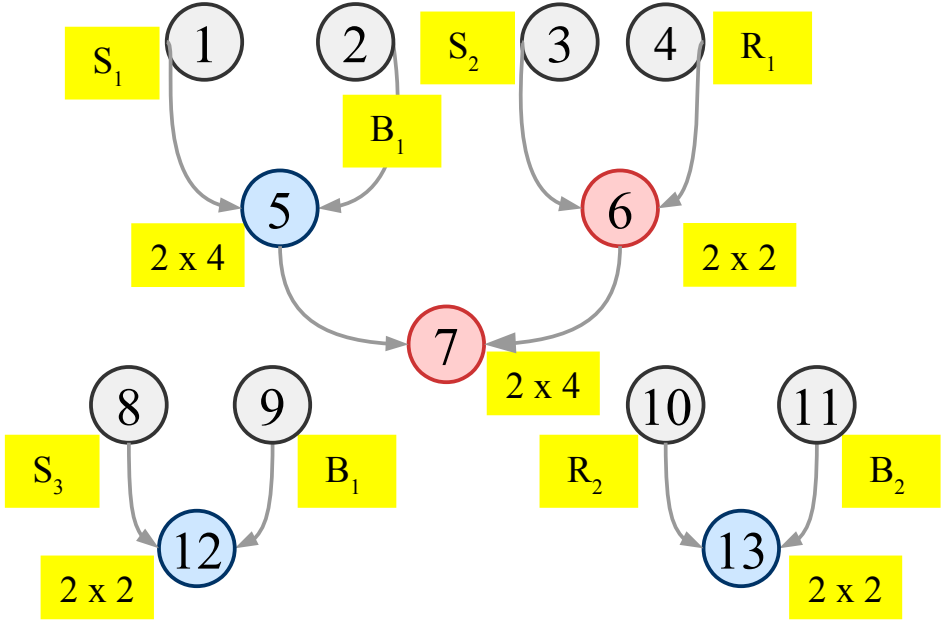
# Example



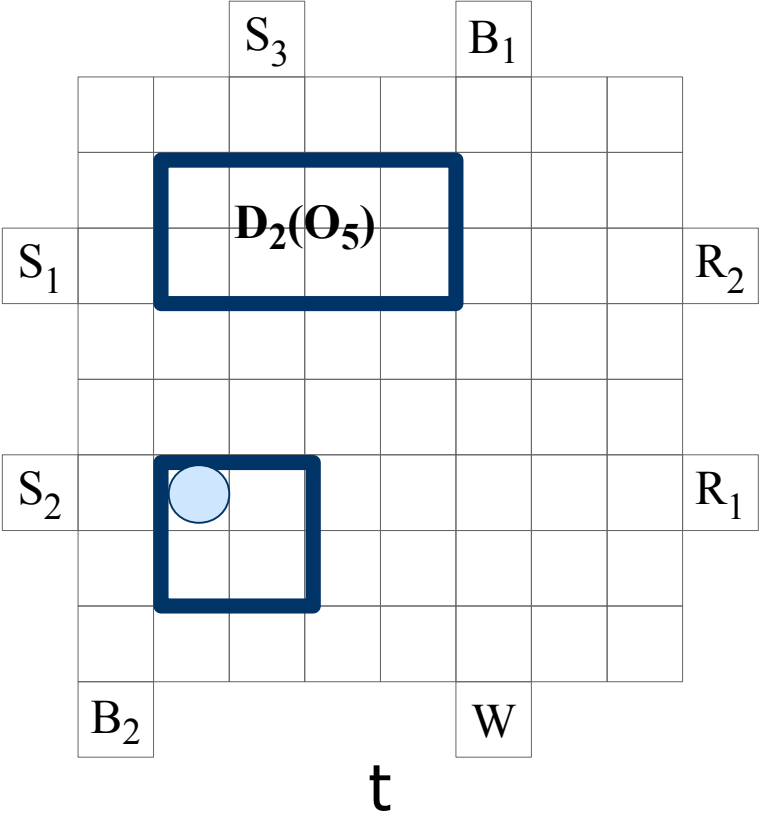
Application graph



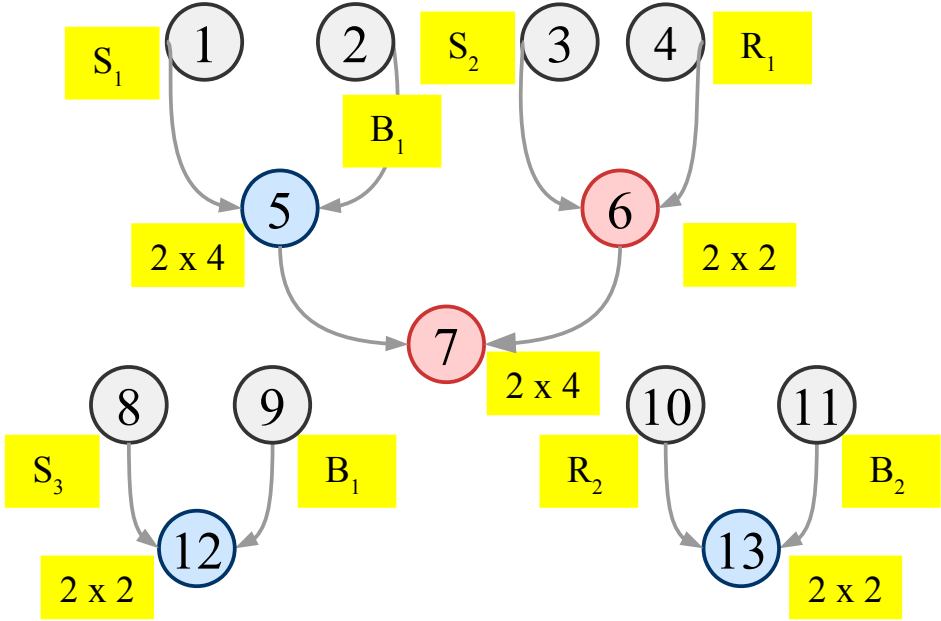
# Example



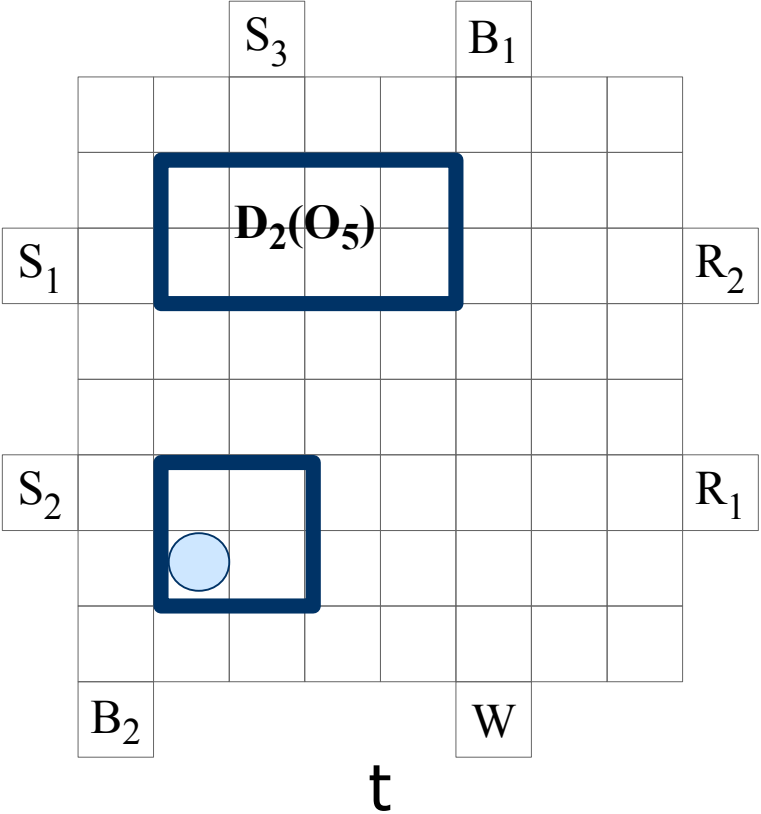
Application graph



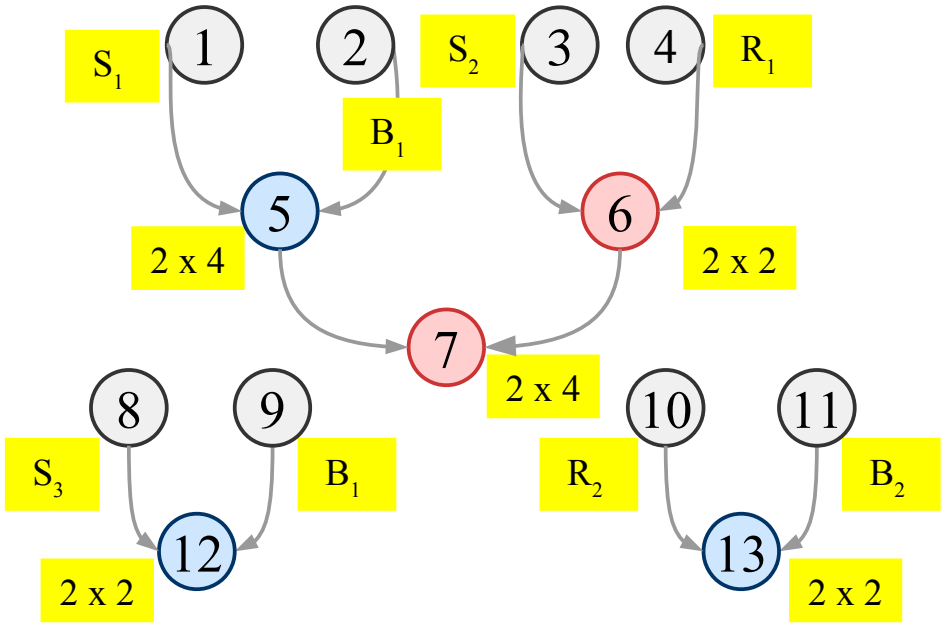
# Example



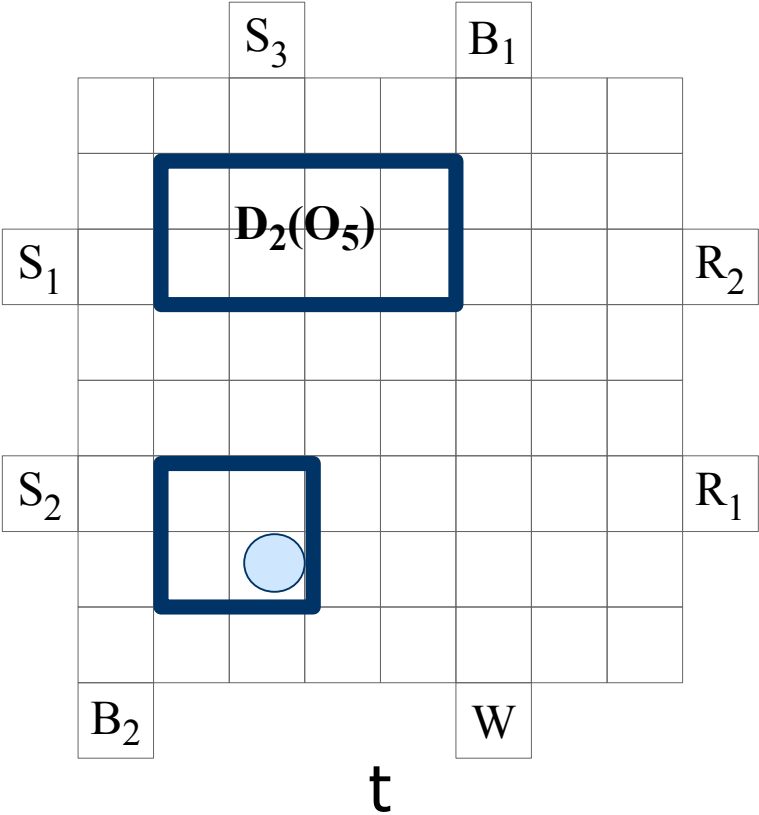
Application graph



# Example

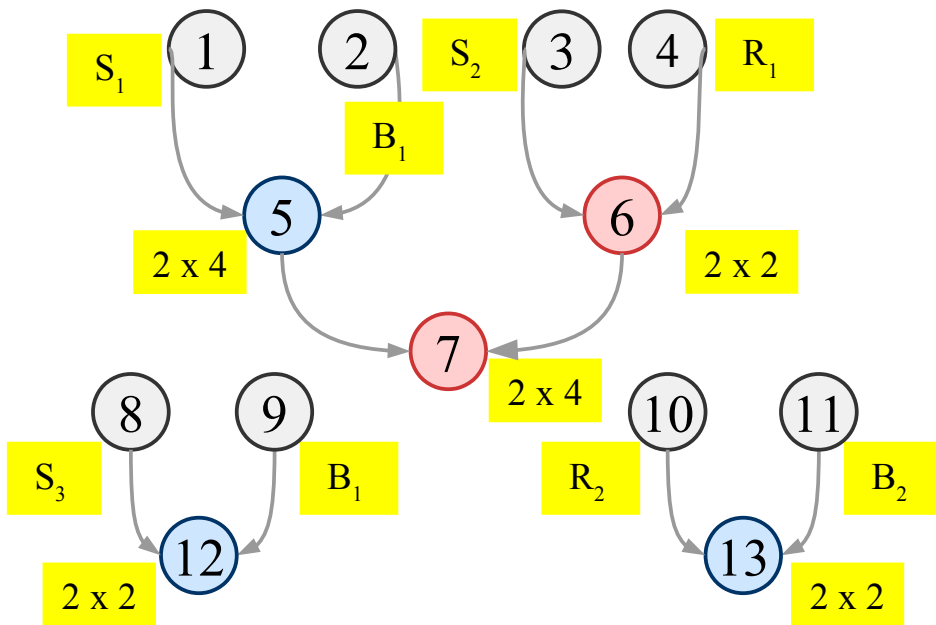


Application graph

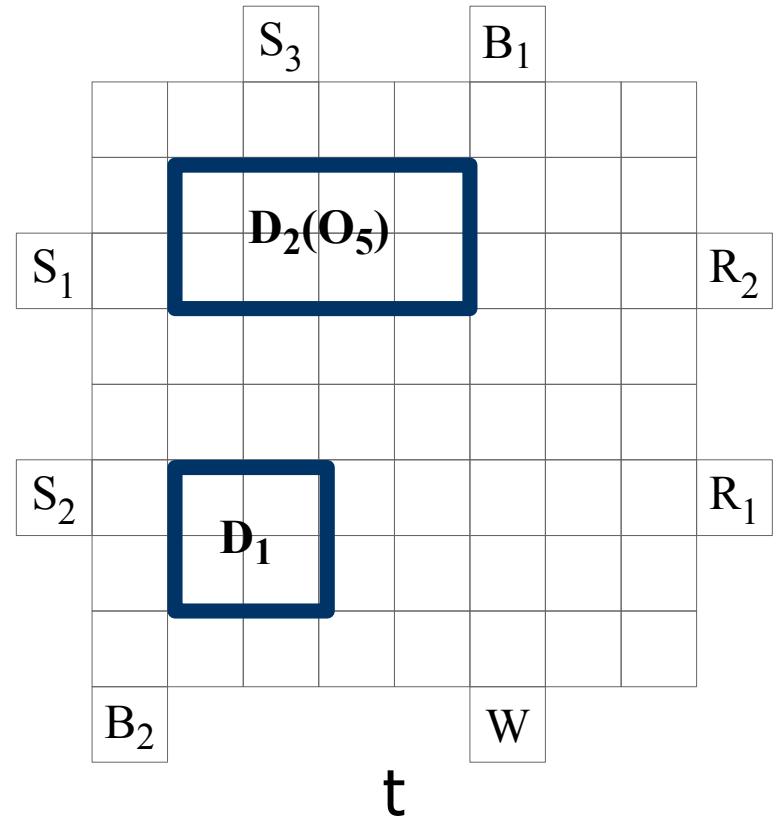




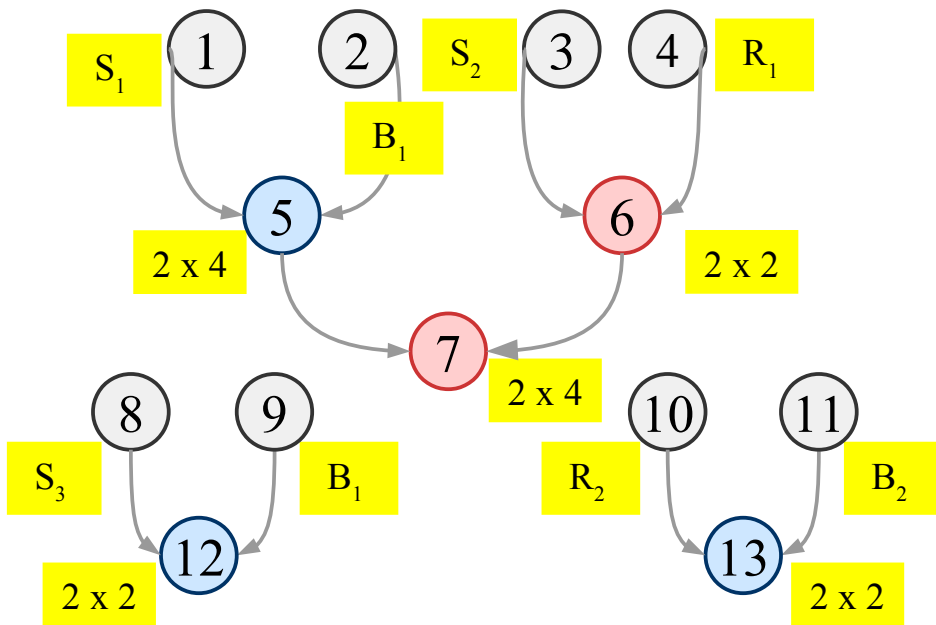
# Example



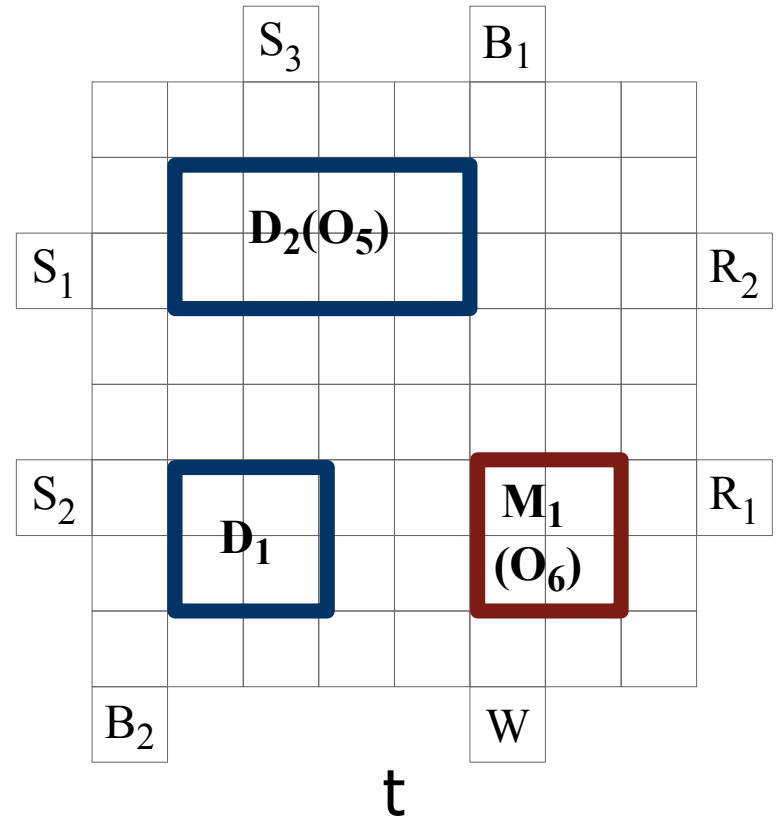
Application graph



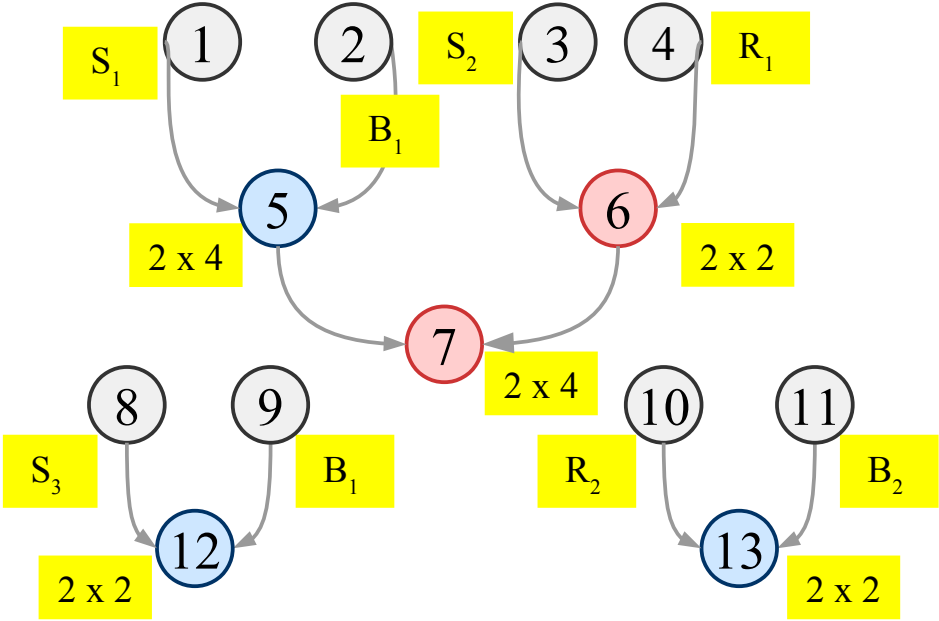
# Example



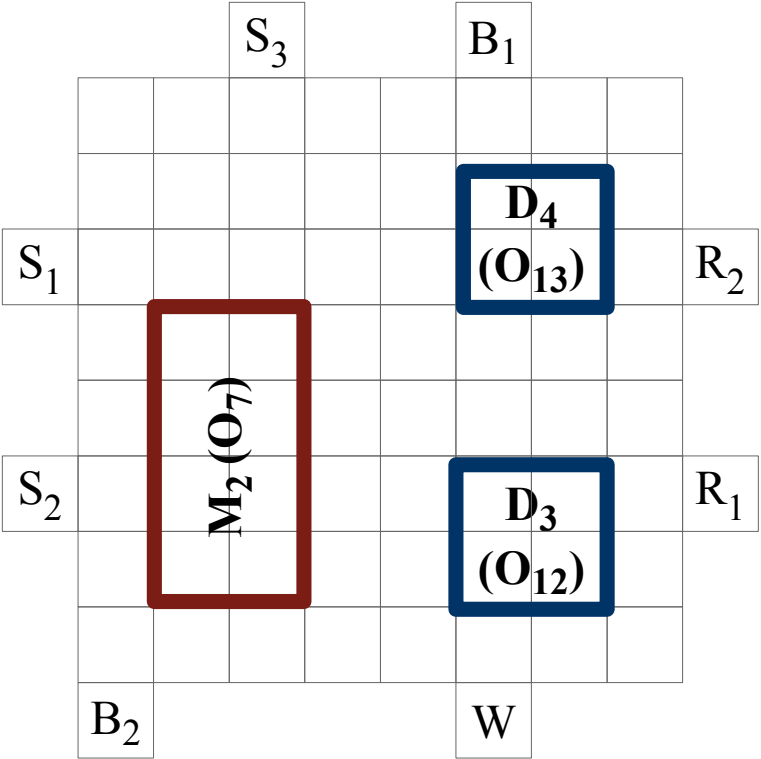
Application graph



# Example

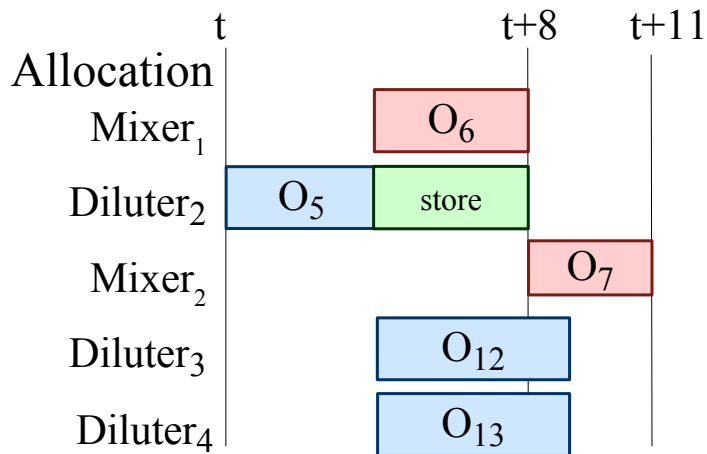


Application graph

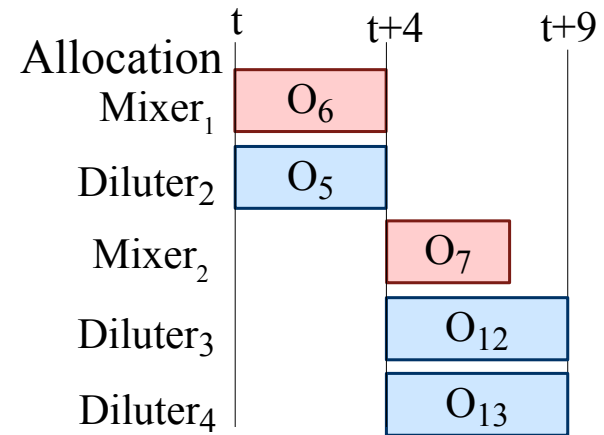


$t+4$

# Example



Schedule – operation execution  
with fixed virtual modules



Schedule – operation execution  
with dynamic virtual modules

# Solution

## Tabu Search

- Binding of modules to operations

## List Scheduling

- Schedule of the operations

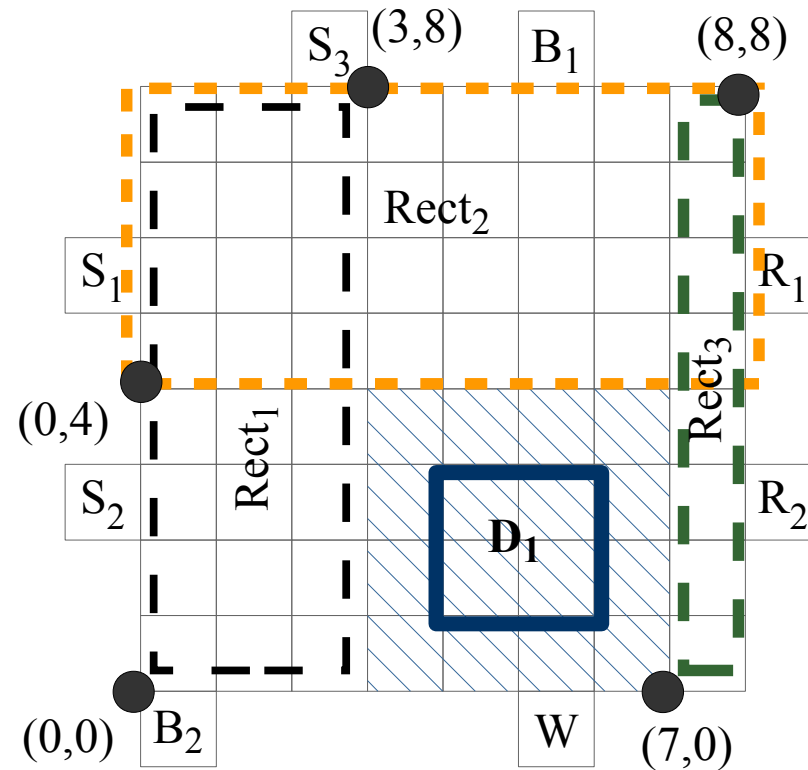
- Placement of modules performed inside scheduling

- Placement of the modules

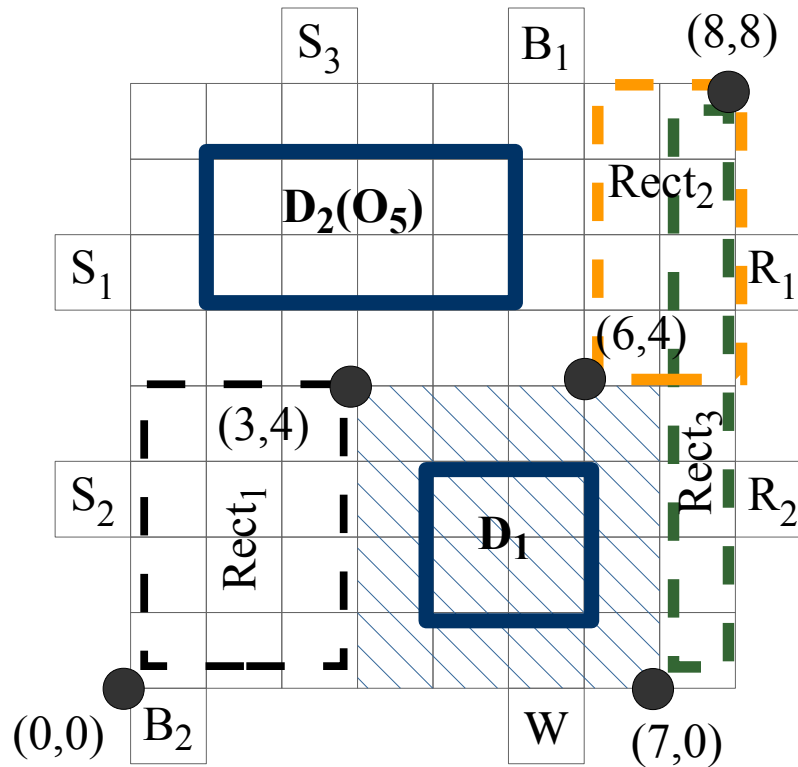
## Maximal Empty Rectangles

- Free space manager based on [Bazargan et al. 2000] that divides free space on the chip into overlapping rectangles

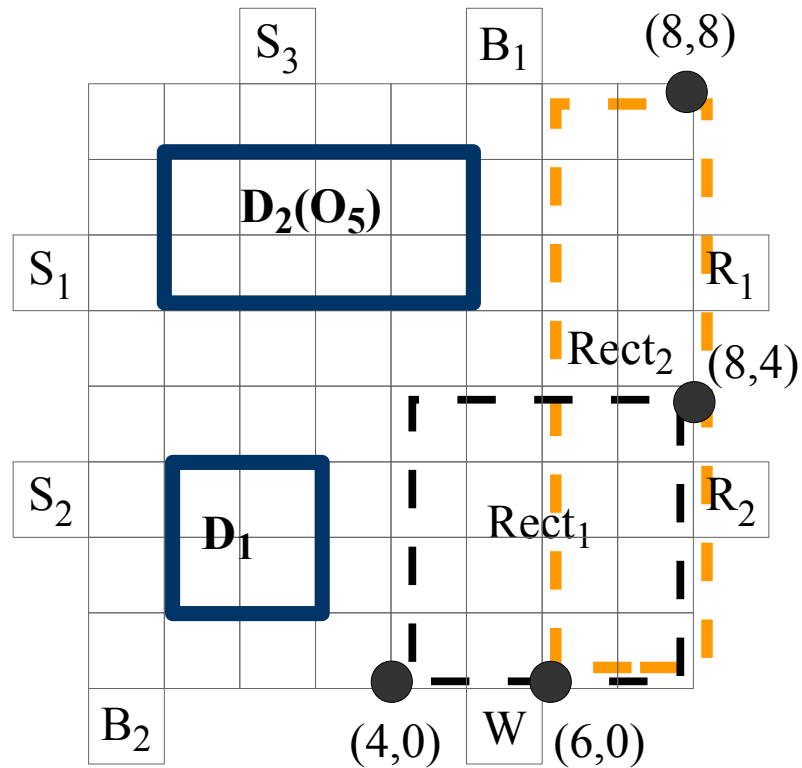
# Dynamic Placement Algorithm



# Dynamic Placement Algorithm



# Dynamic Placement Algorithm





# Experimental Evaluation

- Tabu Search-based algorithm implemented in Java
- Benchmarks
  - Real-life applications
    - Colorimetric protein assay
    - In-vitro diagnosis
    - Polymerase chain reaction – mixing stage
  - Synthetic benchmarks
    - 10 TGFF-generated benchmarks with 10 to 100 operations
- Comparison between:
  - Module-based synthesis with fixed modules (MBS)
  - T-Tree [Yuh et al. 2007]
  - Module-based synthesis with dynamic modules (DMBS)

# Experimental Evaluation

**Best-, average schedule length and standard deviation out of 50 runs for MBS**

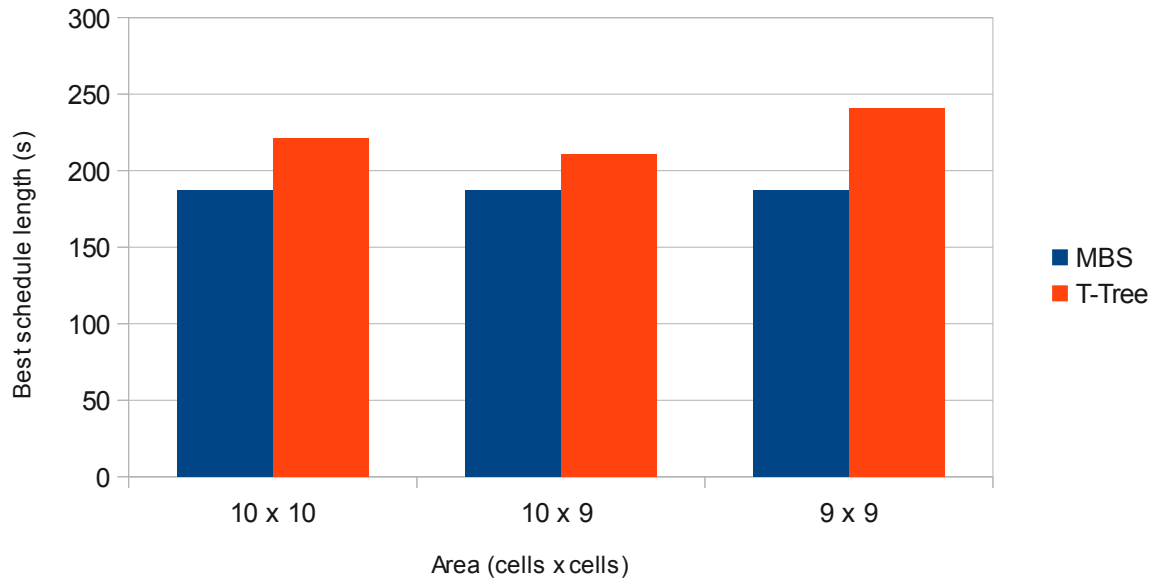
Colorimetric protein assay

Area	Time limit (min)	Best (s)	Average (s)	Standard dev. (%)
13 x 13	60	182	189.99	2.90
	10	182	192.00	3.64
	1	191	199.20	4.70
12 x 12	60	182	190.86	3.20
	10	185	197.73	6.50
	1	193	212.62	10.97
11 x 12	60	184	192.50	3.78
	10	194	211.72	14.37
	1	226	252.19	15.76

# Experimental Evaluation

Best schedule length out of 50 runs for **MBS** vs. **T-Tree**

Colorimetric protein assay

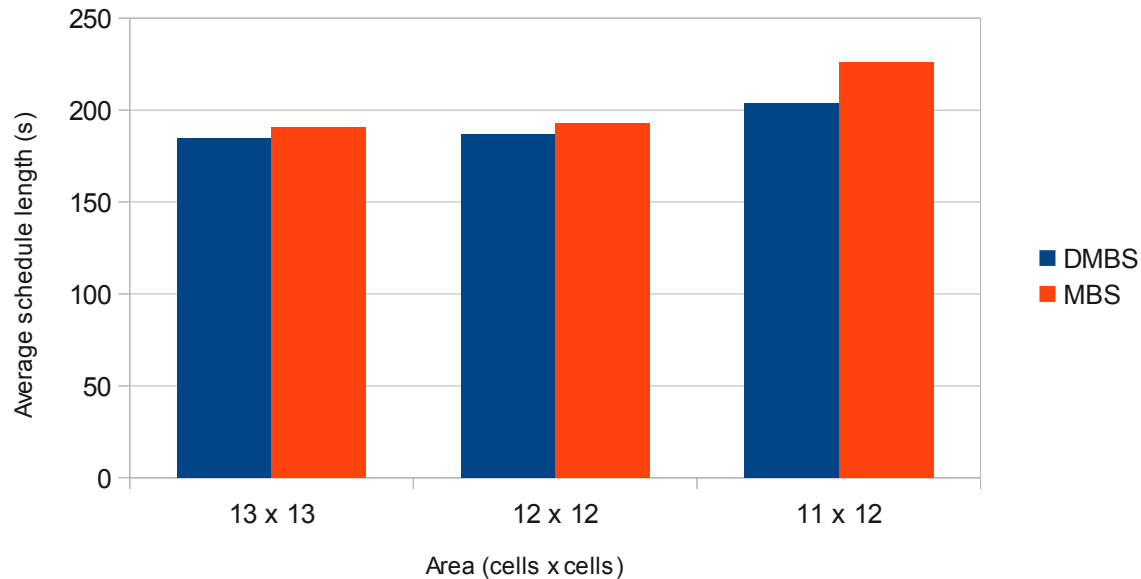


22.91 % improvement for 9 x 9

# Experimental Evaluation

Average schedule length out of 50 runs for **DMBS** vs. **MBS**

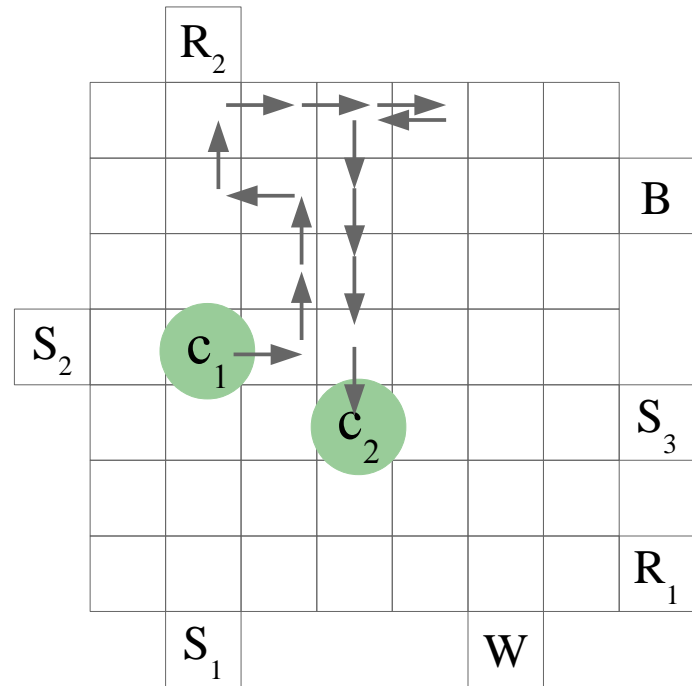
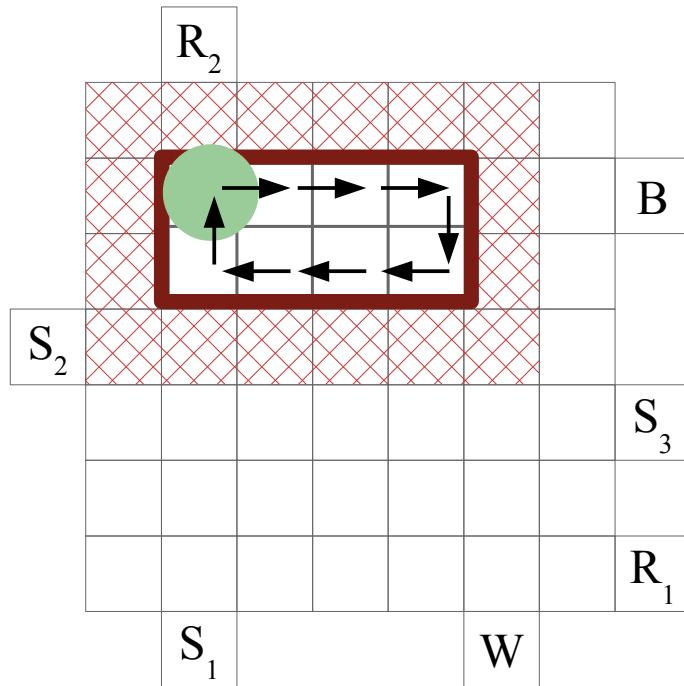
Colorimetric protein assay



7.68 % improvement for 11 x 12

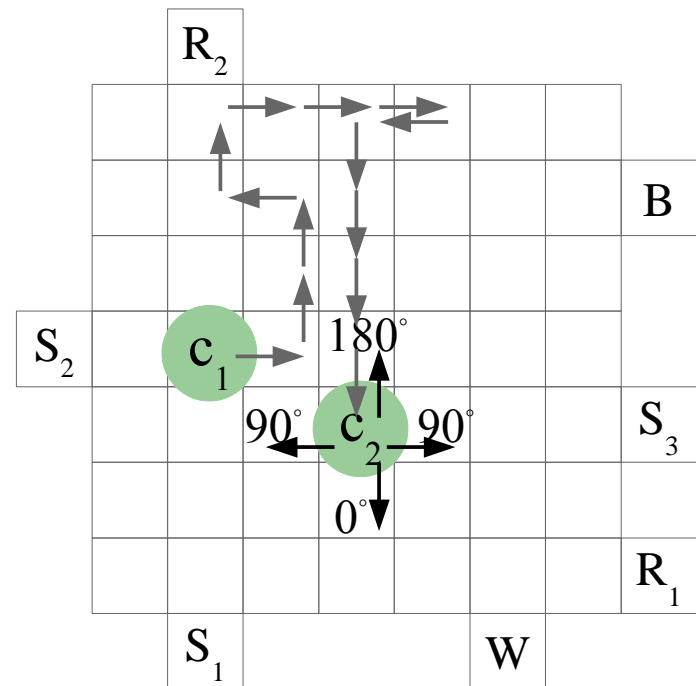
# Routing-Based Operation Execution

# Module-Based vs. Routing-Based Operation Execution



# Operation Execution Characterization

**$p^{90}$ ,  $p^{180}$ ,  $p^0$ ?**



# Operation Execution Characterization



$p^{90}$ ,  $p^{180}$ ,  $p^0$



Type	Area (cells)	Time (s)
Mix/Dlt	2 x 4	2.9
Mix/Dlt	1 x 4	4.6
Mix/Dlt	2 x 3	6.1
Mix/Dlt	2 x 2	9.9
Input	-	2
Detect	1 x 1	30

Electrode pitch size = 1.5 mm, gap spacing = 0.3 mm, average velocity rate = 20 cm/s.



# Operation Execution Characterization

$$p^{90} = 0.1 \%$$

$$p^{180} = -0.5 \%$$

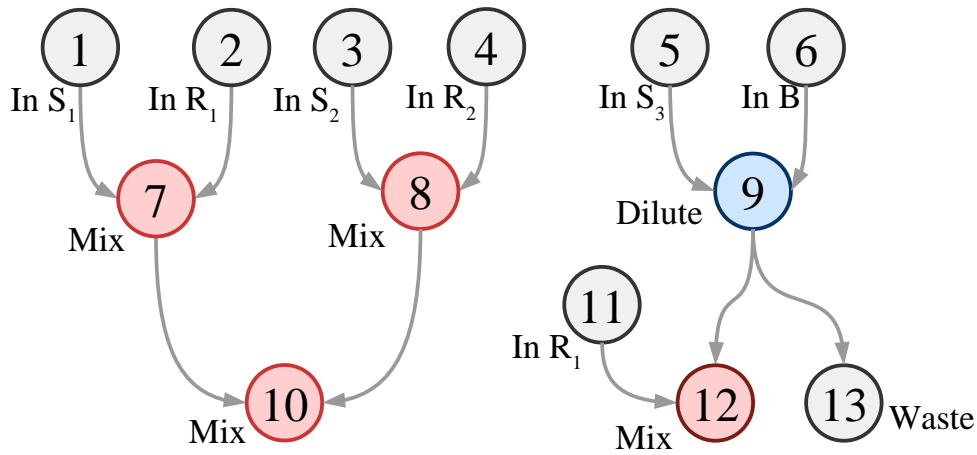
$$p_1^0 = 0.29 \%$$

$$p_2^0 = 0.58 \%$$

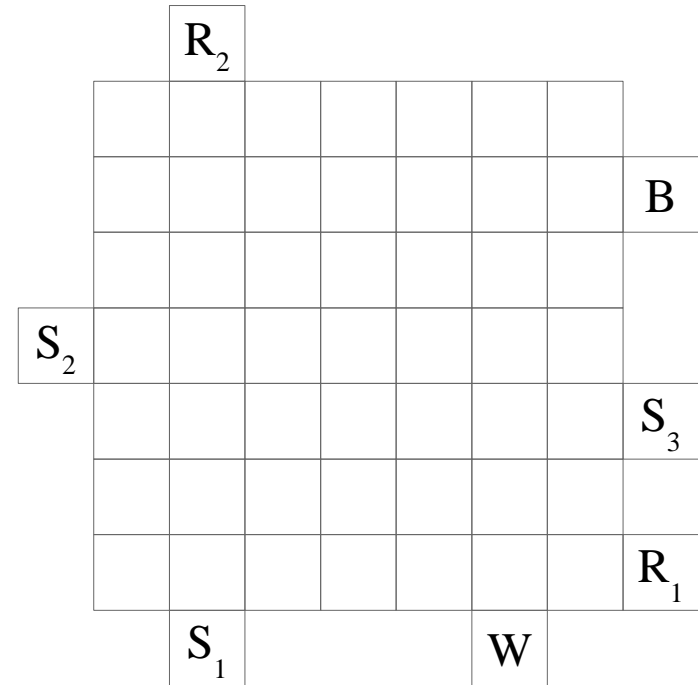
Type	Area (cells)	Time (s)
Mix/Dlt	2 x 4	2.9
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Input	-	2
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Electrode pitch size = 1.5 mm, gap spacing = 0.3 mm, average velocity rate = 20 cm/s.

# Example

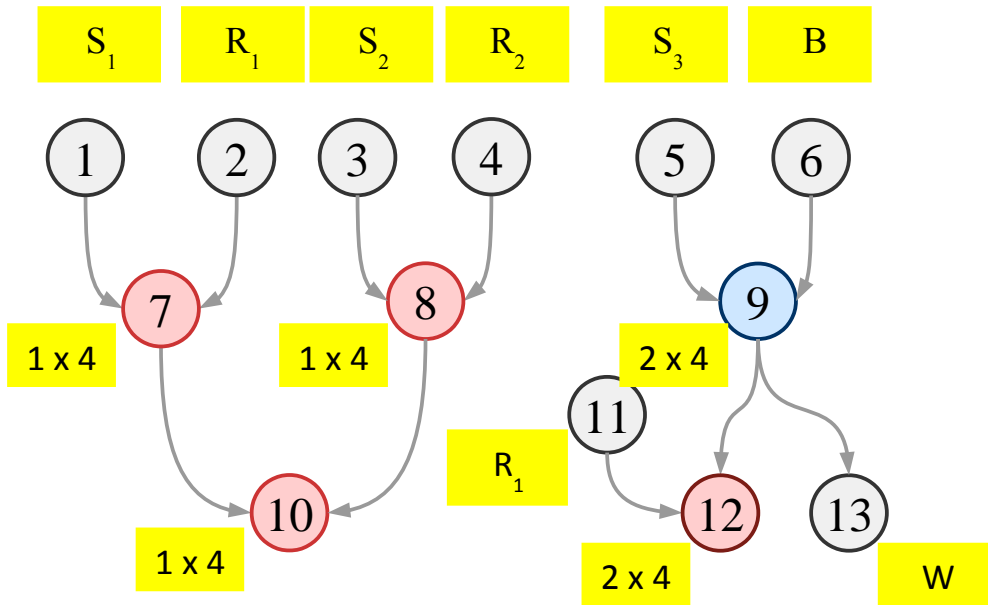


Application graph

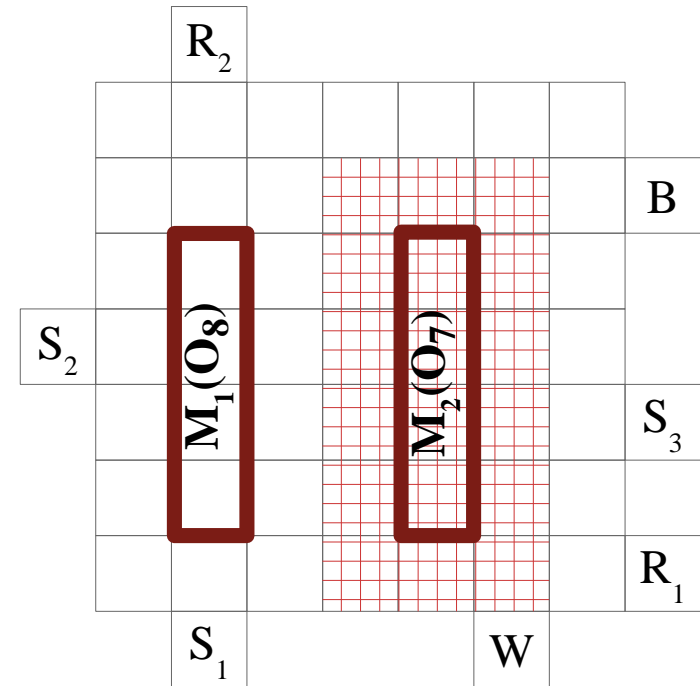


Biochip

# Example

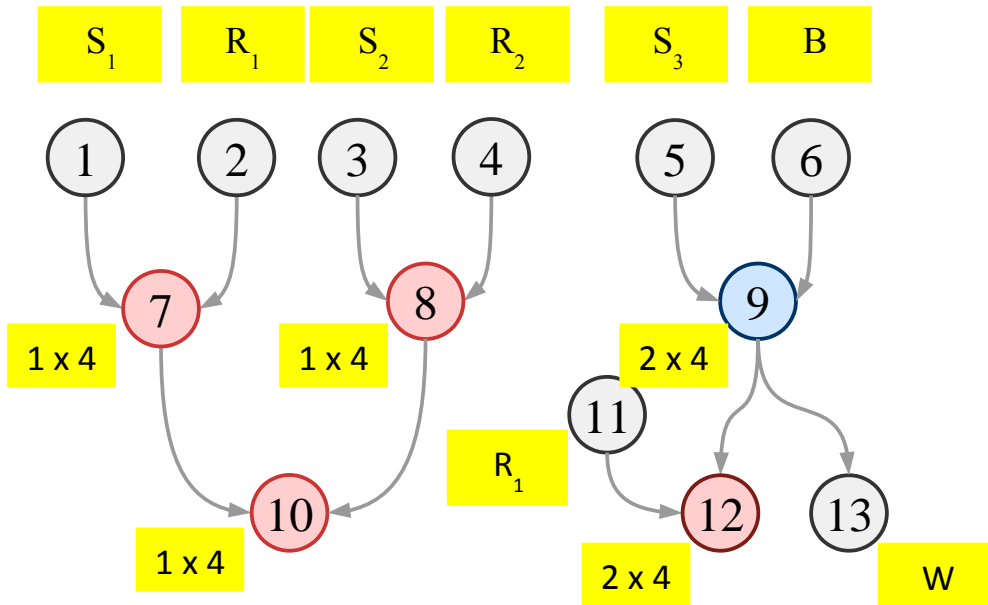


Application graph

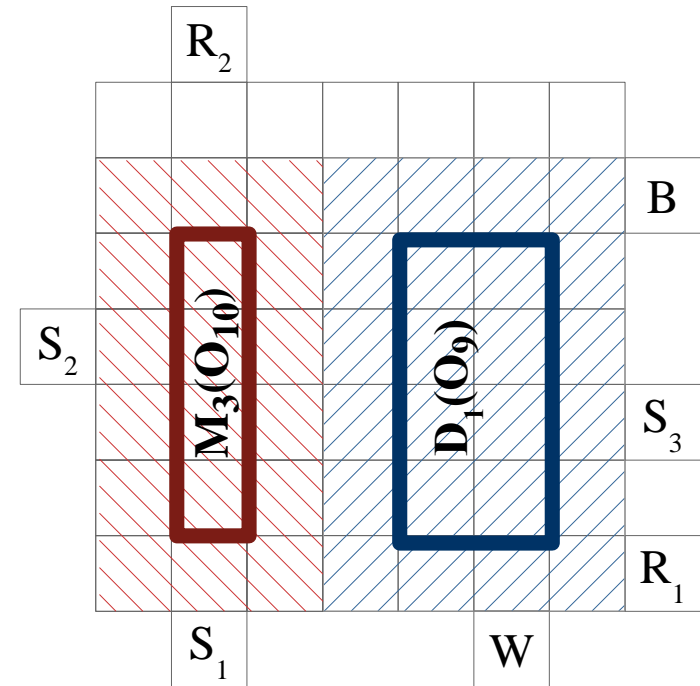


$t = 2.04 \text{ s}$

# Example

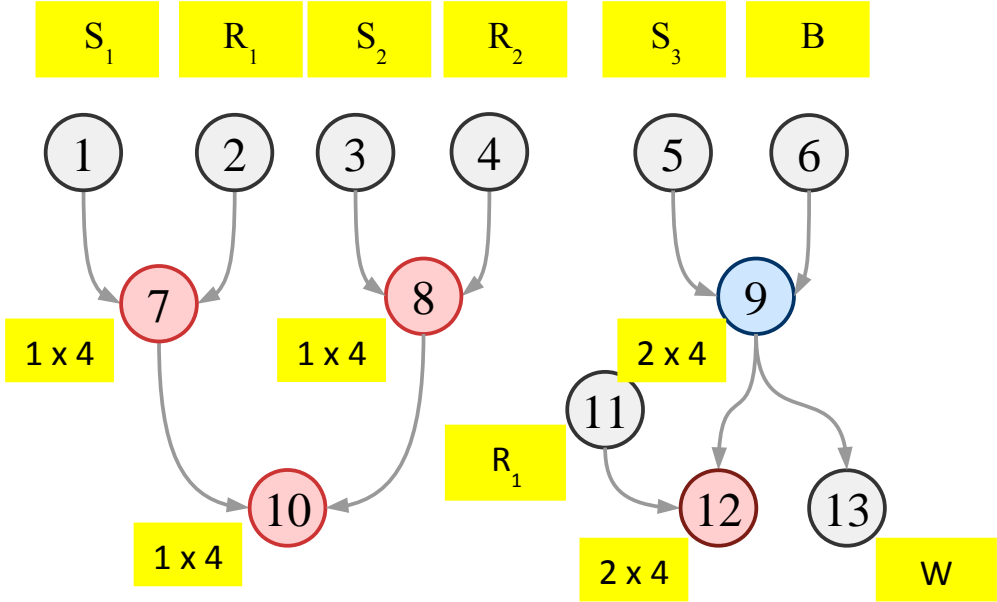


Application graph

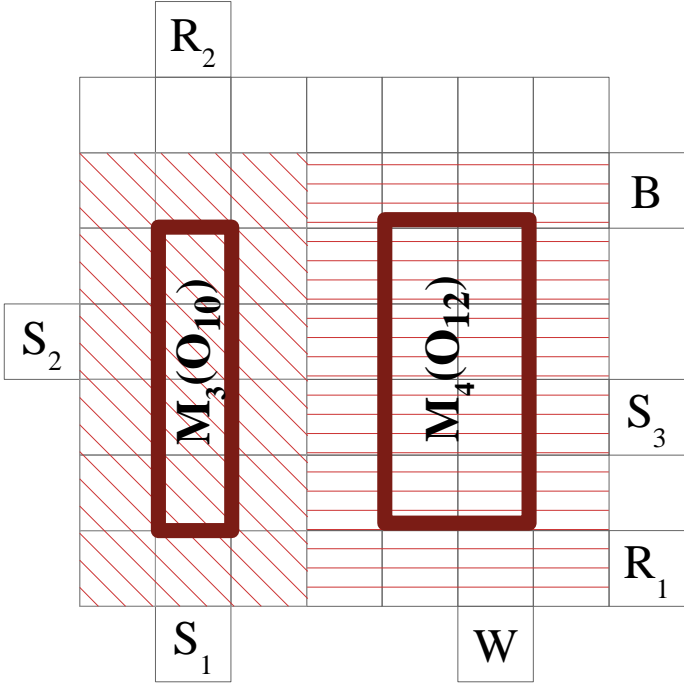


$t = 6.67 \text{ s}$

# Example

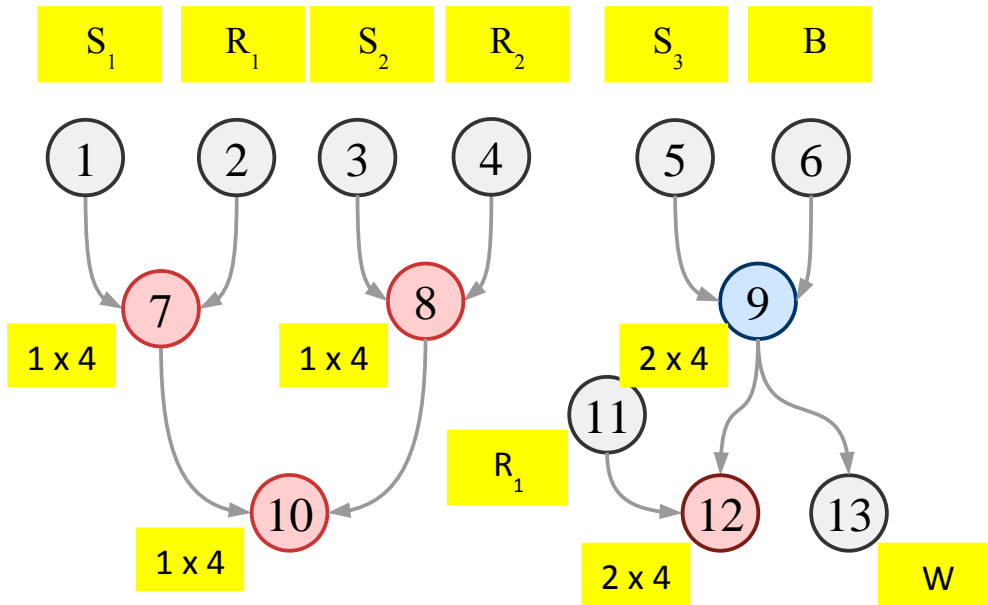


Application graph

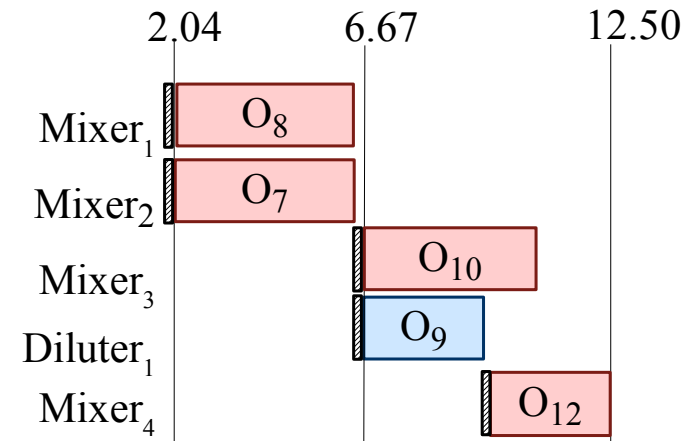


$t = 9.5 \text{ s}$

# Example

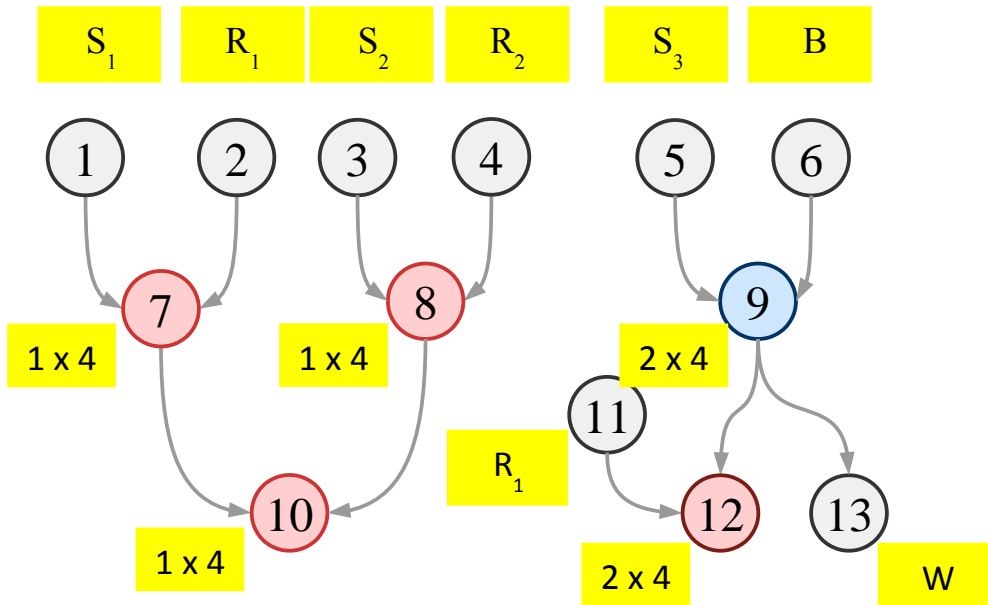


Application graph

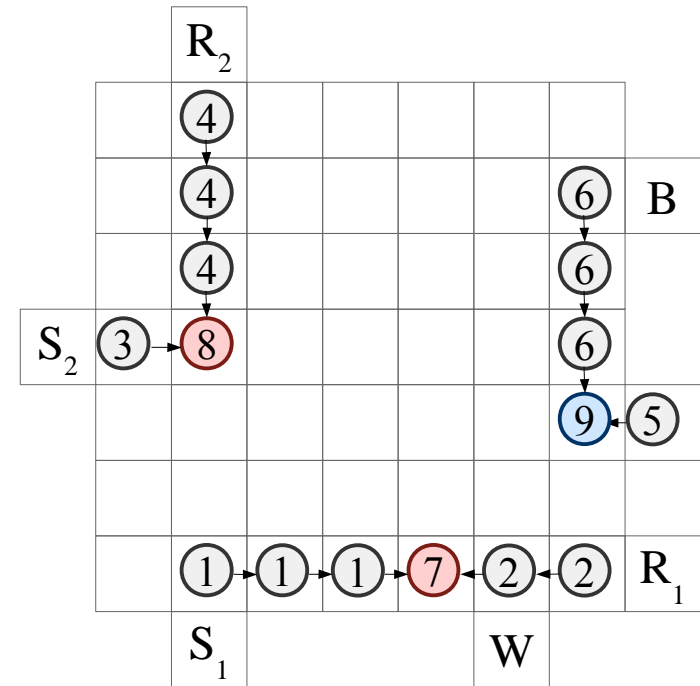


Schedule

# Example

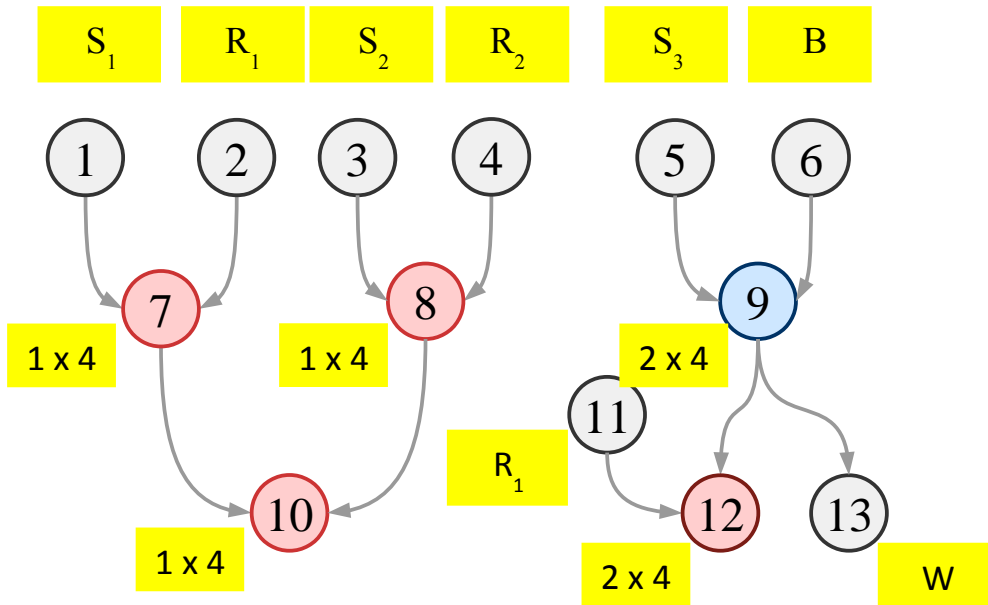


Application graph

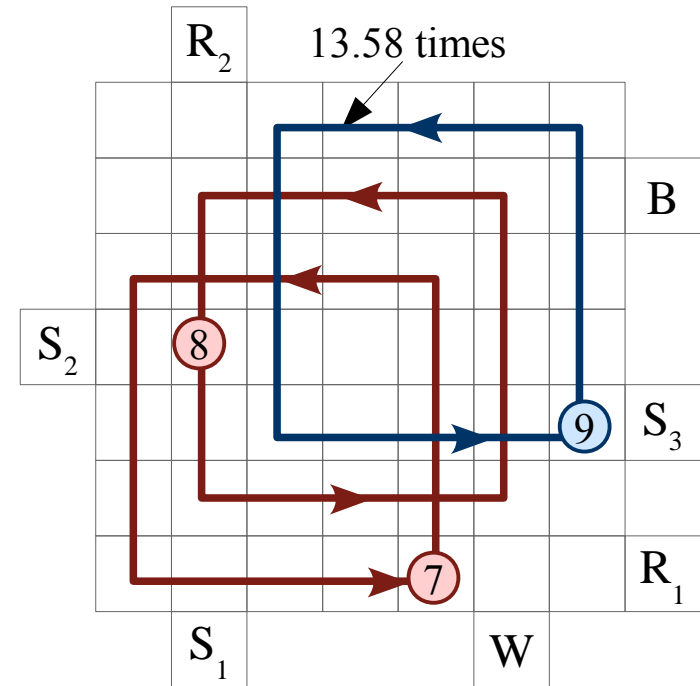


$t = 2.03 \text{ s}$

# Example



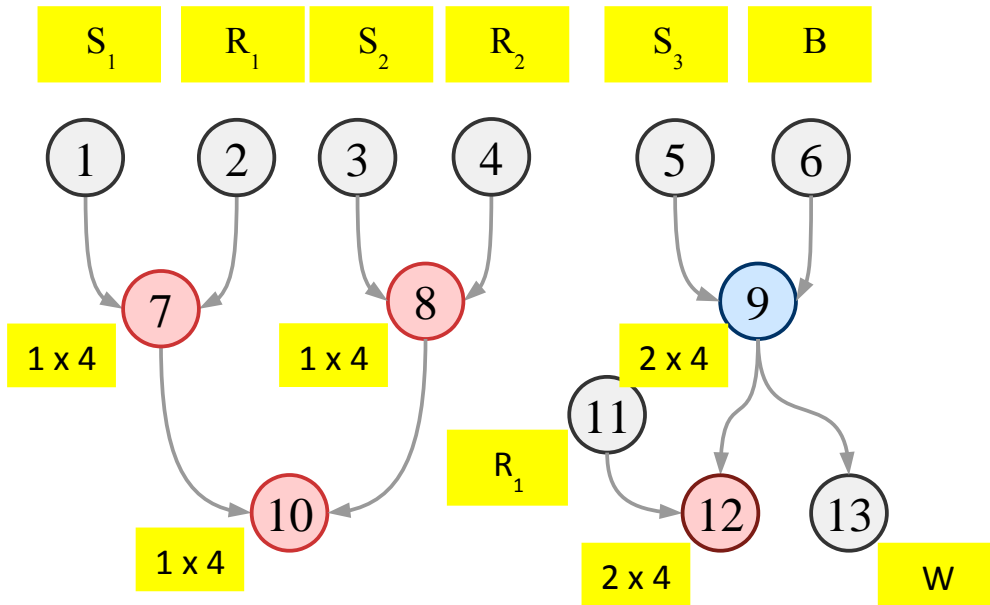
Application graph



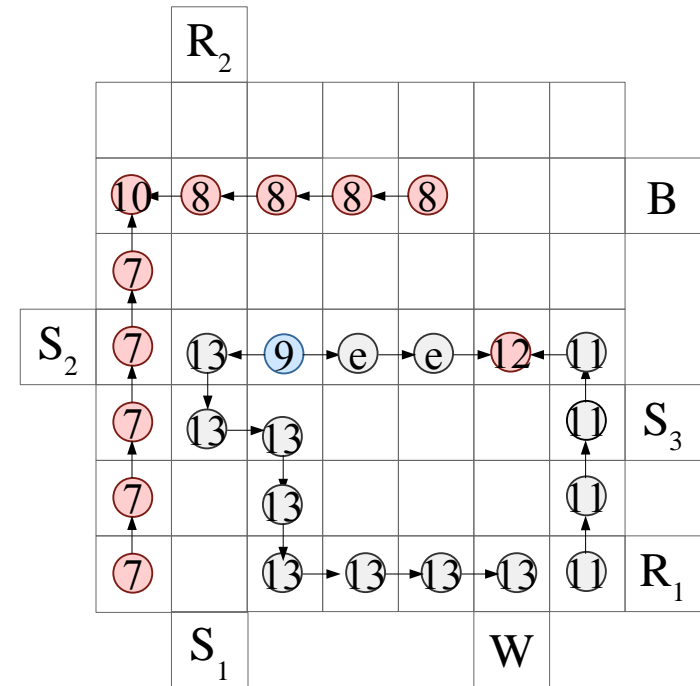
$$t = 4.20 \text{ s}$$



# Example

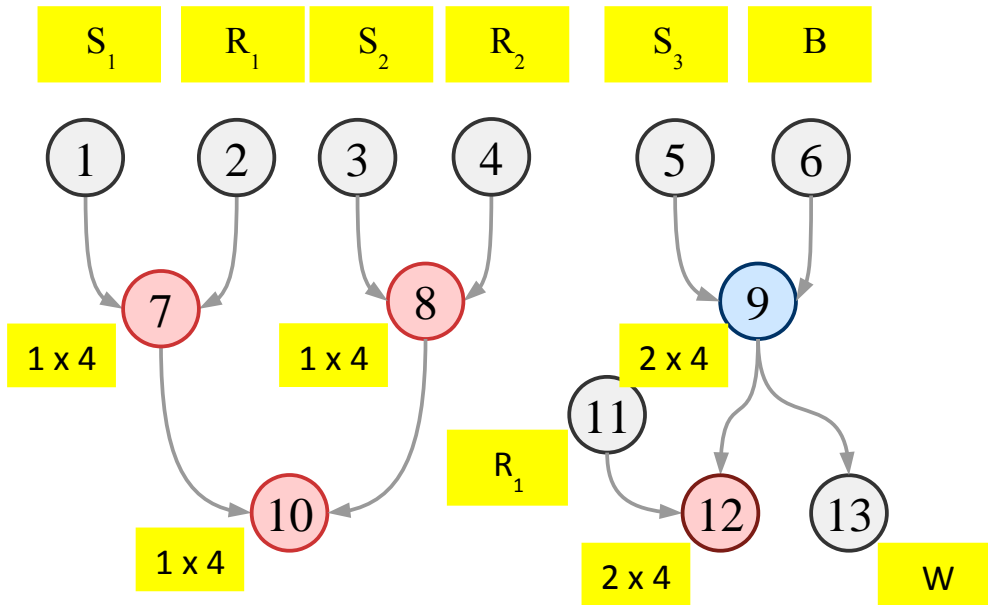


Application graph

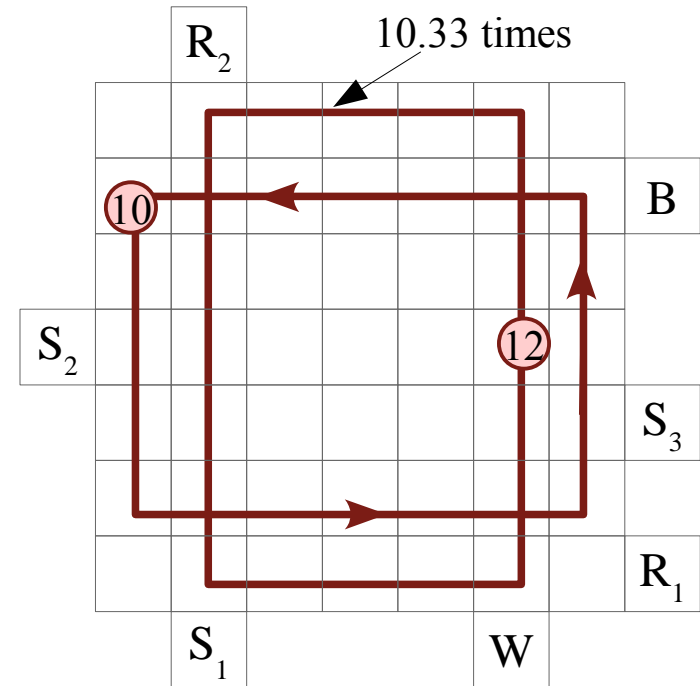


$t = 4.28 \text{ s}$

# Example

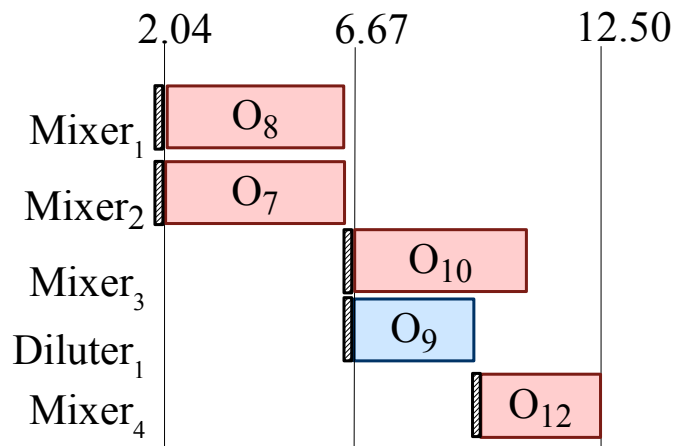


Application graph

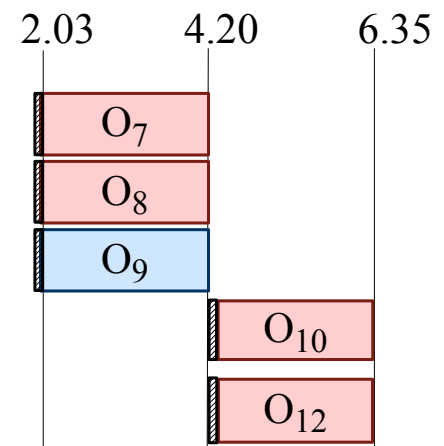


$t = 6.34 \text{ s}$

# Example

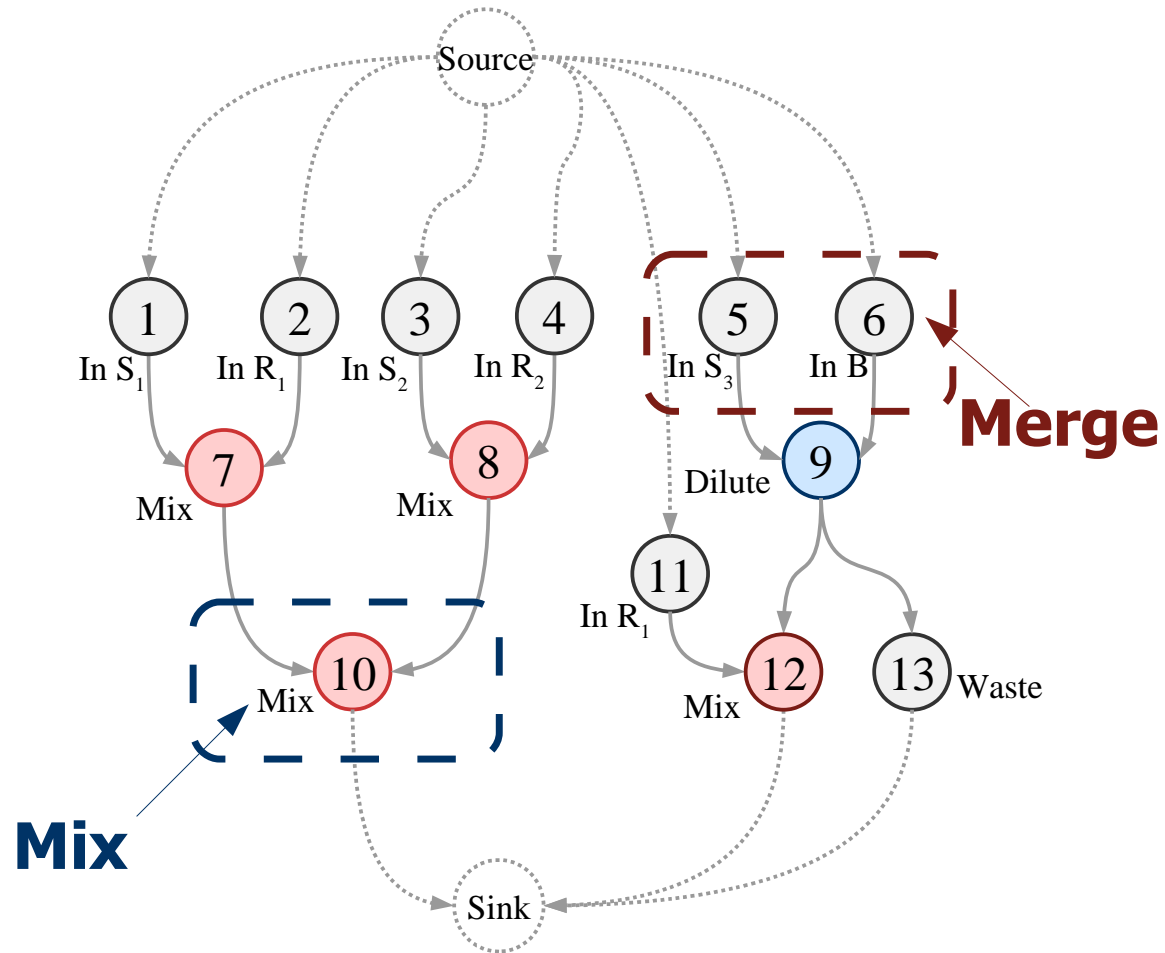


Schedule – module-based operation execution

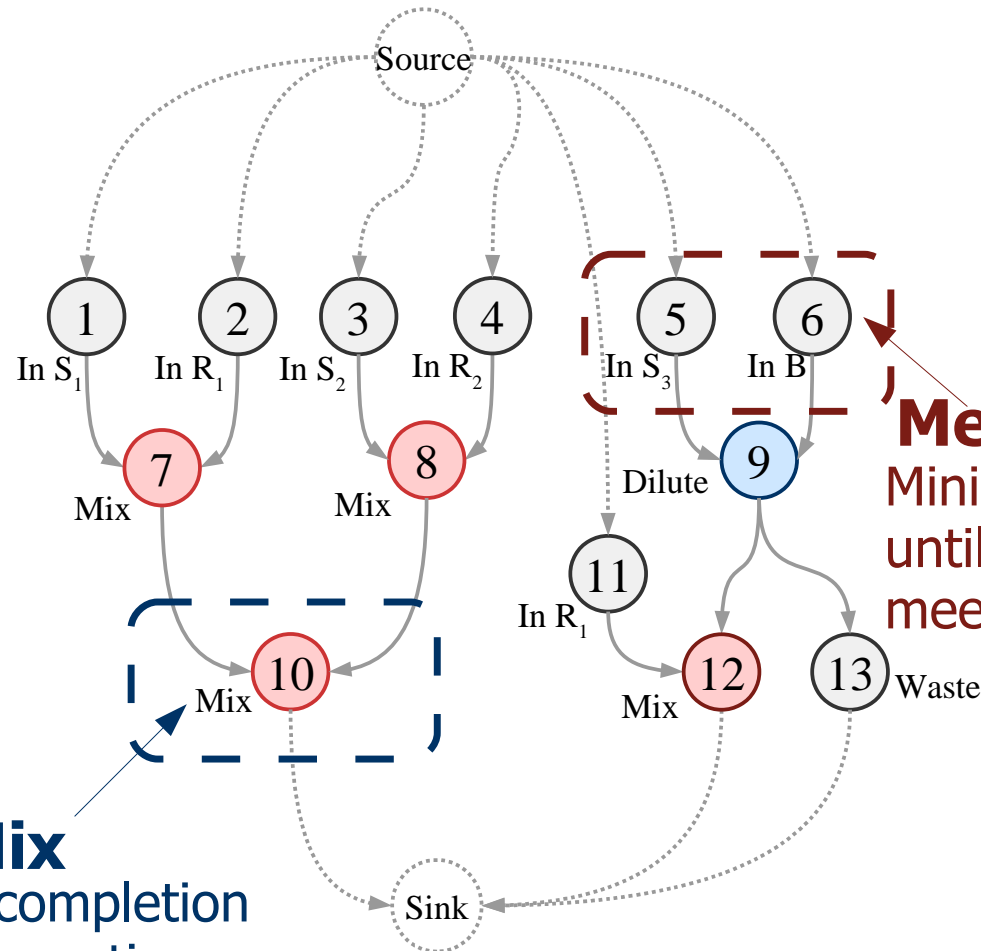


Schedule – routing-based operation execution

# Solution



# Solution

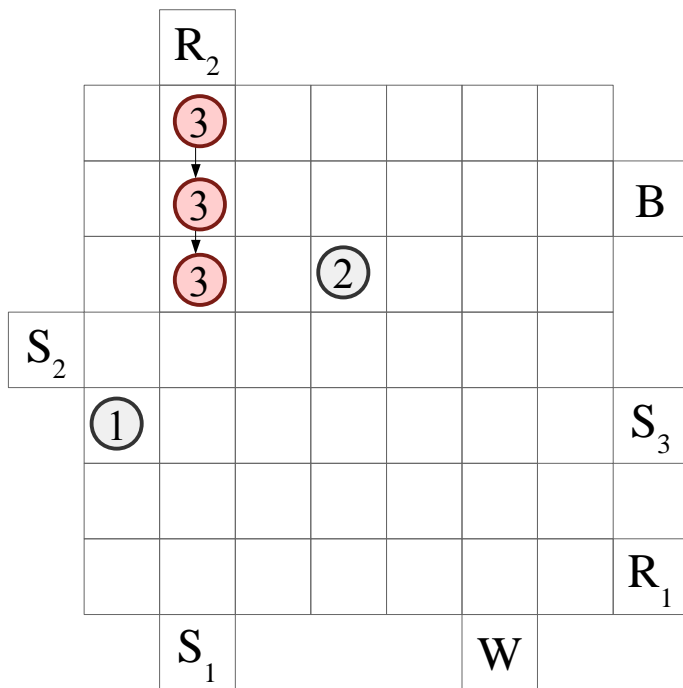


**Merge**  
Minimize the time  
until the droplets  
meet

**Mix**  
Minimize the completion  
time for the operation

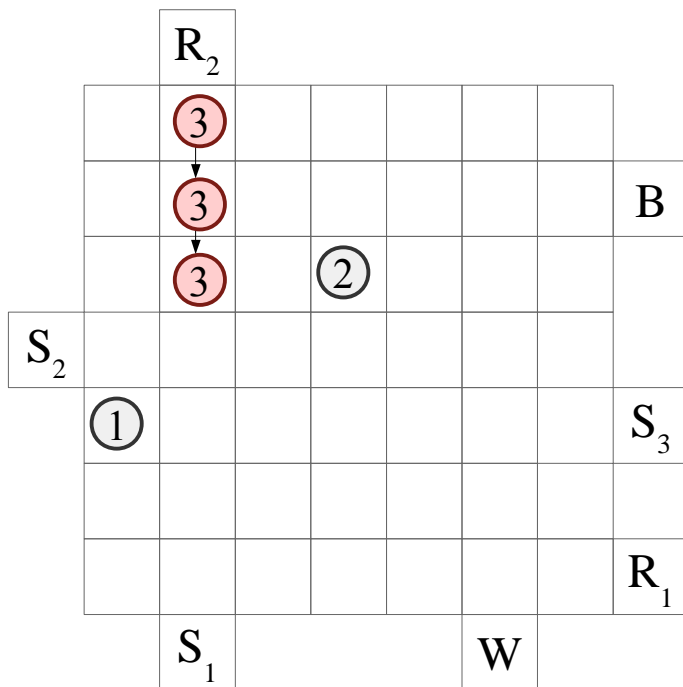
# Solution

- Greedy Randomized Adaptive Search Procedure (GRASP)



# Solution

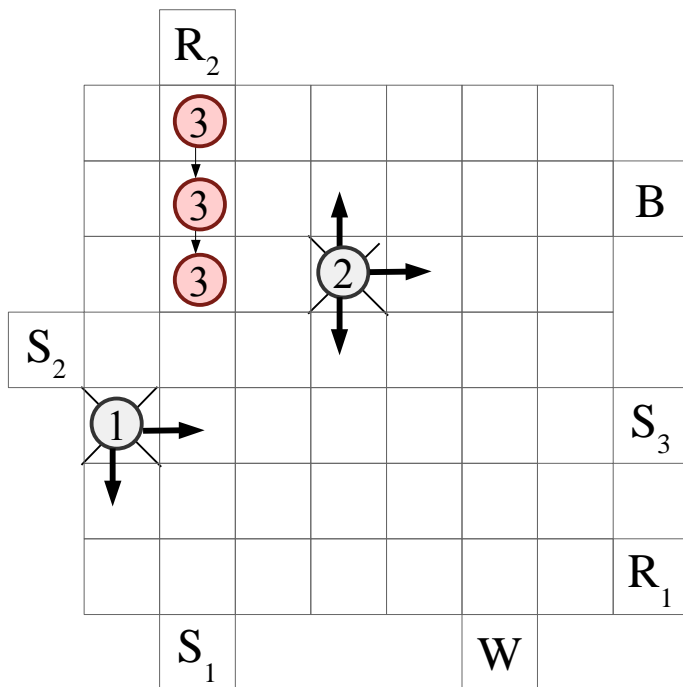
- Greedy Randomized Adaptive Search Procedure (GRASP)



- For each droplet:
  - Determine possible moves
  - Evaluate each move
    - Merge: minimize Manhattan distance
    - Mix: maximize operation execution
  - Make a list of the best  $N$  moves
  - Perform a random move from  $N$

# Solution

- Greedy Randomized Adaptive Search Procedure (GRASP)

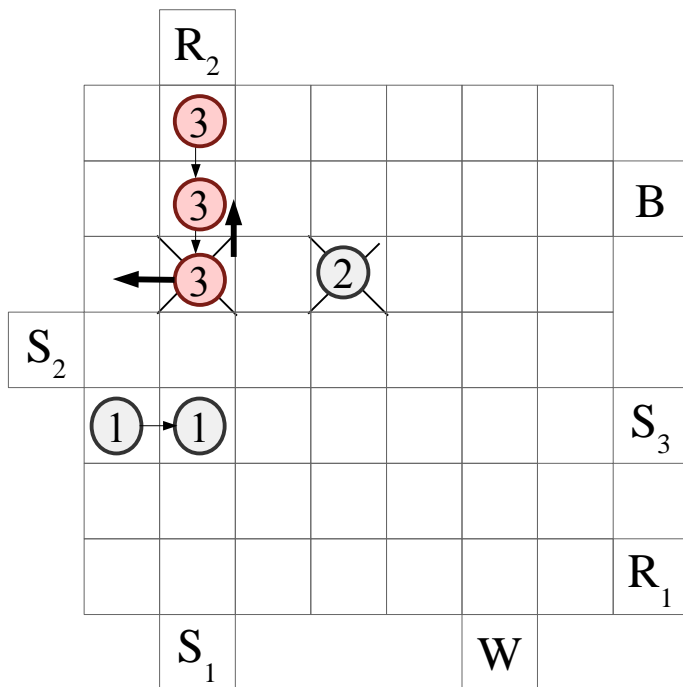


- For each droplet:
  - Determine possible moves
  - Evaluate each move
    - Merge: minimize Manhattan distance
    - Mix: maximize operation execution
  - Make a list of the best N moves
  - Perform a random move from N



# Solution

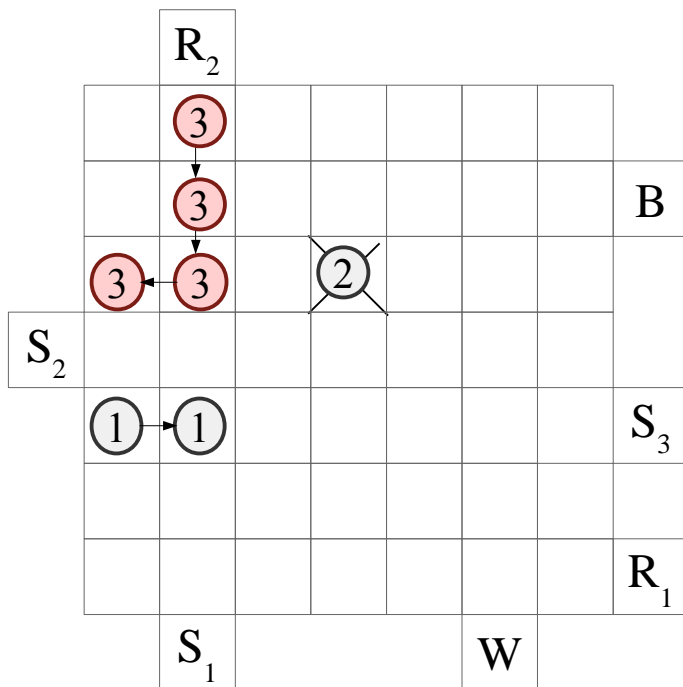
- Greedy Randomized Adaptive Search Procedure (GRASP)



- For each droplet:
  - Determine possible moves
  - Evaluate each move
    - Merge: minimize Manhattan distance
    - Mix: maximize operation execution
  - Make a list of the best N moves
  - Perform a random move from N

# Solution

- Greedy Randomized Adaptive Search Procedure (GRASP)



- For each droplet:
  - Determine possible moves
  - Evaluate each move
    - Merge: minimize Manhattan distance
    - Mix: maximize operation execution
  - Make a list of the best N moves
  - Perform a random move from N

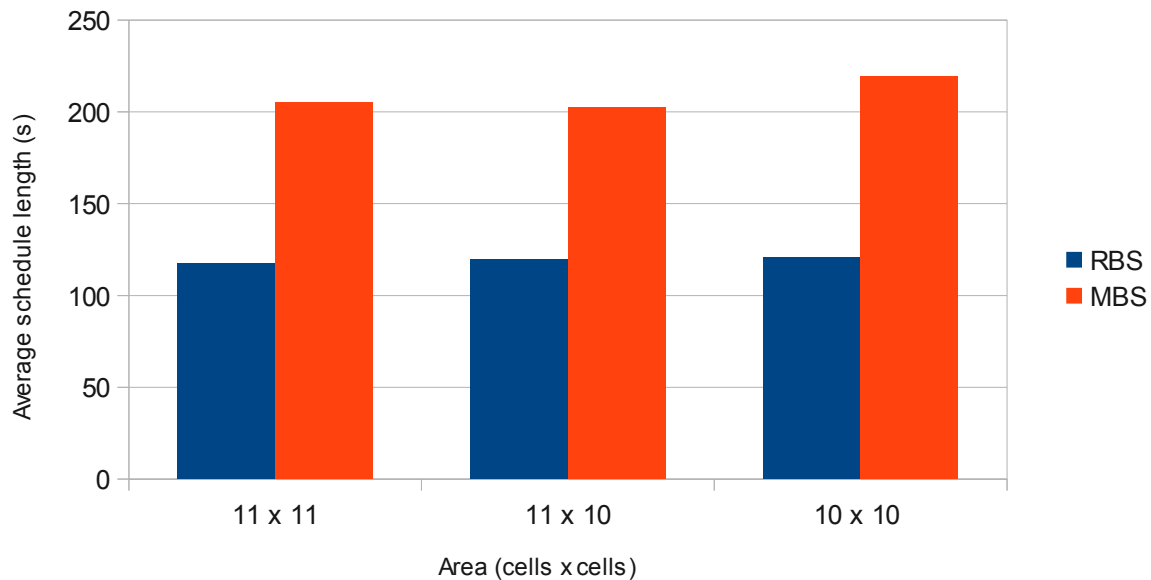
# Experimental Evaluation

- GRASP-based algorithm implemented in Java
- Benchmarks
  - Real-life applications
    - Colorimetric protein assay
  - Synthetic benchmarks
    - 10 TGFF-generated benchmarks with 10 to 100 operations
- Comparison between:
  - Routing-based synthesis (RBS)
  - Module-based synthesis with fixed modules (MBS)

# Experimental Evaluation

Average schedule length out of 50 runs for **RBS** vs. **MBS**

Colorimetric protein assay



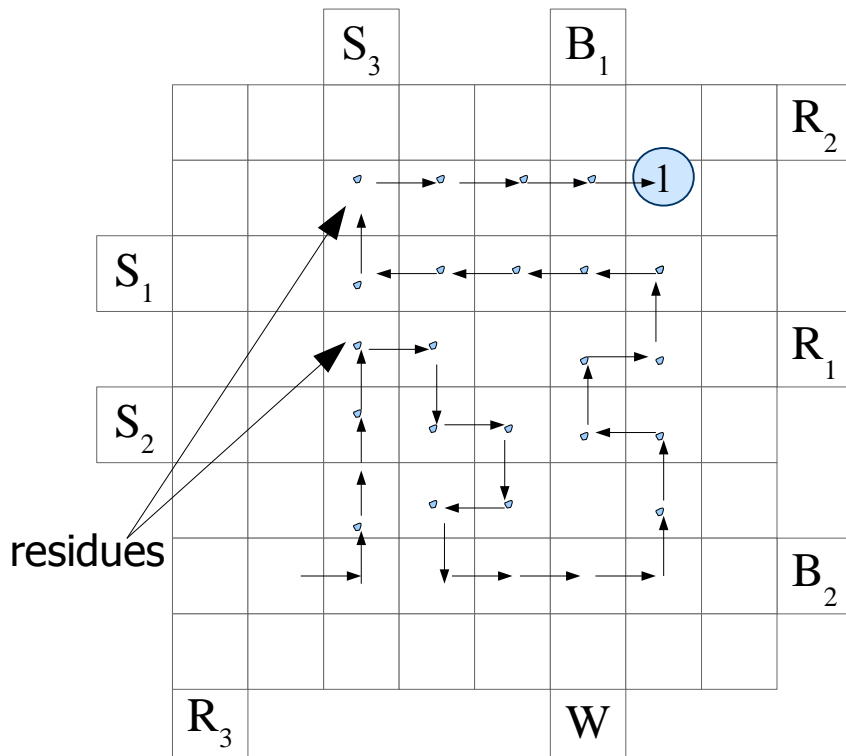
44.95 % improvement for 10 x 10

# Routing-Based Operation Execution - Conclusions

- Improved completion time compared to module-based synthesis
- Challenge: contamination

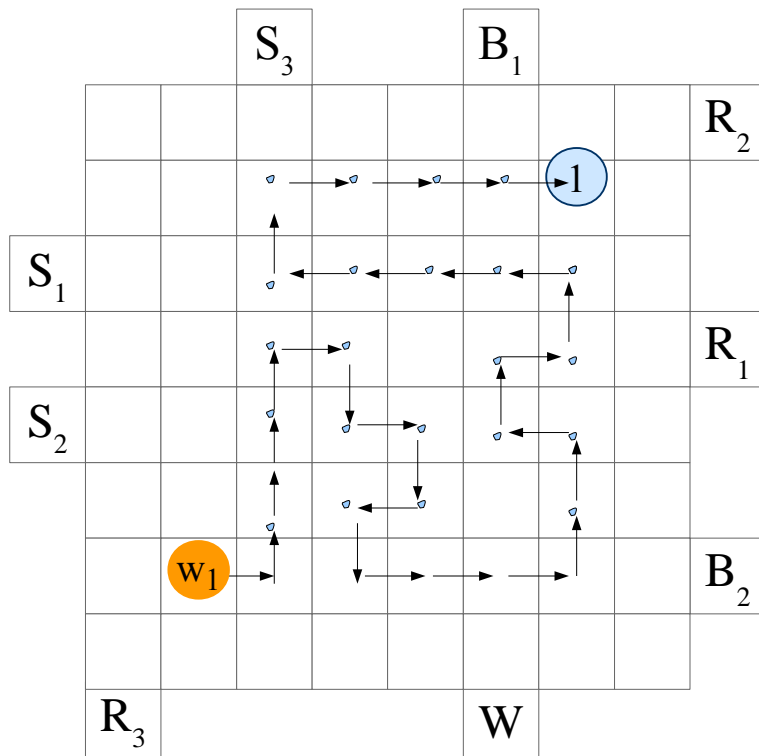
# Routing-Based Operation Execution - Conclusions

- Improved completion time compared to module-based synthesis
- Challenge: contamination



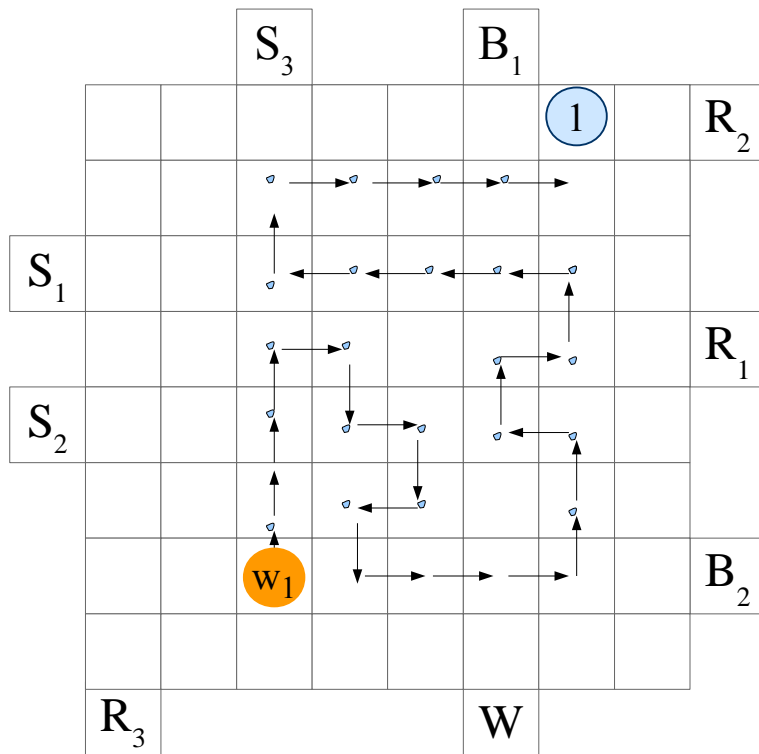
# Routing-Based Operation Execution - Conclusions

- Improved completion time compared to module-based synthesis
- Challenge: contamination



# Routing-Based Operation Execution - Conclusions

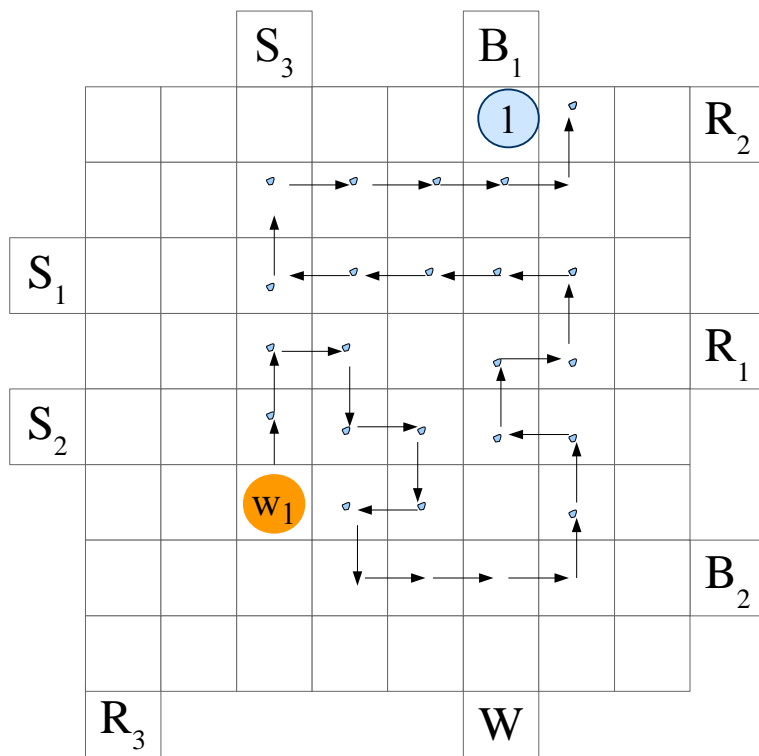
- Improved completion time compared to module-based synthesis
- Challenge: contamination





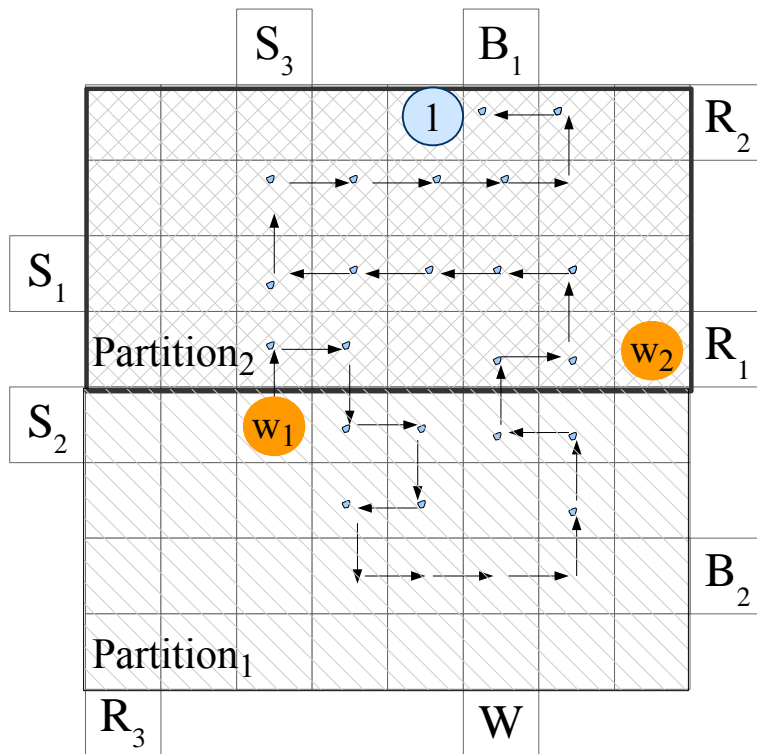
# Routing-Based Operation Execution - Conclusions

- Improved completion time compared to module-based synthesis
- Challenge: contamination



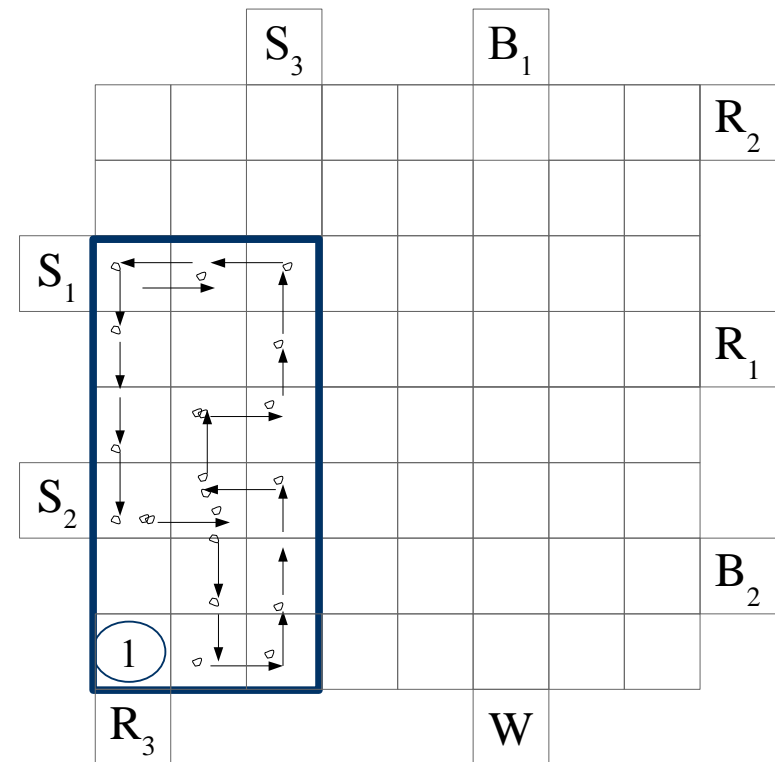
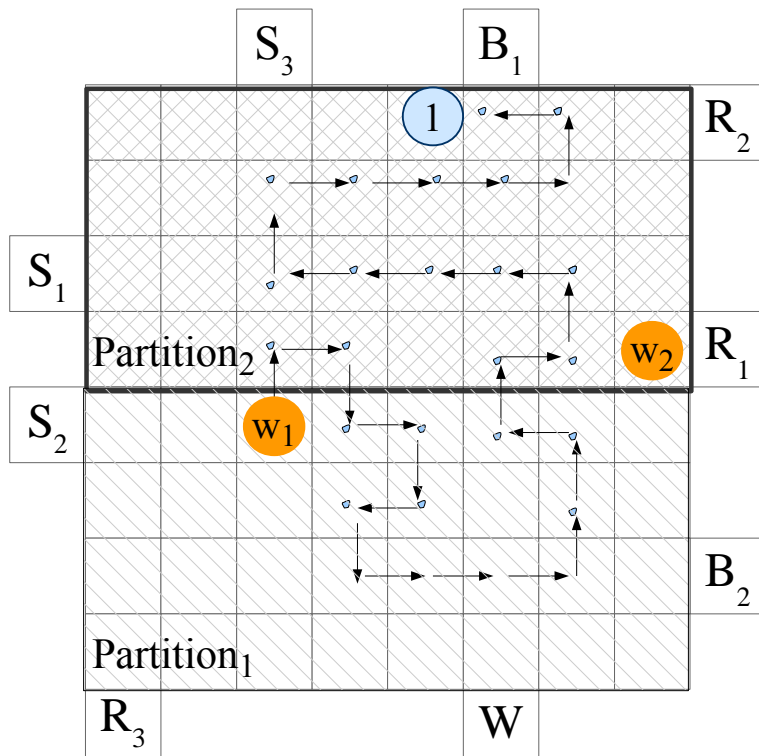
# Routing-Based Operation Execution - Conclusions

- Improved completion time compared to module-based synthesis
- Challenge: contamination



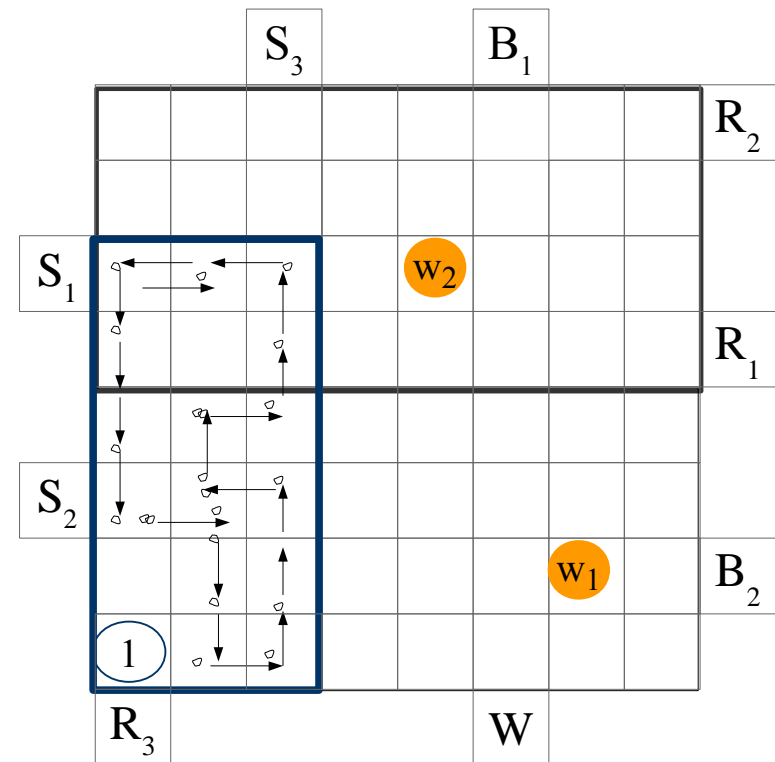
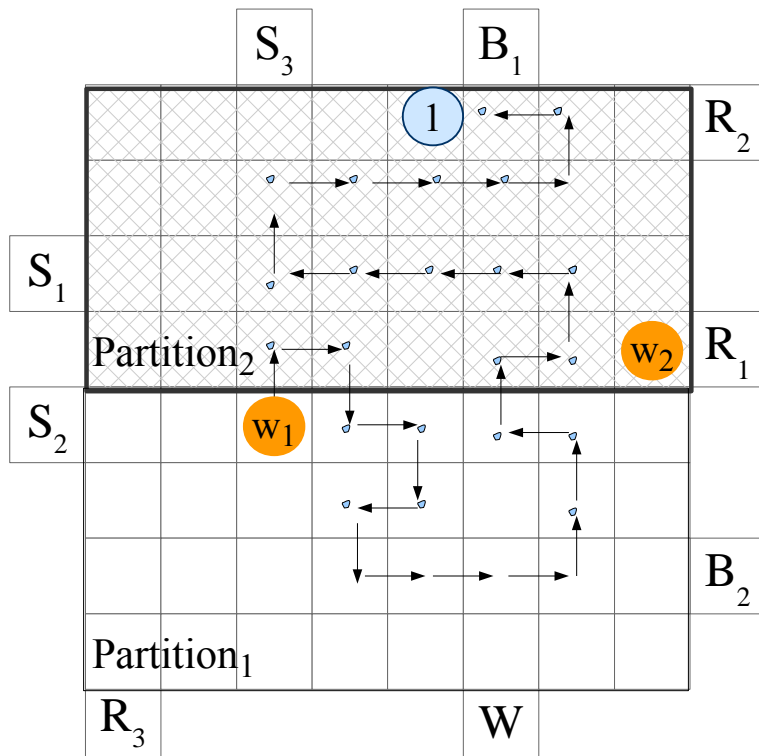
# Routing-Based Operation Execution - Conclusions

- Improved completion time compared to module-based synthesis
- Challenge: contamination



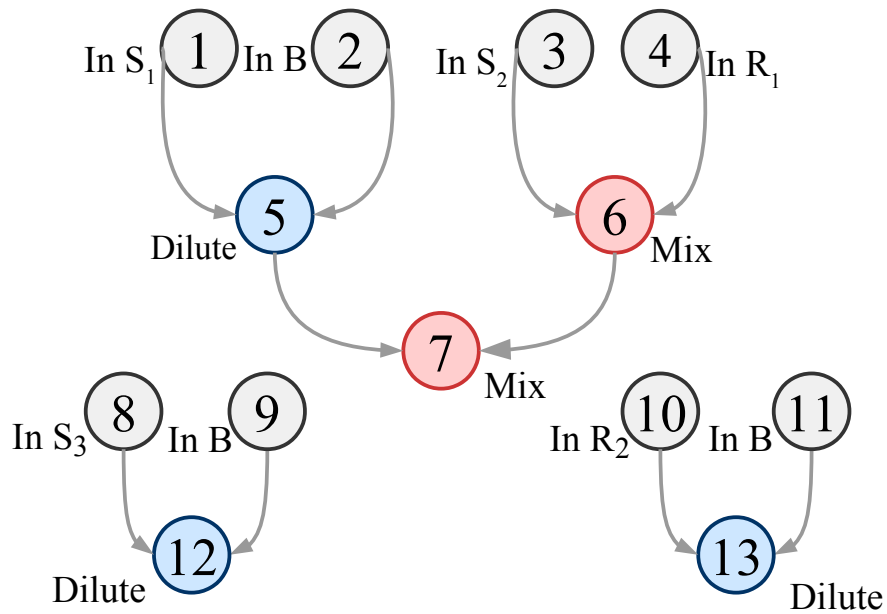
# Routing-Based Operation Execution - Conclusions

- Improved completion time compared to module-based synthesis
- Challenge: contamination

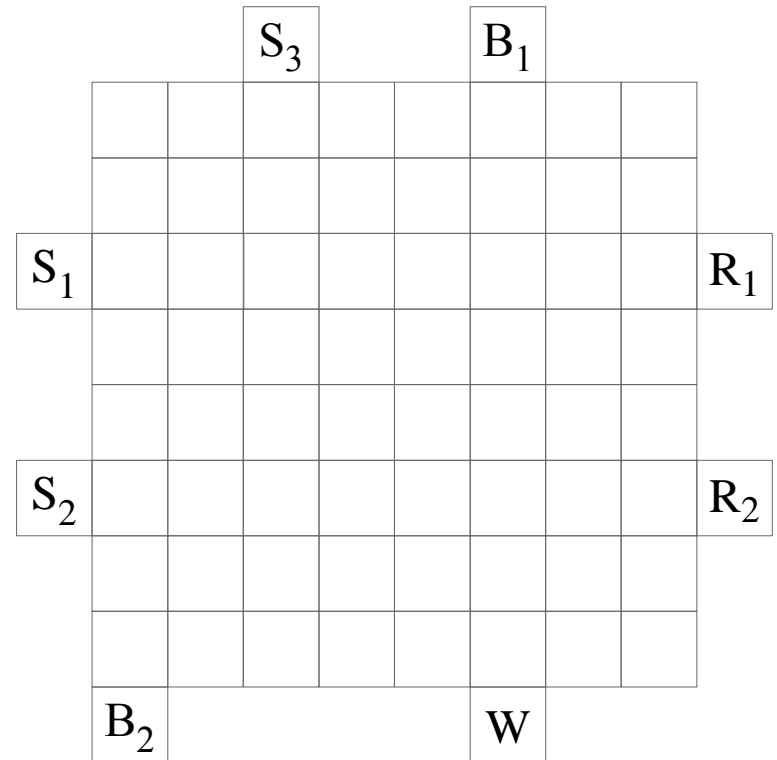


# Droplet-Aware Operation Execution without Contamination

# Example

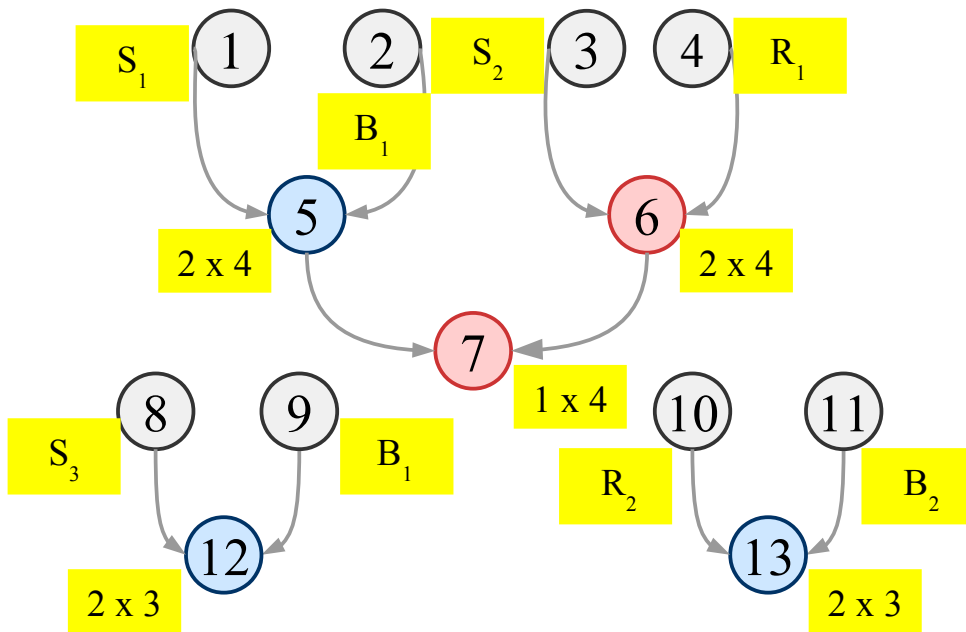


Application graph

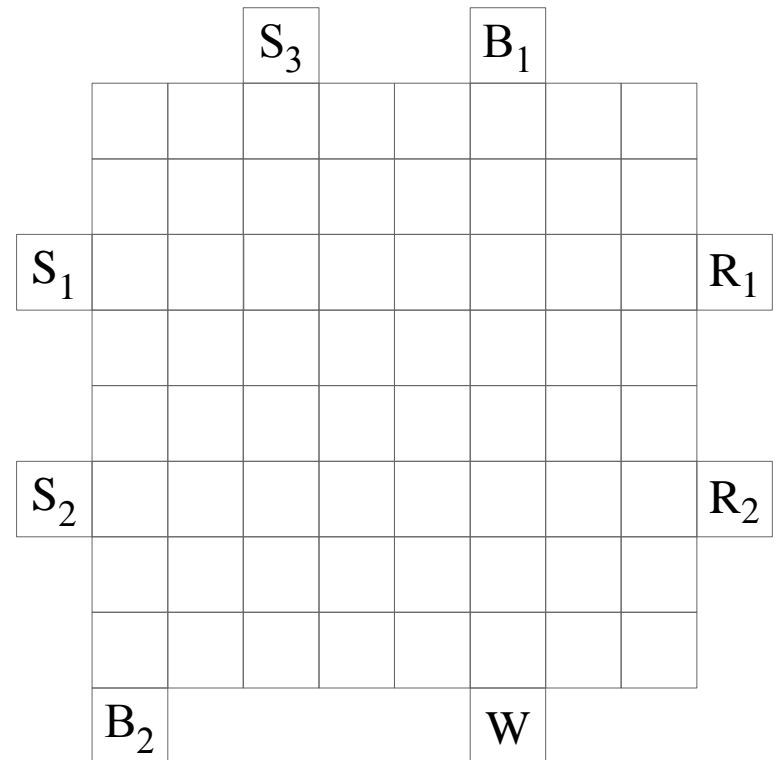


Biochip

# Example

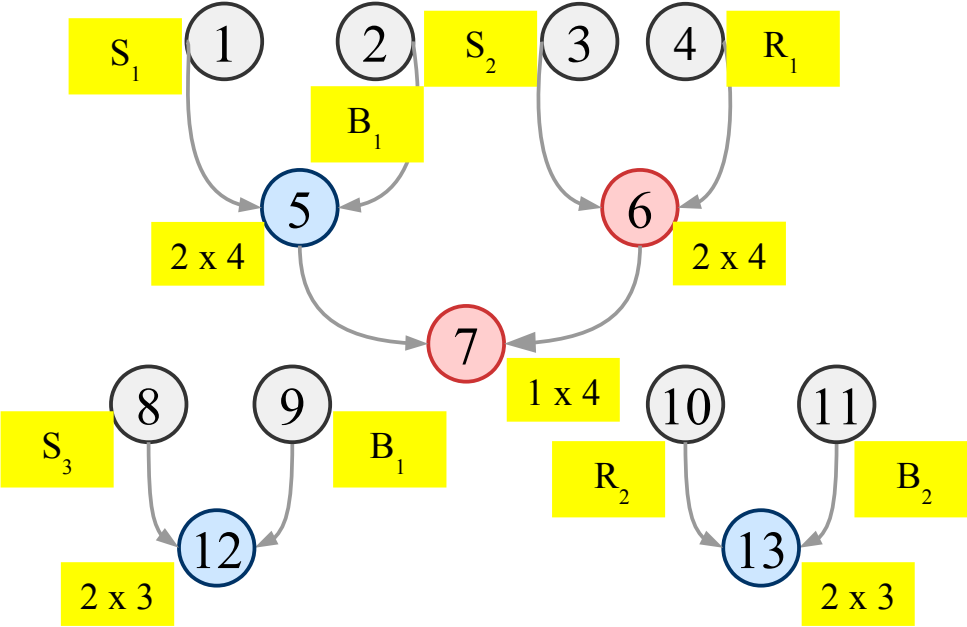


Application graph

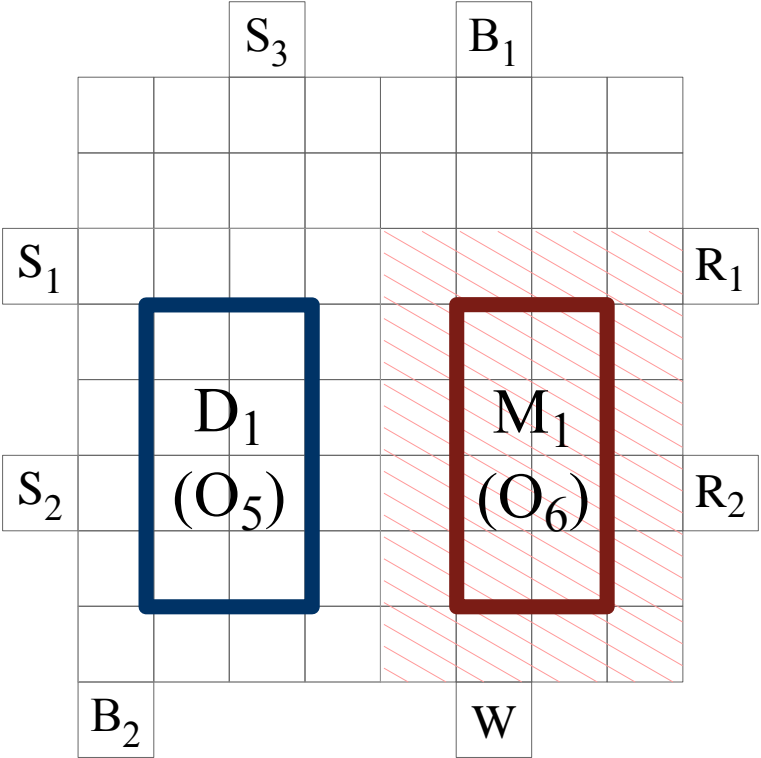


Biochip

# Example



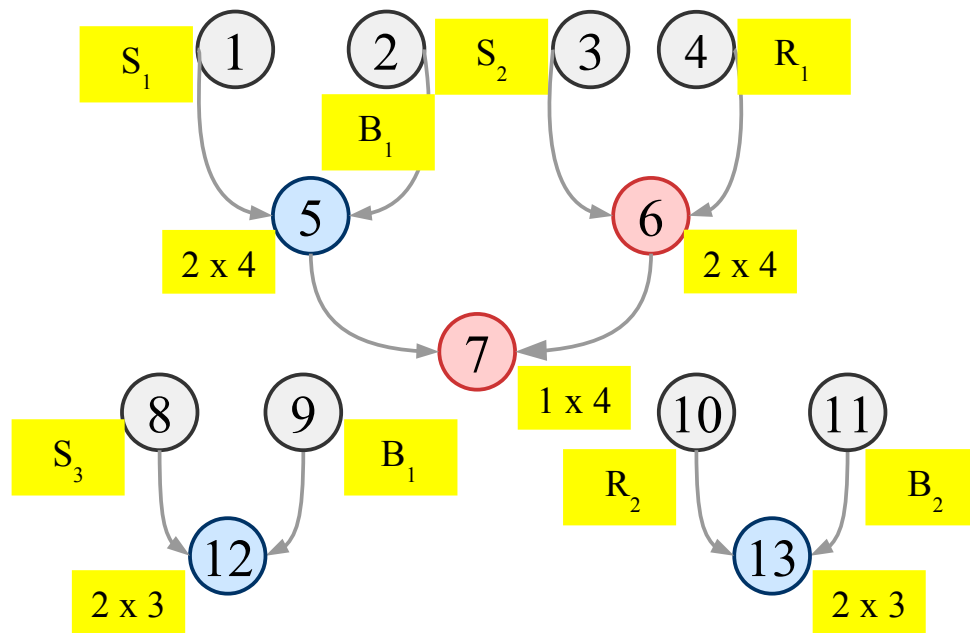
Application graph



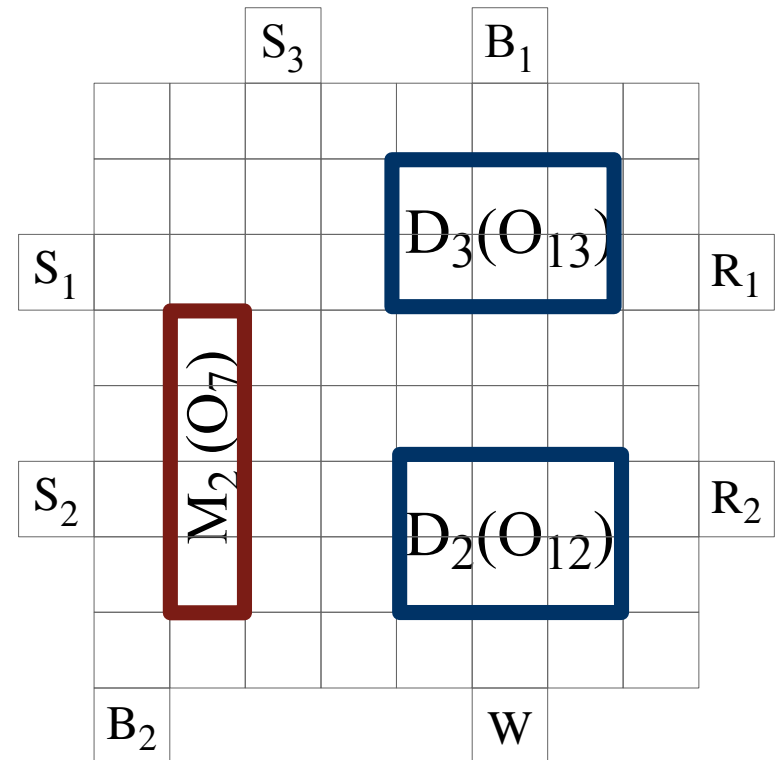
$t = 2s$



# Example

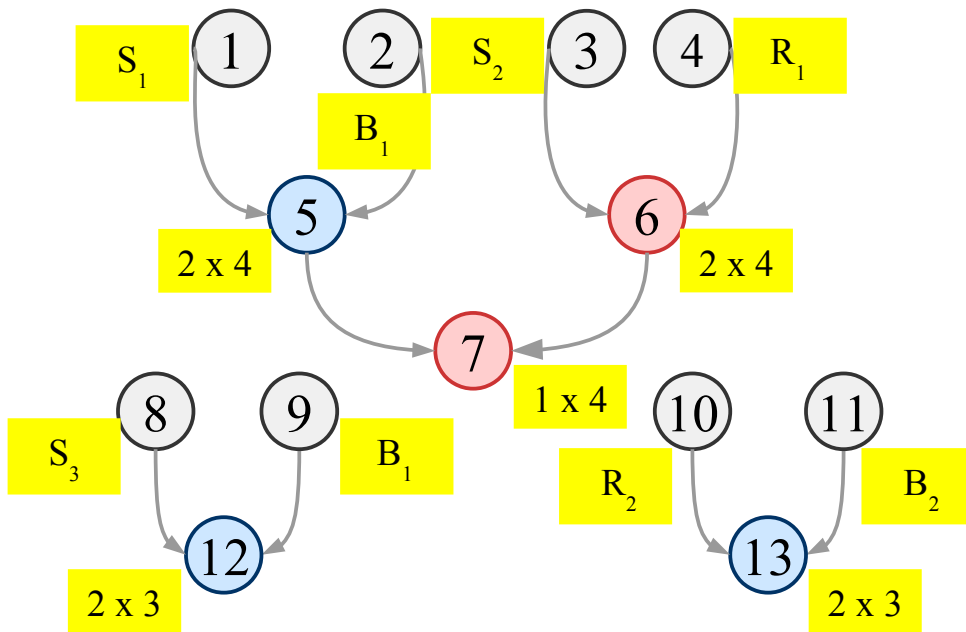


Application graph

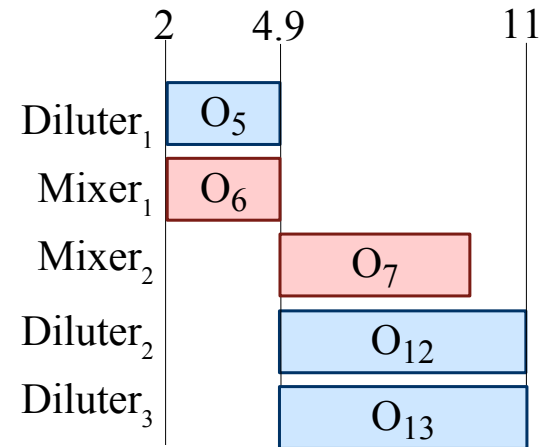


$t = 4.9$  s

# Example

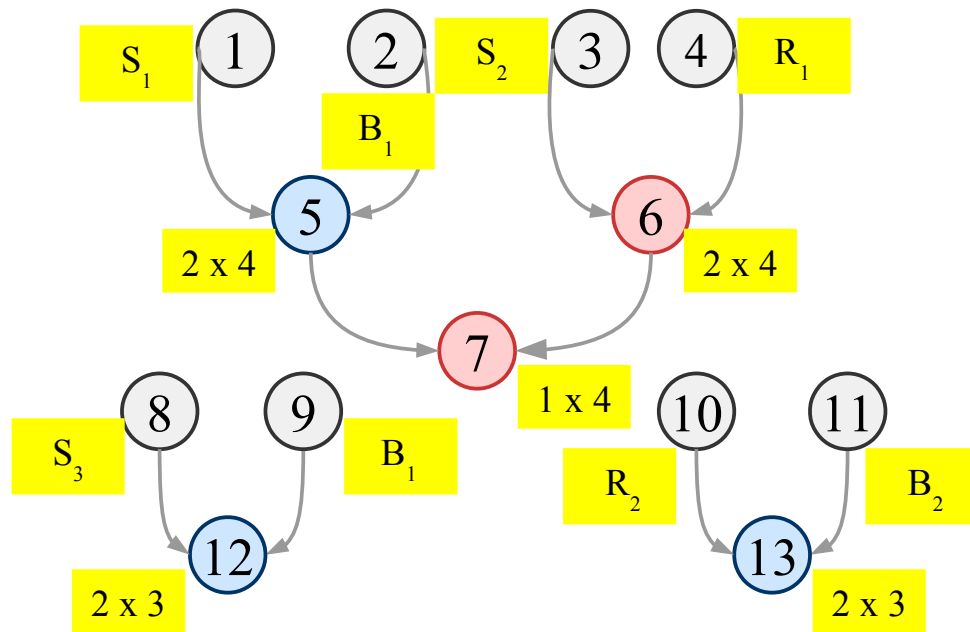


Application graph

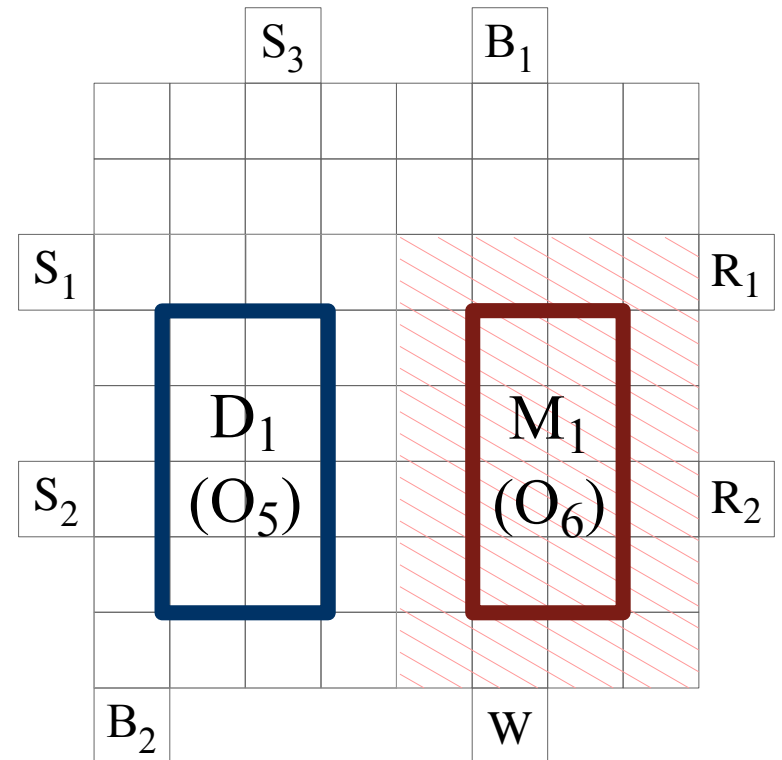


Schedule

# Example

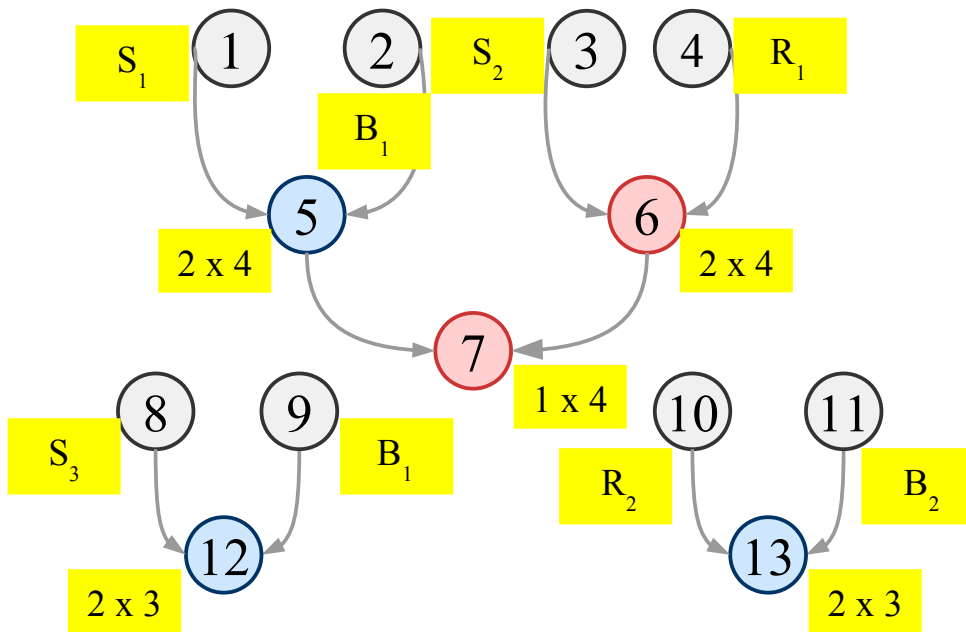


Application graph

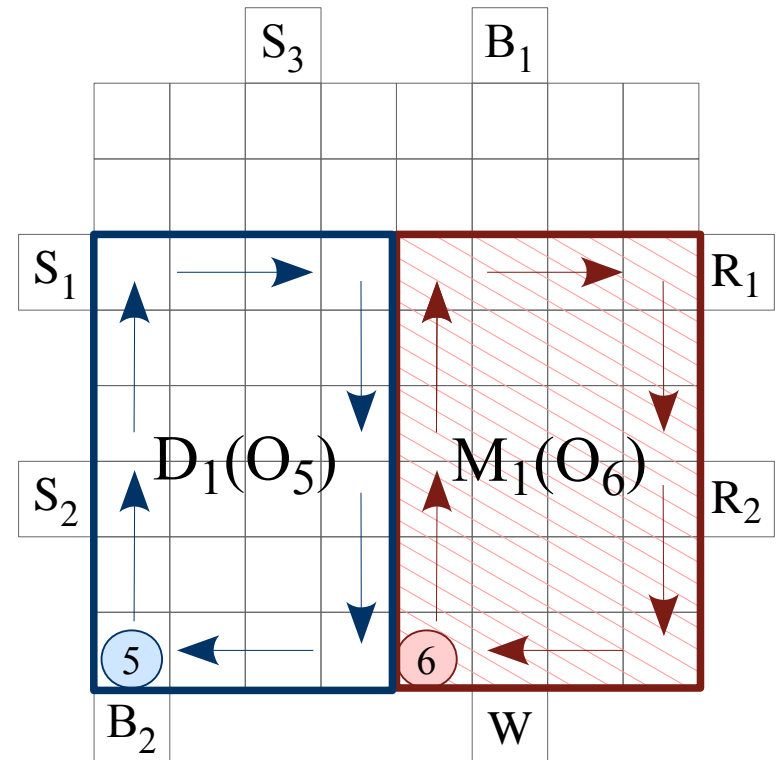


$t = 2s$

# Example

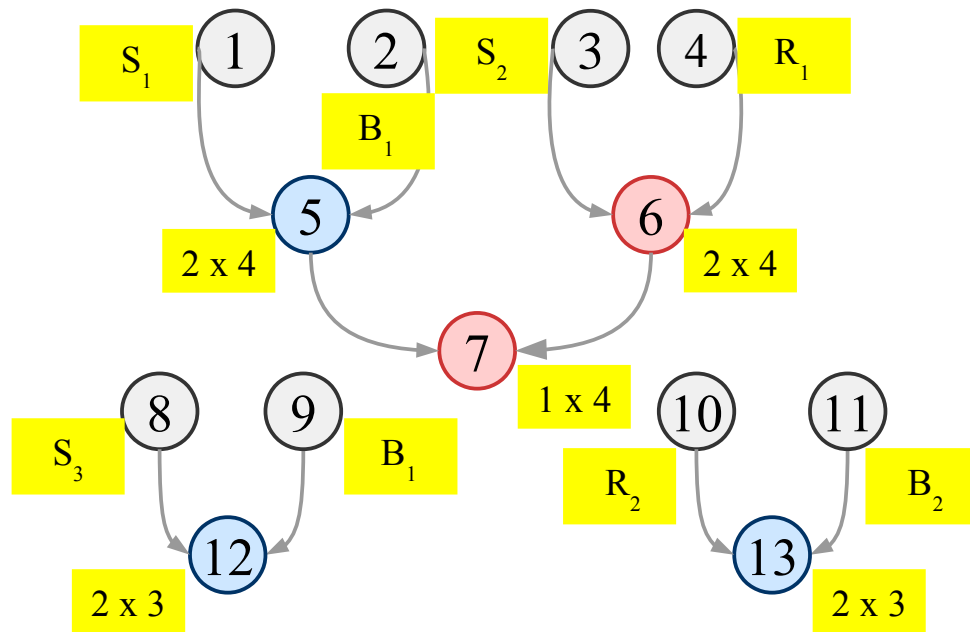


Application graph

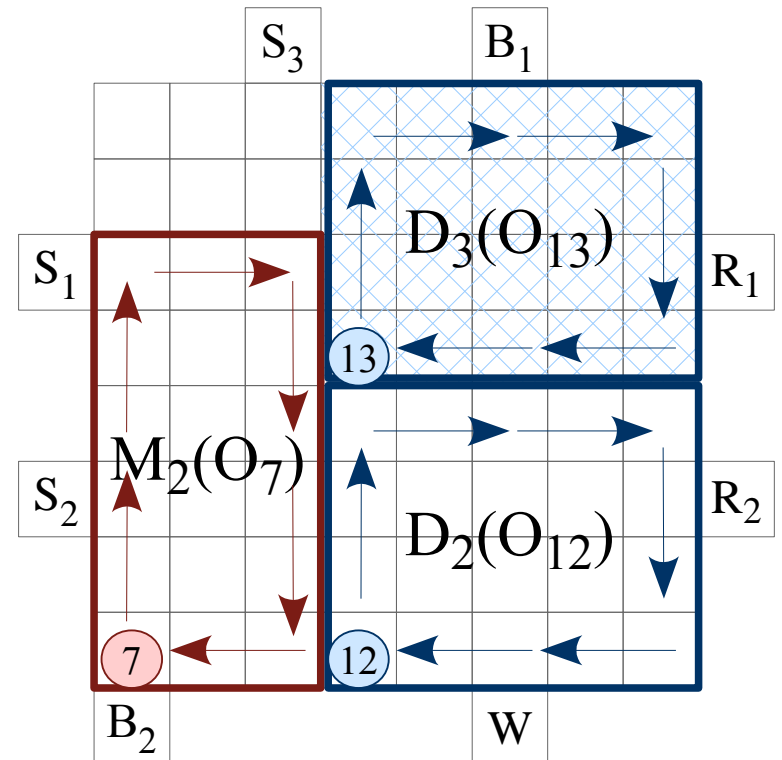


$t = 2s$

# Example

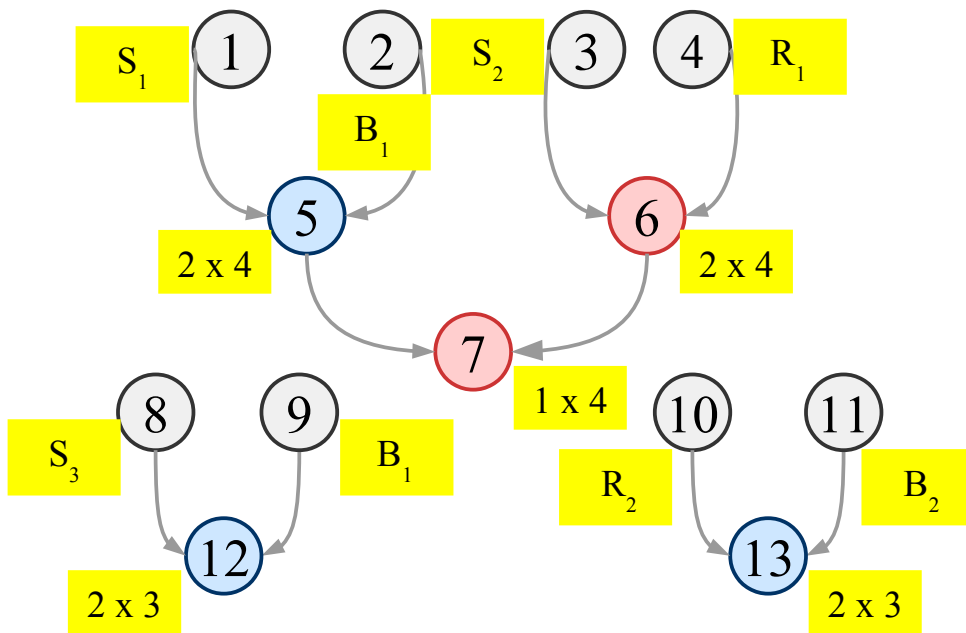


Application graph

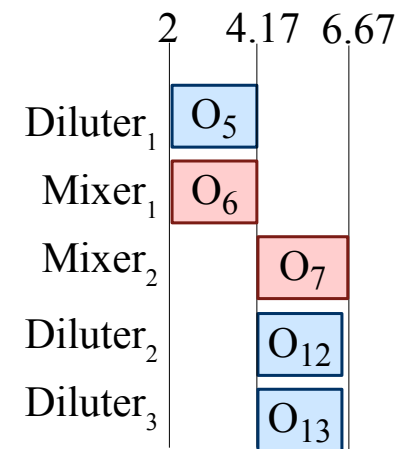


$t = 4.17$  s

# Example

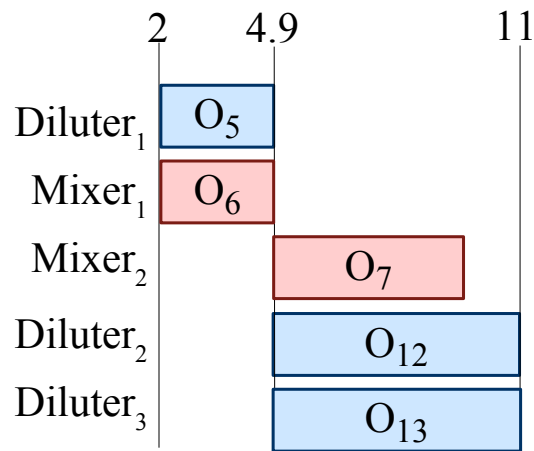


Application graph

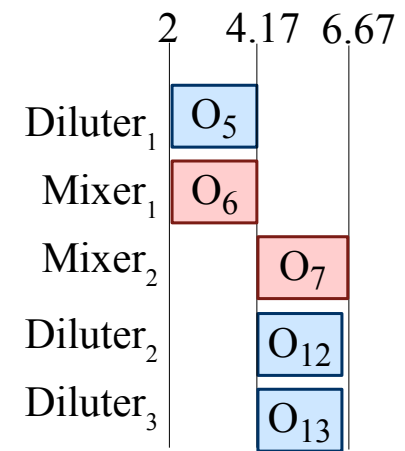


Schedule

# Example



Schedule – module-based operation execution



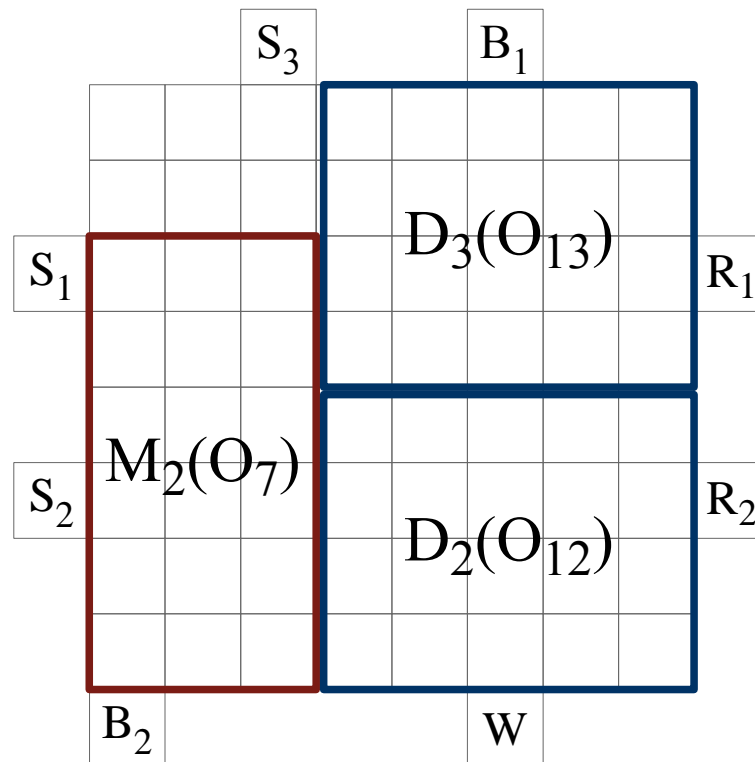
Schedule – droplet-aware operation execution

# Solution

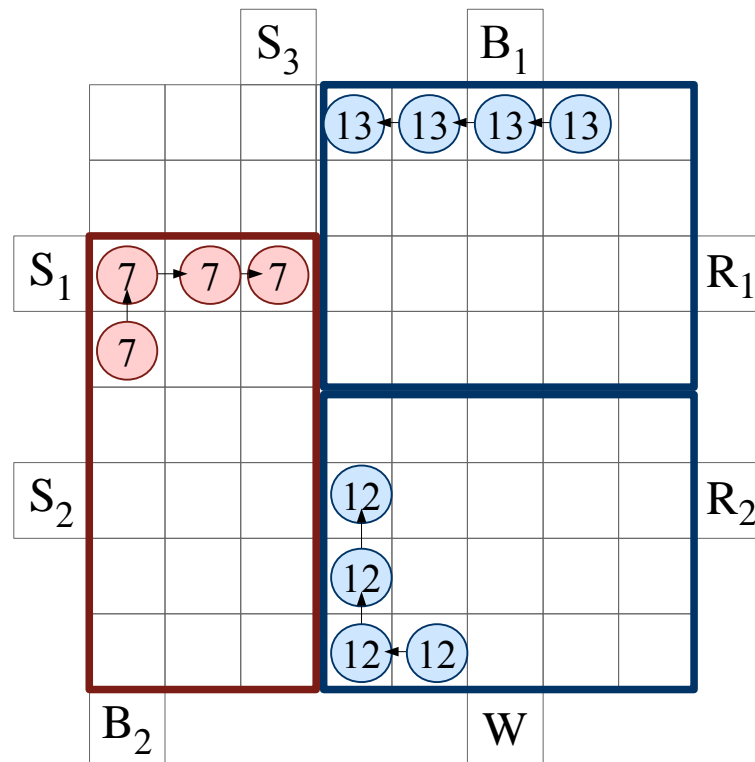
- Location of modules determined using Tabu Search
- Greedy movement of droplets inside modules
- Routing of droplets between modules and between modules and I/O ports determined using GRASP



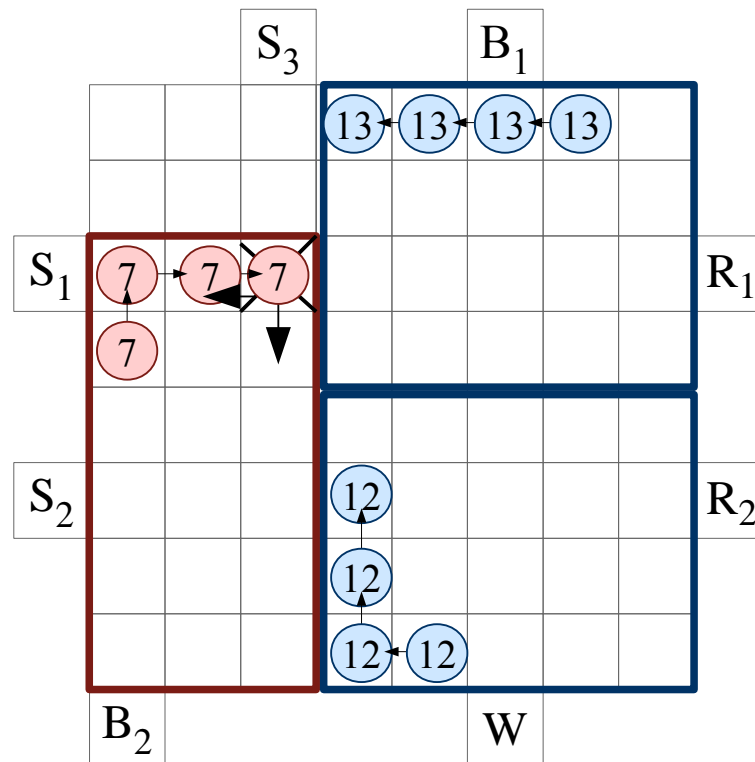
# Droplet-Aware Operation Execution



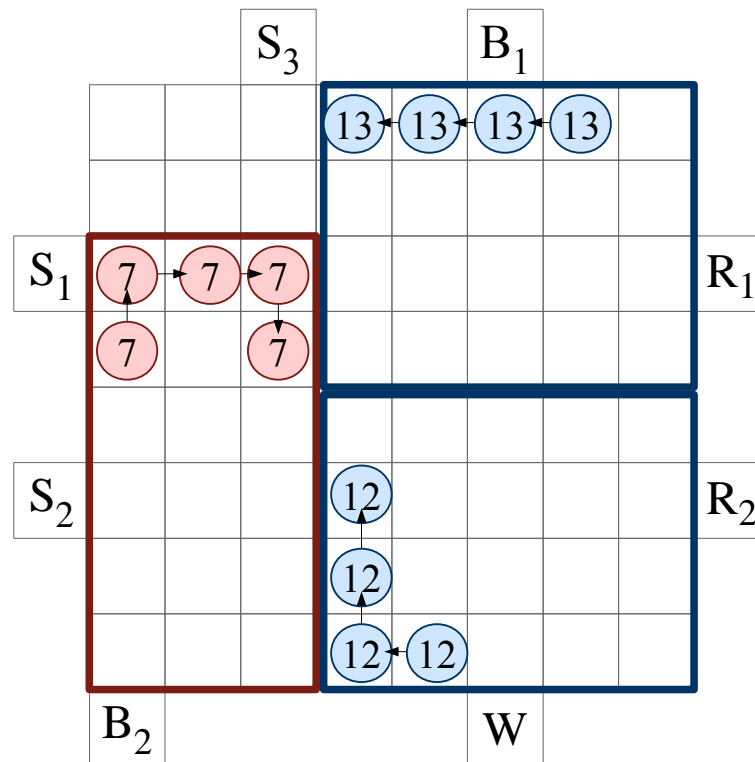
# Droplet-Aware Operation Execution



# Droplet-Aware Operation Execution



# Droplet-Aware Operation Execution



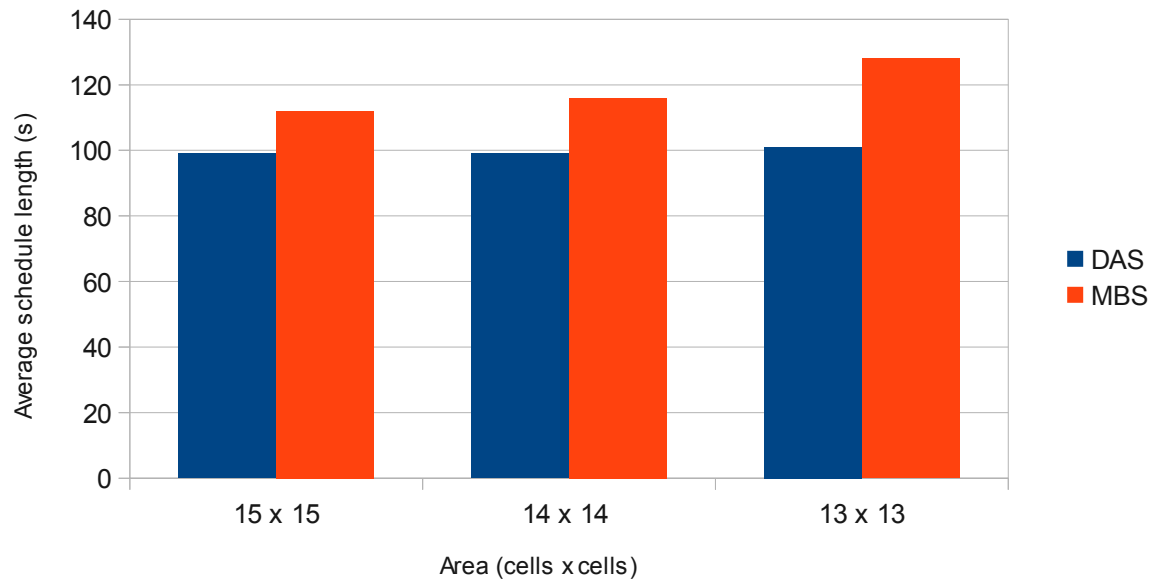
# Experimental Evaluation

- Algorithm implemented in Java
- Benchmarks
  - Real-life applications
    - In-vitro diagnosis
    - Colorimetric protein assay
  - Synthetic benchmarks
    - 3 TGFF-generated benchmarks with 20, 40, 60 operations
- Comparison between:
  - Droplet-aware module-based synthesis (DAS)
  - Module-based synthesis (MBS)

# Experimental Evaluation

Average schedule length out of 50 runs for **DAS** vs. **MBS**

Colorimetric protein assay



21.55 % improvement for 13 x 13

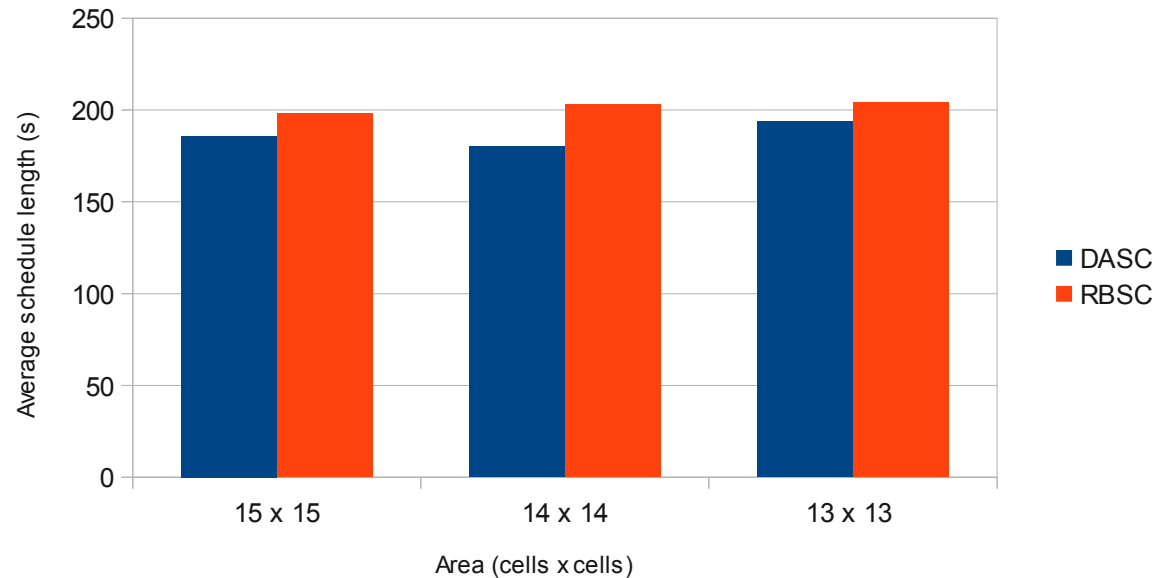
# Experimental Evaluation

- Algorithm implemented in Java
- Benchmarks
  - Real-life applications
    - Colorimetric protein assay
  - Synthetic benchmarks
    - 3 TGFF-generated benchmarks with 20, 40, 60 operations
- Comparison between:
  - Droplet-aware module-based synthesis (DASC)
  - Routing-based synthesis (RBSC)  
**with contamination avoidance**

# Experimental Evaluation

Average schedule length out of 50 runs for **DASC** vs. **RBSC**

Colorimetric protein assay



11.19 % improvement for 14 x 14



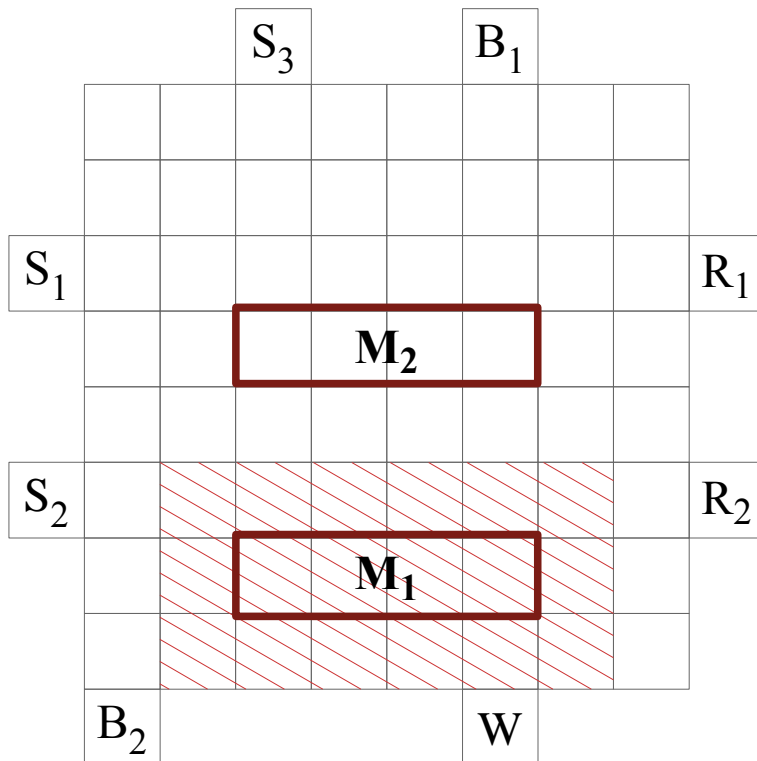
# Contributions

- Tabu Search-based algorithm for the module-based synthesis with fixed devices [CASES09]
- Module-based synthesis with virtual devices [CASES09]
- Module-based synthesis with non-rectangular virtual devices [DAEM10]
- Analytical method for operation execution characterization [CASES10]
- Routing-based synthesis [CASES10] + contamination [DAEM, submitted]
- Droplet-aware module based synthesis [JETC, submitted]
- ILP formulation for the synthesis of digital biochips [VLSI-SoC08]

# Conclusions

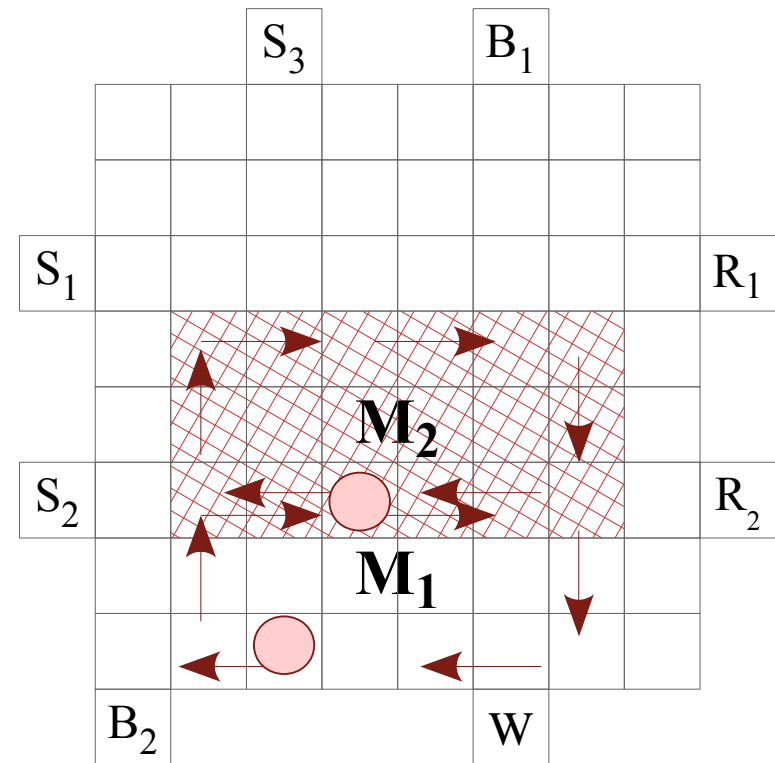
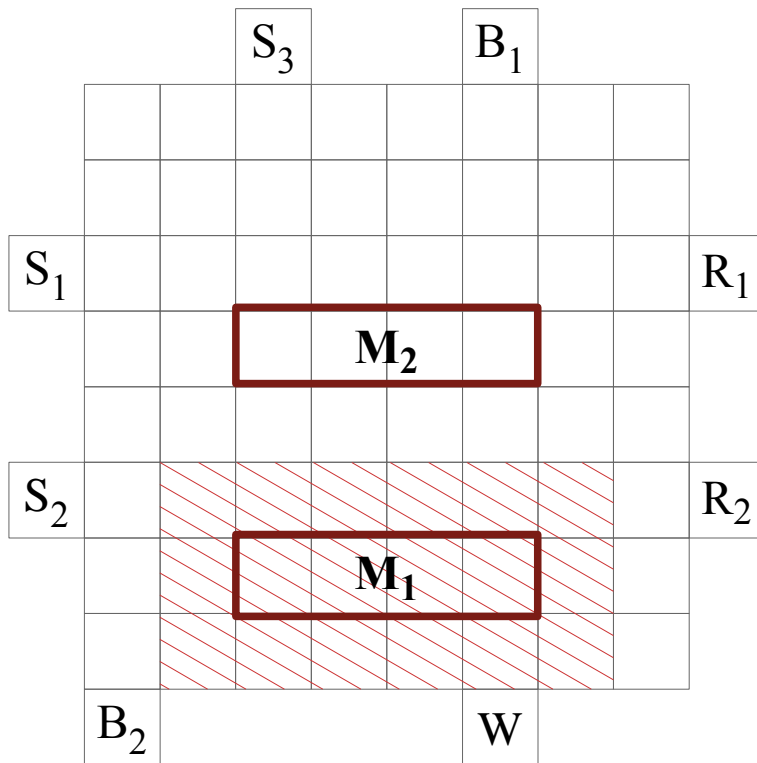
- Proposed several synthesis techniques for DMBs
- Considered the reconfigurability characteristic of DMBs
- Shown that by considering reconfigurability during operation execution improvements in the completion time of applications can be obtained

# Future Directions



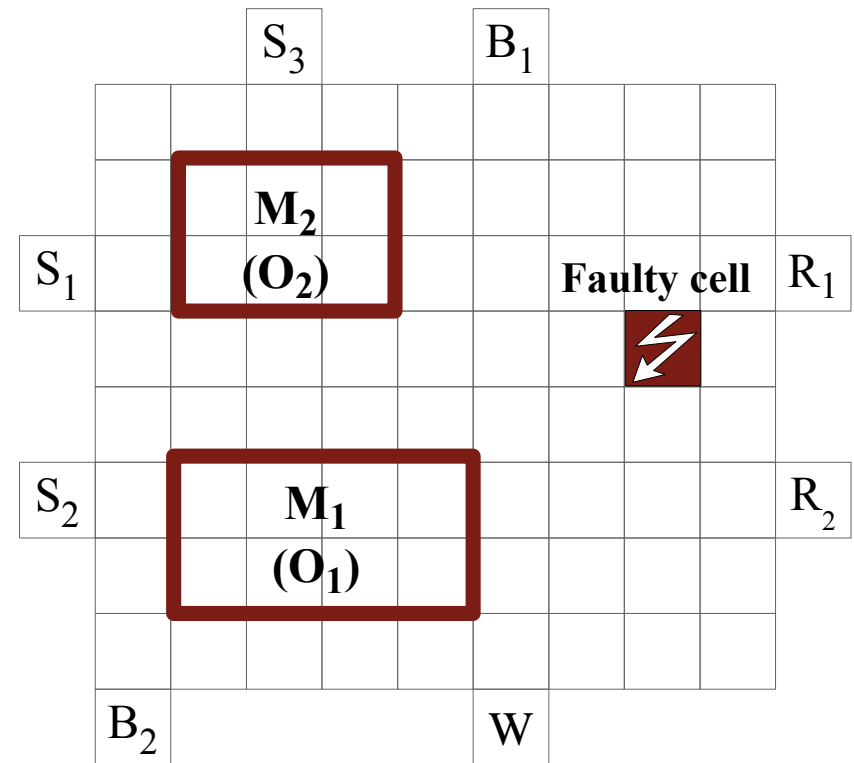
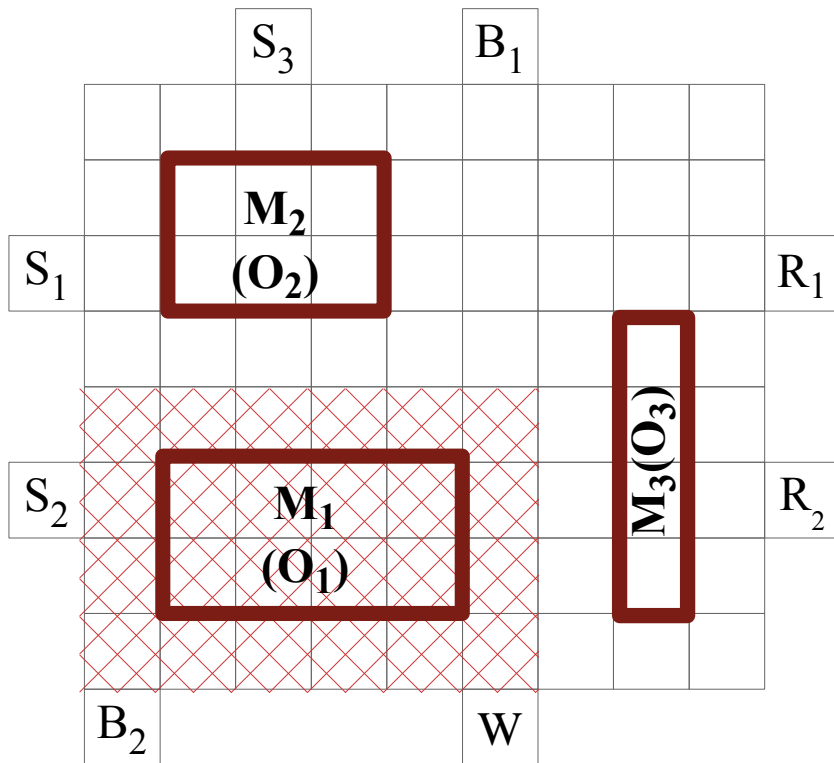
# Future Directions

## Module-Based Synthesis with Overlapping Devices



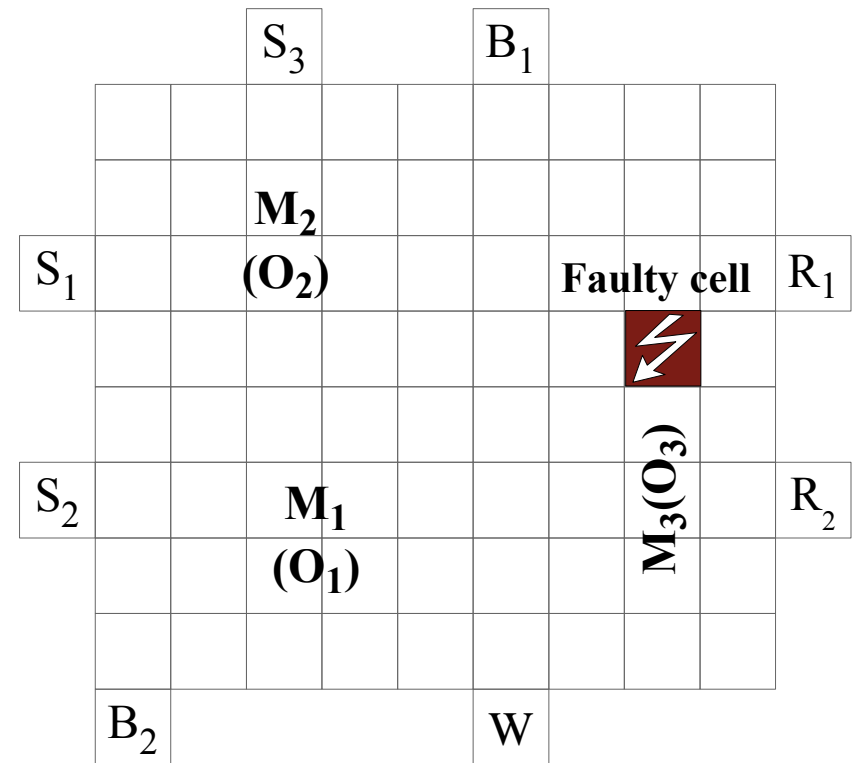
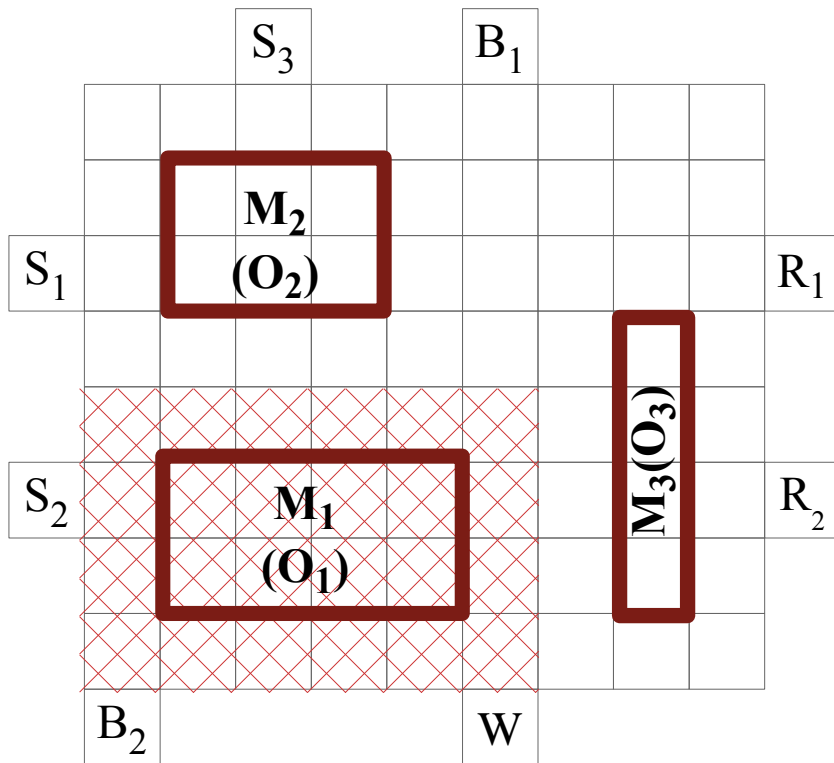
# Future Directions

## Fault-Tolerant Module-Based Synthesis



# Future Directions

## Fault-Tolerant Module-Based Synthesis

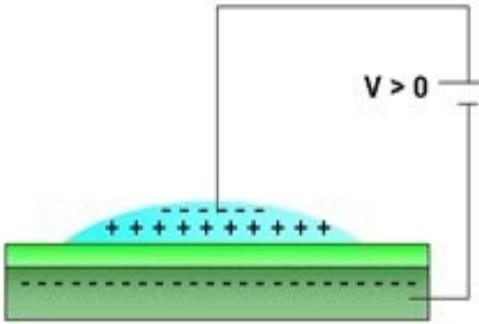
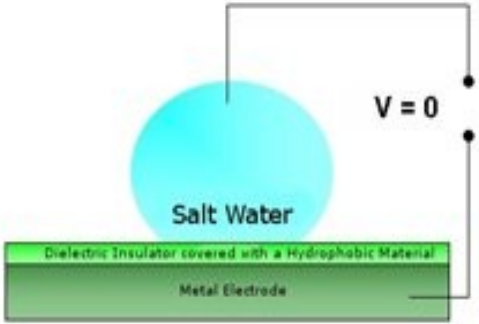
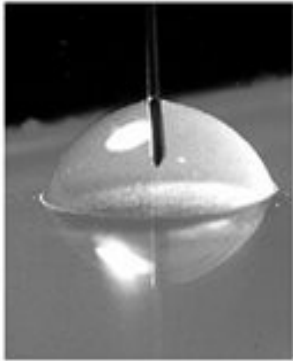




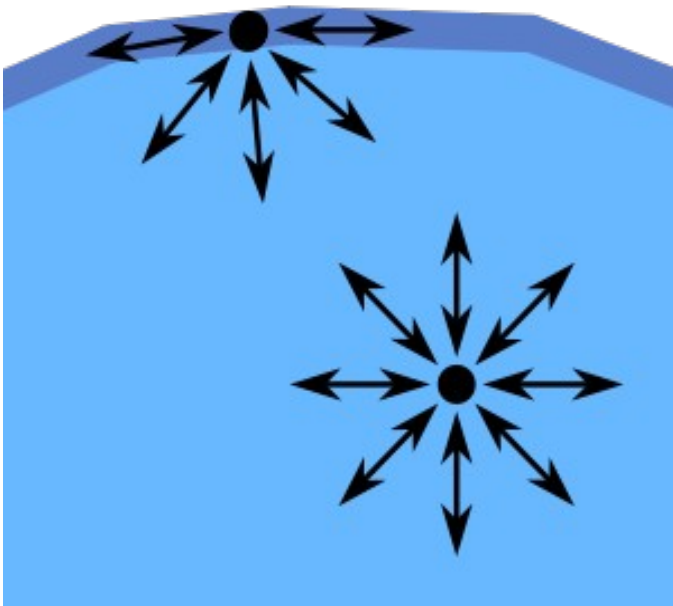
# Back-up slides



# Electrowetting

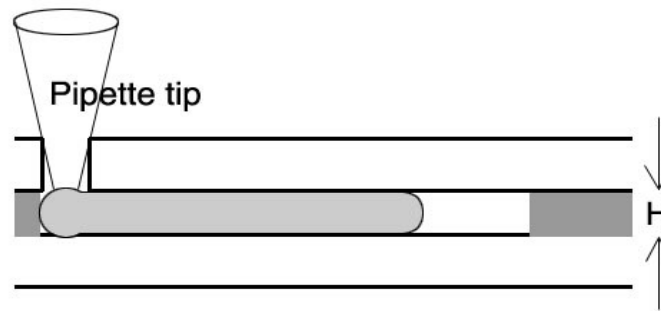
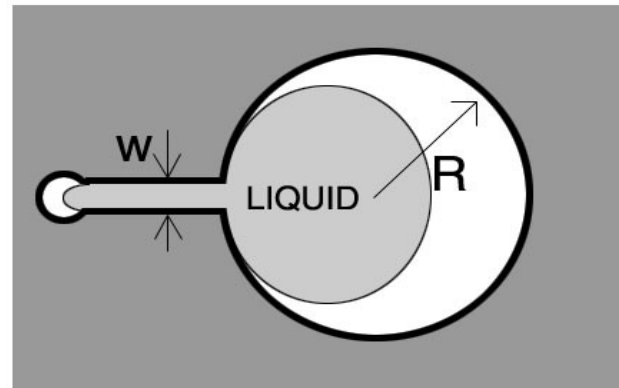


# Surface Tension

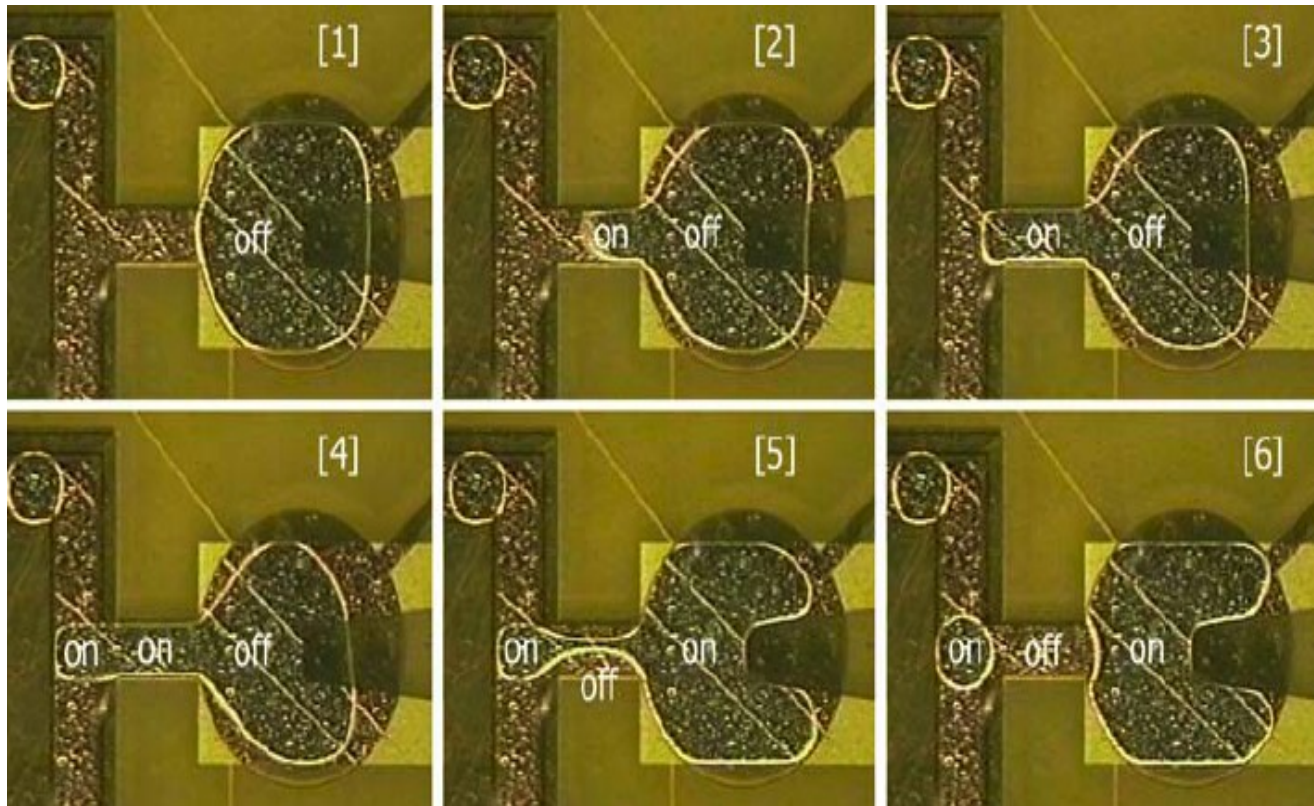


Imbalance of forces between molecules at an interface (gas/liquid, liquid/liquid, gas/solid, liquid/solid)

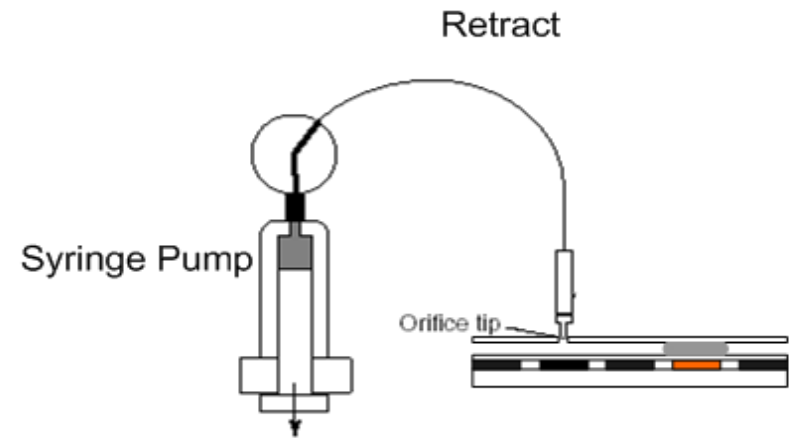
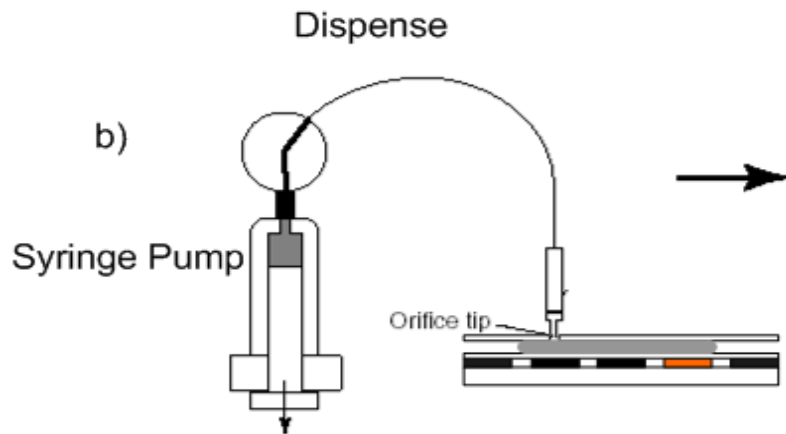
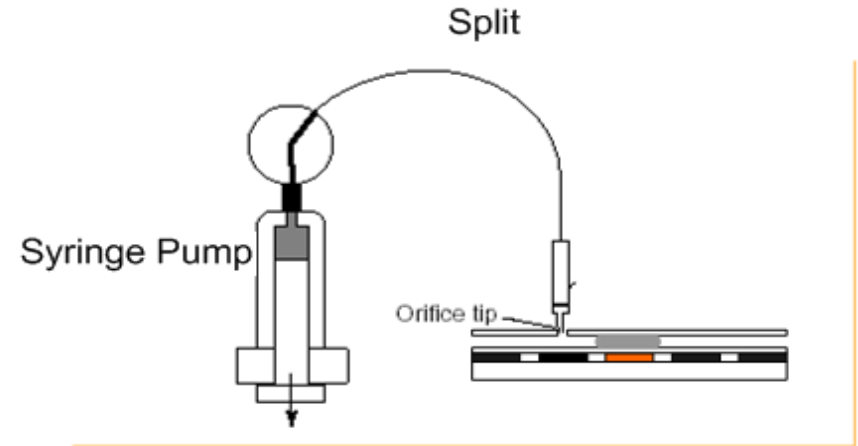
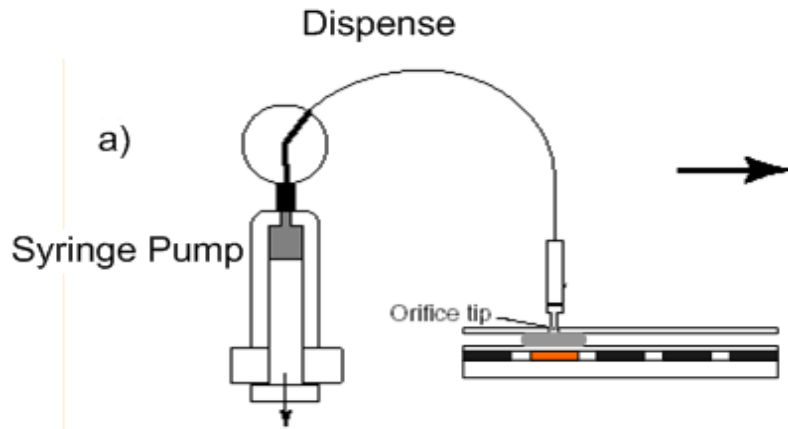
# Dispensing



# Dispensing



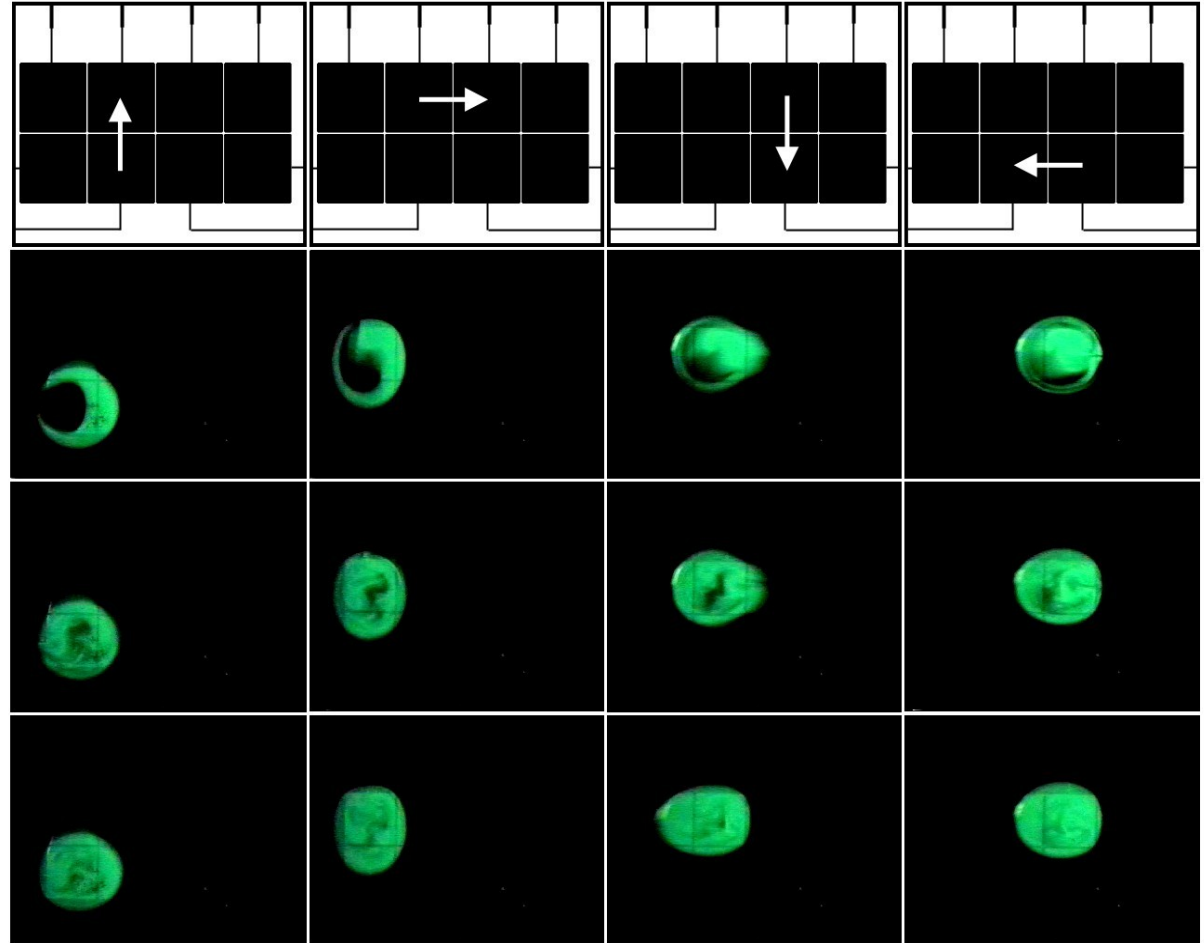
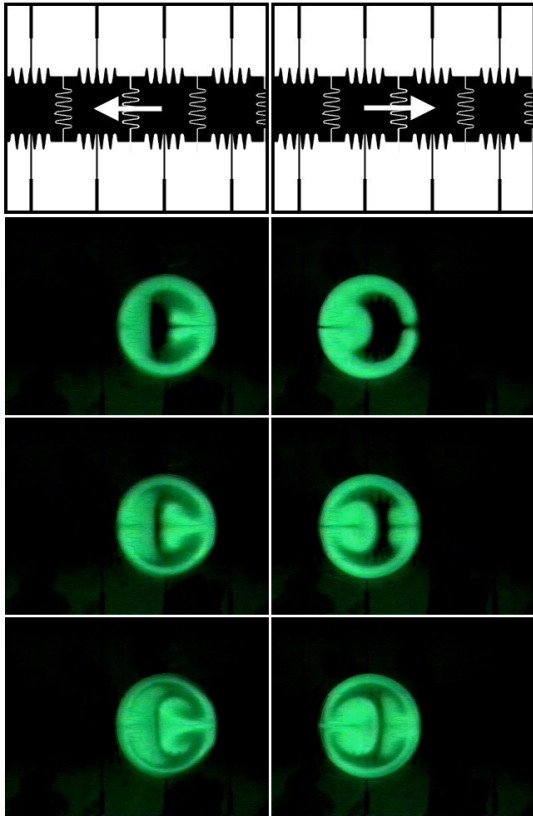
# Dispensing



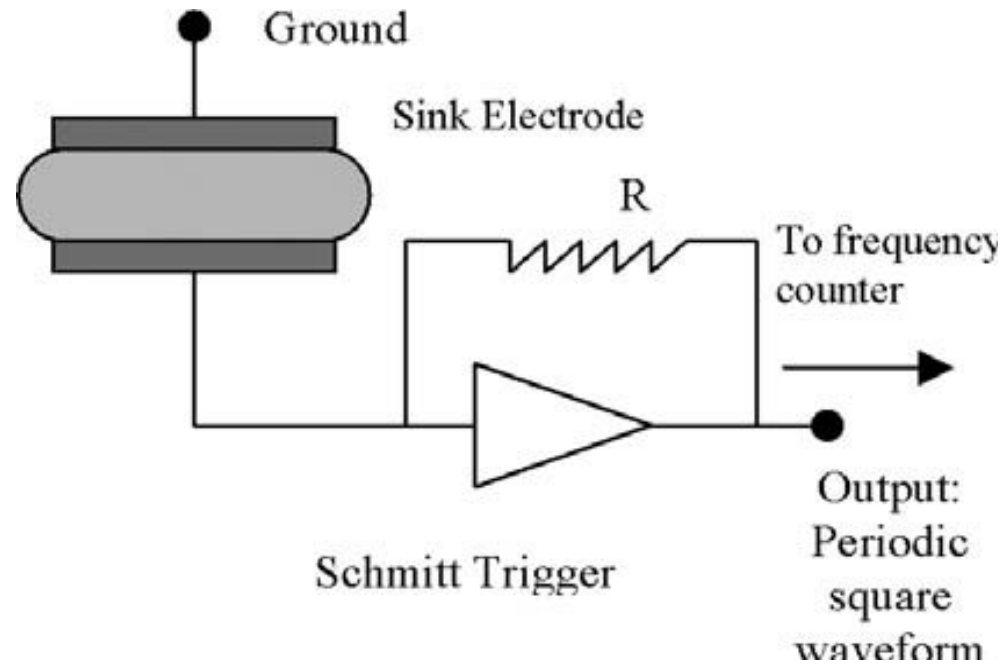
# Splitting



# Mixing

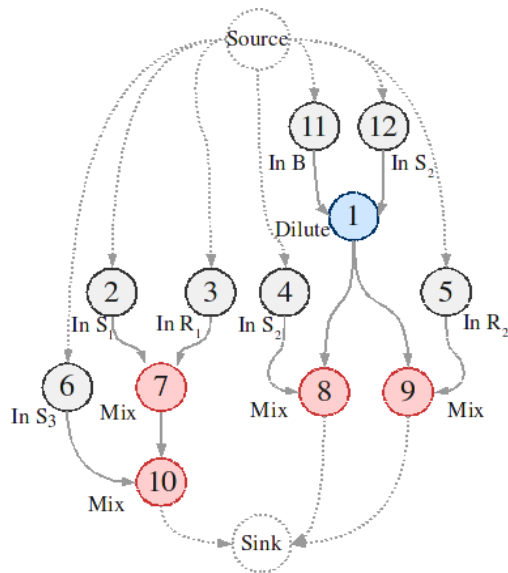


# Capacitive sensor



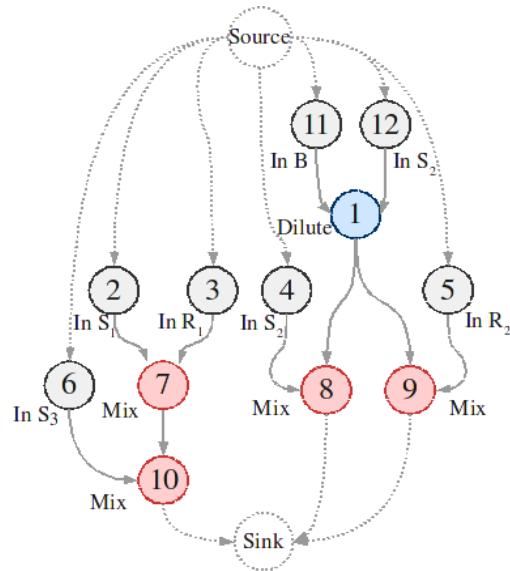


# Design Tasks

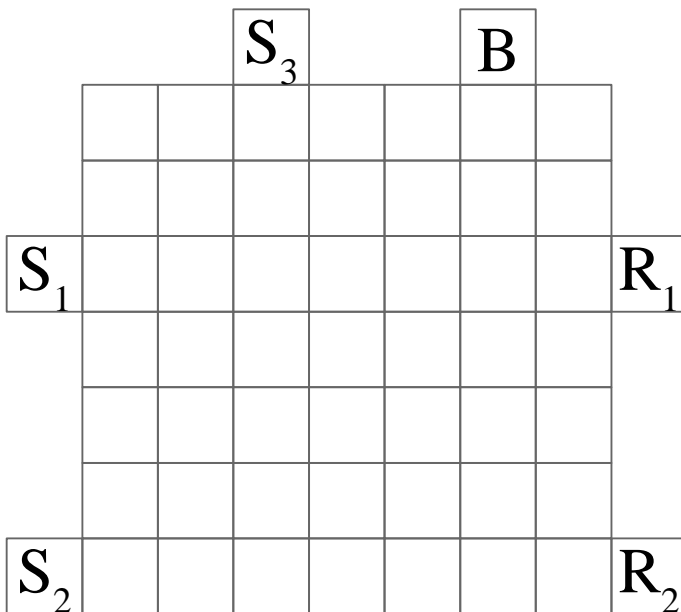


Operation	Area(cells)	Time(s)
Mix	2 x 2	10
Mix	1 x 3	5
Dilute	1 x 3	8
Dilute	2 x 5	3

# Design Tasks



Operation	Area(cells)	Time(s)
Mix	2 x 2	10
Mix	1 x 3	5
Dilute	1 x 3	8
Dilute	2 x 5	3

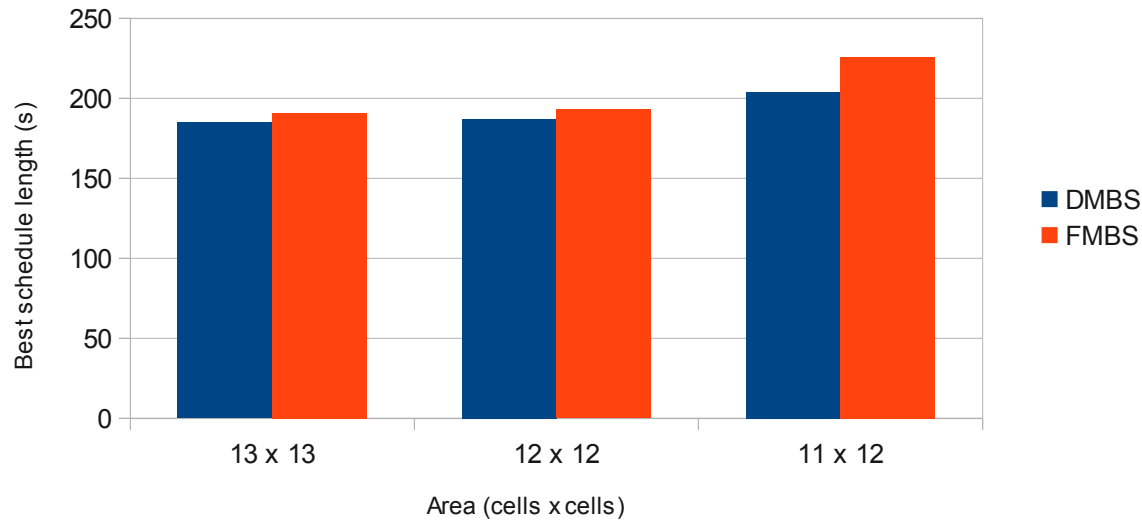


# Experimental Evaluation

Quality of the solution compared to classical operation execution  
Best out of 50

Colorimetric protein assay

DMBS vs. FMBS

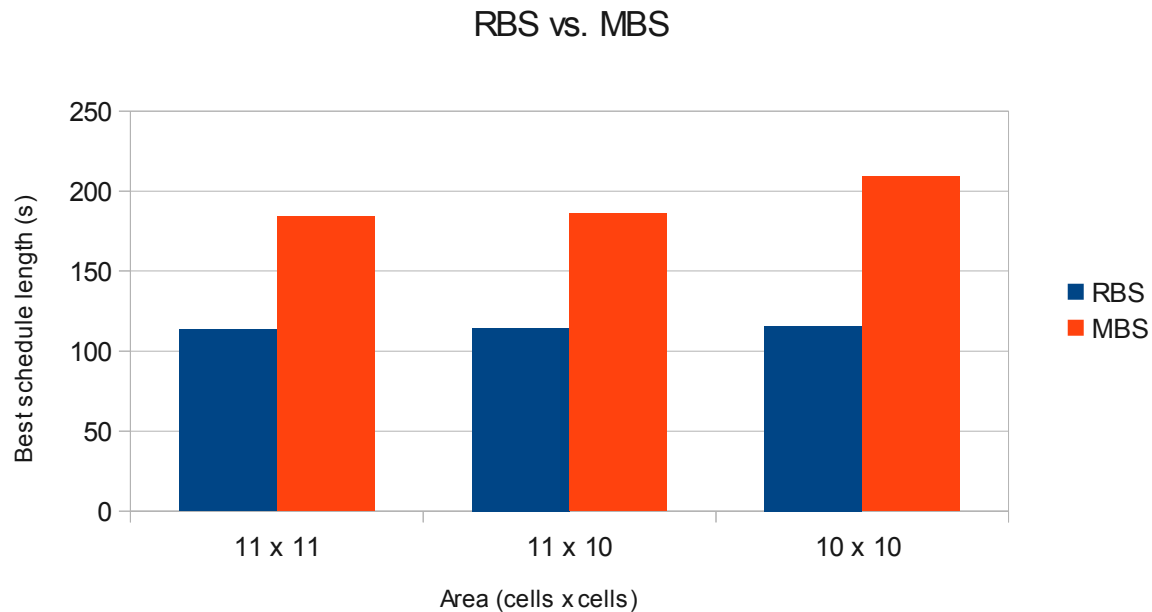


**9.73% improvement for 11 x 12**

# Experimental Evaluation

Quality of the solution compared to classical operation execution  
Best out of 50

Colorimetric protein assay



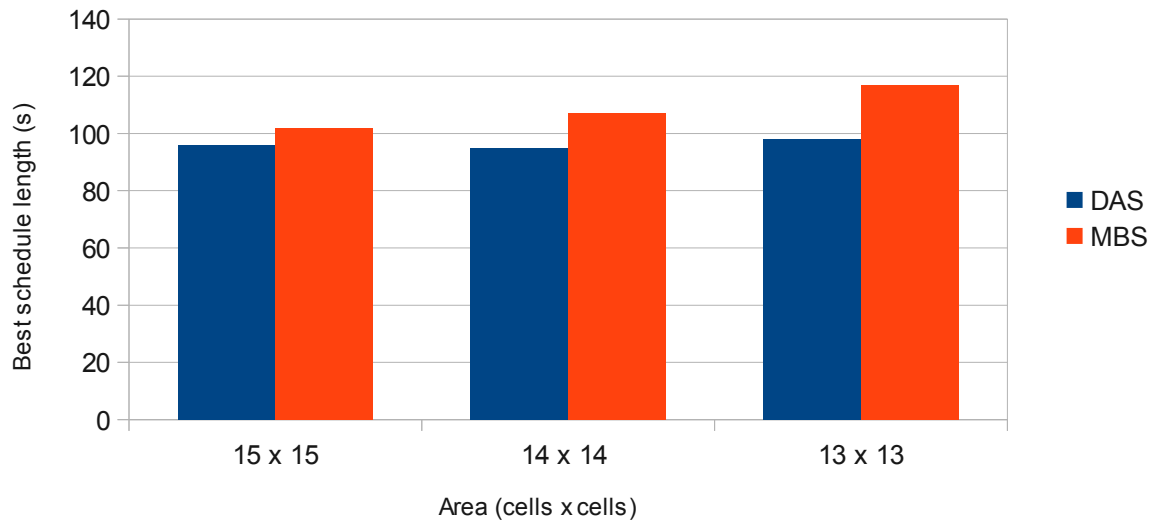
**44.63% improvement for 10 x 10**

# Experimental Evaluation

Quality of the solution compared to classical operation execution  
Best out of 50

Colorimetric protein assay

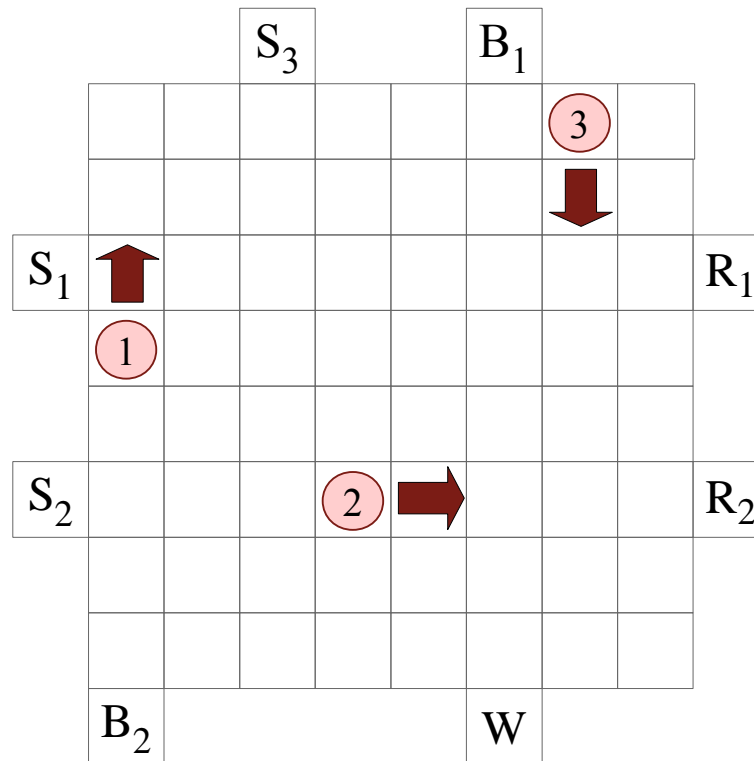
DAS vs. MBS



**15.76% improvement for 13 x 13**

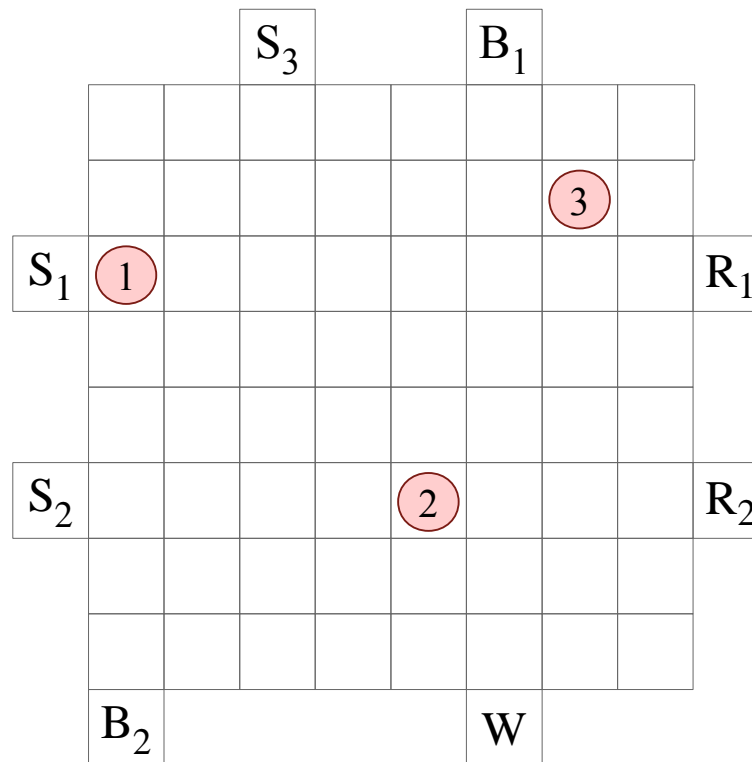
# Future Directions

## Pin-Constrained Routing-Based Synthesis



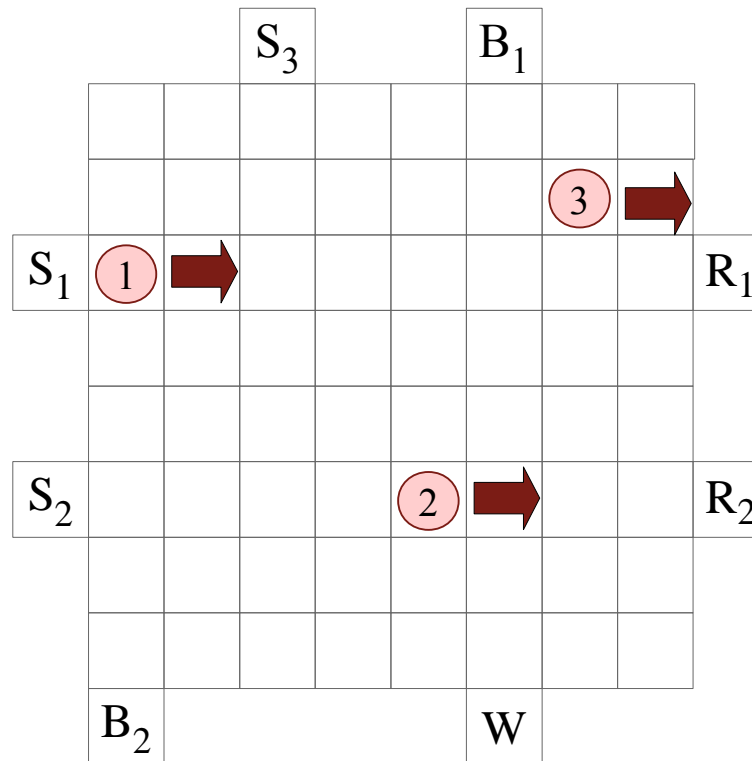
# Future Directions

## Pin-Constrained Routing-Based Synthesis



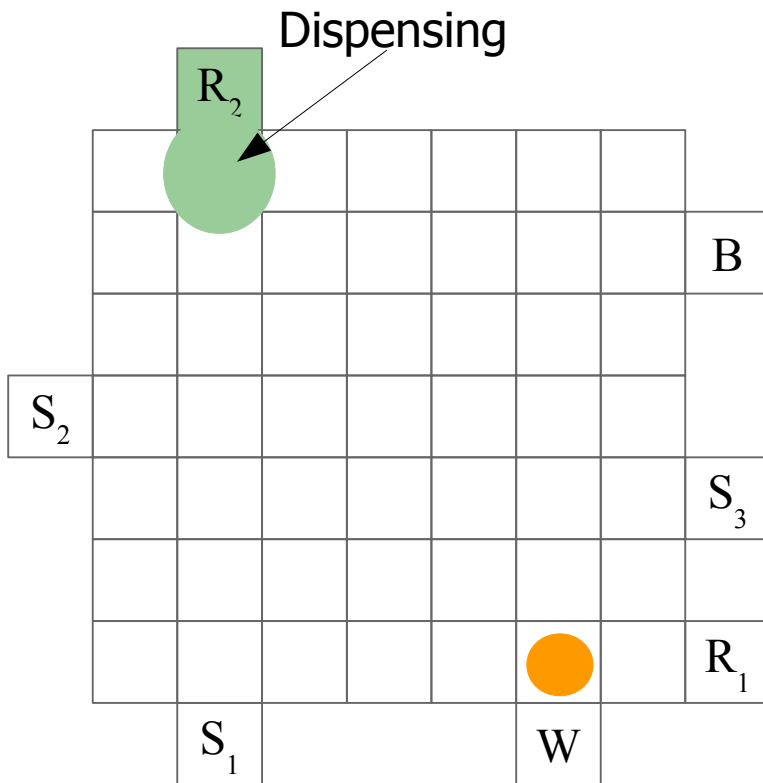
# Future Directions

## Pin-Constrained Routing-Based Synthesis



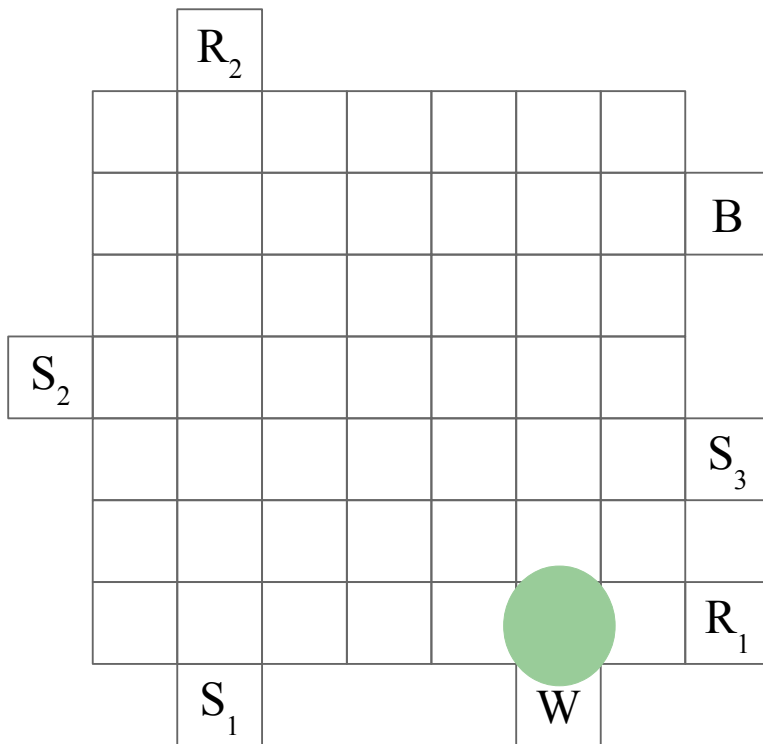


# Microfluidic Operations



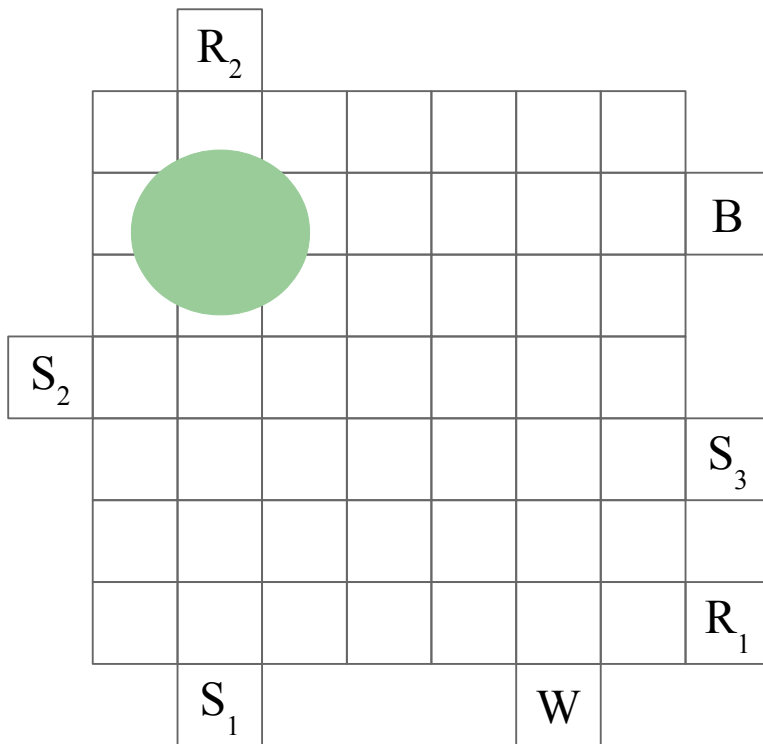
- Dispensing

# Microfluidic Operations



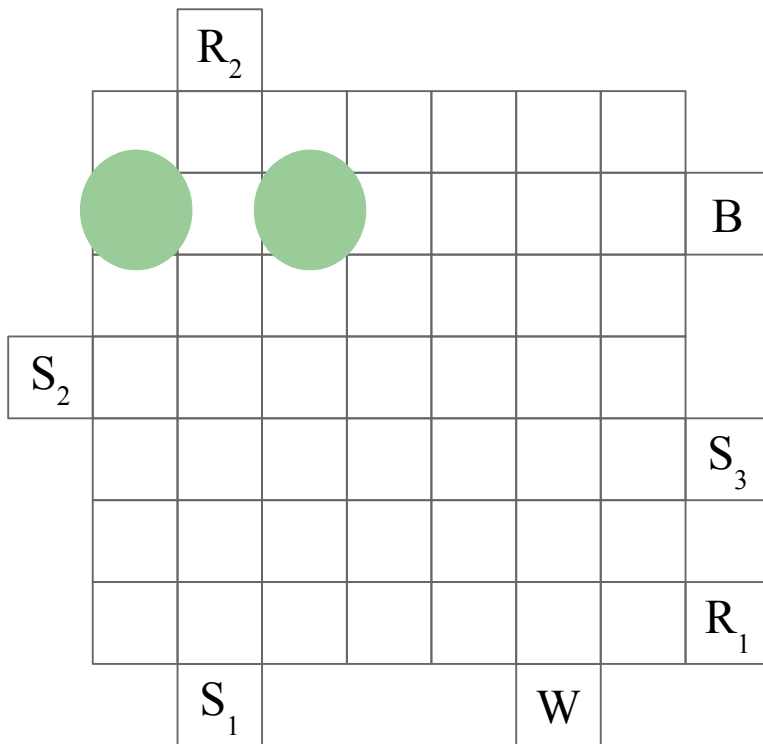
- Dispensing
- Detection

# Microfluidic Operations



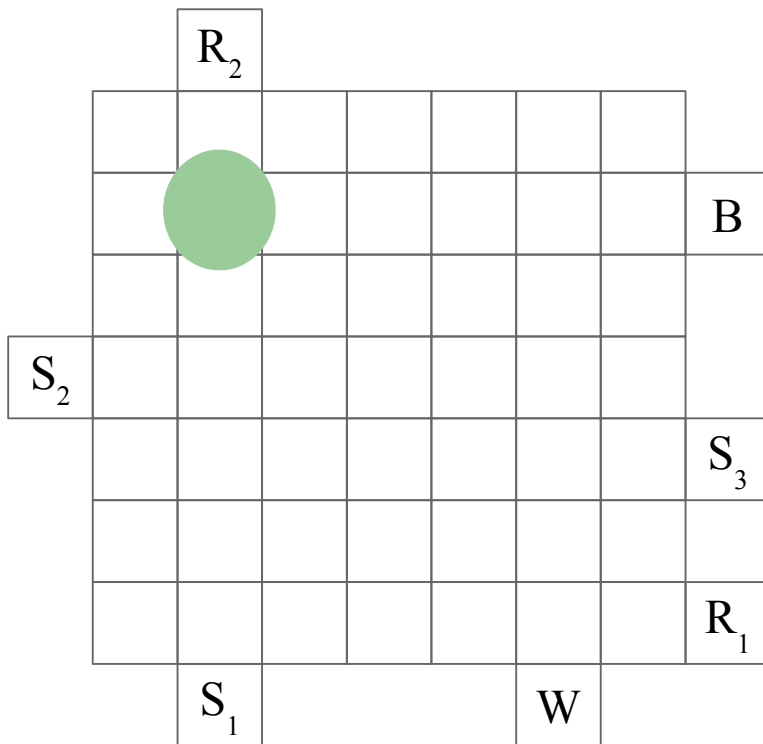
- Dispensing
- Detection
- Splitting/Merging

# Microfluidic Operations



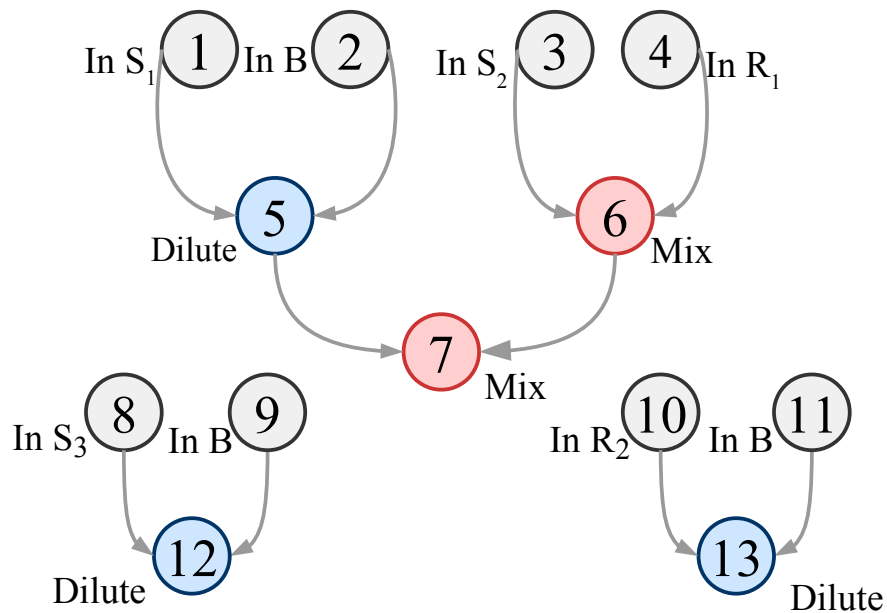
- Dispensing
- Detection
- Splitting/Merging

# Microfluidic Operations



- Dispensing
- Detection
- Splitting/Merging
- Storage

# Motivational Example (for the first contrib)

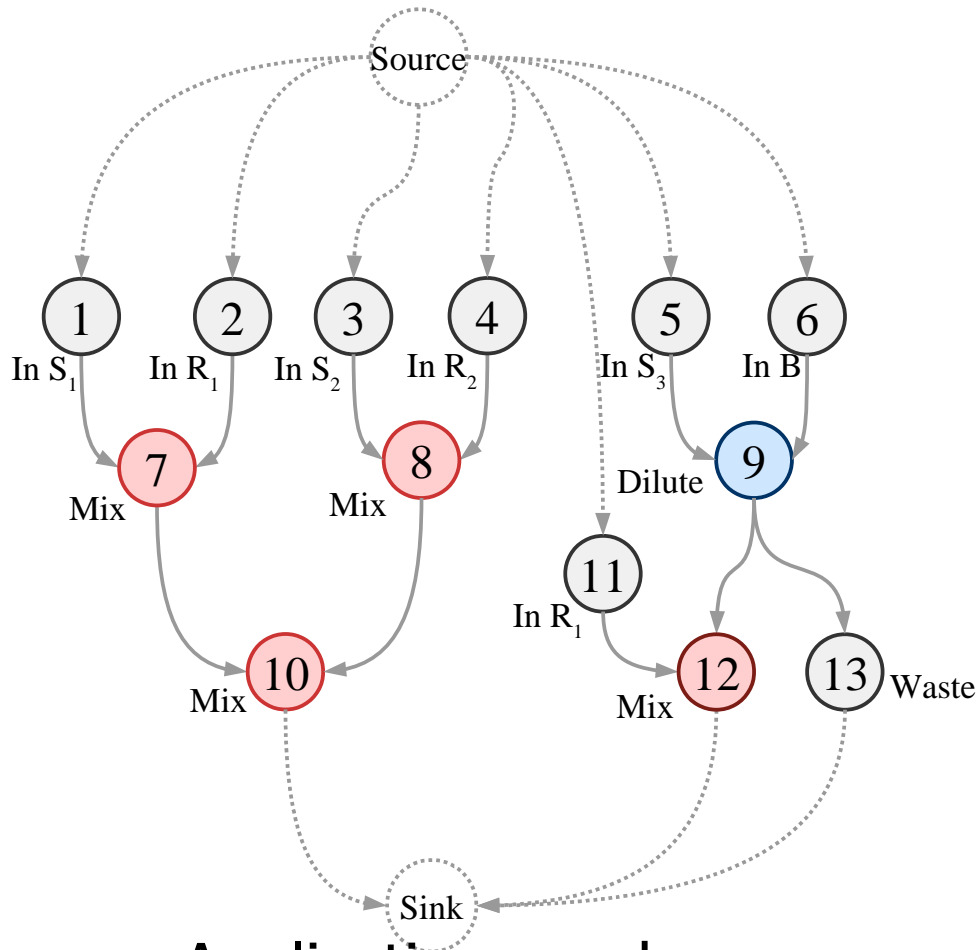


Application graph

Operation	Area(cells)	Time(s)
Mix	2 x 4	3
Mix	2 x 2	4
Dilution	2 x 4	4
Dilution	2 x 2	5
Dispense	-	2

Module library

# Motivational Example (for the 2<sup>nd</sup> contrib)

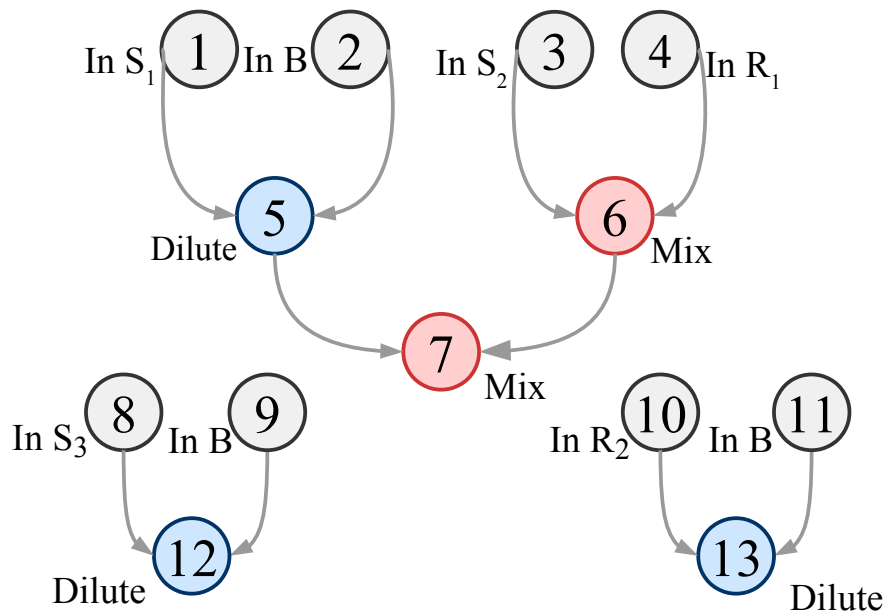


Application graph

Type	Area (cells)	Time (s)
Mix/Dlt	2 x 4	2.9
Mix/Dlt	1 x 4	4.6
Mix/Dlt	2 x 3	6.1
Mix/Dlt	2 x 2	9.9
Input	-	2
Detect	1 x 1	30

Module library

# Example(for the 3<sup>rd</sup> contrib)



Application graph

Type	Area (cells)	Time (s)
Mix/Dlt	2 x 4	2.9
Mix/Dlt	1 x 4	4.6
Mix/Dlt	2 x 3	6.1
Mix/Dlt	2 x 2	9.9
Input	-	2
Detect	1 x 1	30

Module library