

3. Lecture 3: Domain Descriptions — Endurants

3.1. What is a Part?

- By a **part** we mean an observable manifest endurant.

3.1.1. Classes of “Same Kind” Parts

- We repeat:
 - ◇ the **domain describer** does not describe instances of parts,
 - ◇ but seeks to describe classes of parts of the same kind.
- Instead of the term ‘same kind’ we shall use either the terms
 - ◇ **part sort** or
 - ◇ **part type**.
- By a **same kind class of parts**, that is a **part sort** or **part type** we shall mean
 - ◇ a class all of whose members, i.e., **parts**,
 - ◇ enjoy “exactly” the same **properties**
 - ◇ where a **property** is expressed as a **proposition**.

Example: 18 Part Properties.

- Examples of part properties are:
 - ◇ *has unique identity,*
 - ◇ *has mereology,*
 - ◇ *has length,*
 - ◇ *has location,*
 - ◇ *has traffic movement restriction,*
 - ◇ *has position,*
 - ◇ *has velocity* and
 - ◇ *has acceleration.*



3.1.2. Concept Analysis as a Basis for Part Typing

- The domain analyser examines collections of **parts**.
 - ⊠ In doing so the **domain analyser** discovers and thus identifies and lists a number of **properties**.
 - ⊠ Each of the **parts** examined usually satisfies only a subset of these properties.
 - ⊠ The **domain analyser** now groups **parts** into collections
 - ⊗ such that each collection have its **parts** satisfy the same set of **properties**,
 - ⊗ such that no two distinct collections are indexed, as it were, by the same set of **properties**, and
 - ⊗ such that all **parts** are put in some collection.
 - ⊠ The **domain analyser** now
 - ⊗ assigns distinct **type names** (same as **sort names**)
 - ⊗ to distinct collections.
- That is how we assign **types** to **parts**.
- We shall return later to a proper treatment of **formal concept analysis** [Wille:ConceptualAnalysis1999].

3.2. Atomic and Composite Parts

- Parts may be analysed into disjoint sets of
 - ◇ atomic parts and
 - ◇ composite parts.
- **Atomic parts** are those which,
 - ◇ in a given context,
 - ◇ are deemed *not* to consist of meaningful, separately observable proper **sub-parts**.
- **Composite parts** are those which,
 - ◇ in a given context,
 - ◇ are deemed to *indeed* consist of meaningful, separately observable proper **sub-parts**.
- A **sub-part** is a **part**.

Example: 19 Atomic and/or Composite Parts. To one person a part may be atomic; to another person the same part may be composite.

- It is the domain describer who decides the outcome of this aspect of domain analysis.
 - ⊗ In some domain analysis a ‘person’ may be considered an atomic part.
 - ⊗ For the domain of ferrying cars with passengers
 - ⊗ persons are considered parts.
 - ⊗ In some other domain analysis a ‘person’ may be considered a composite part.
 - ⊗ For the domain of medical surgery
 - ⊗ persons may be considered composite parts. ■

Example: 20 Container Lines.

- We shall presently consider **containers** (as used in container line shipping) to be atomic parts.
- And we shall consider a **container vessel** to be a composite part consisting of
 - ❖ an **indexed set of container bays**
 - ❖ where each container bay consists of **indexed set of container rows**
 - ❖ where each container row consists of **indexed set of container stacks**
 - ❖ where each container stack consists of a **linearly indexed sequence of containers**.
- Thus container vessels, container bays, container rows and container stacks are composite parts. ■

3.2.1. Atomic Parts

- When we observe
 - ❖ what we have decided, i.e., analysed, to be an endurant,
 - ❖ more specifically an **atomic part**, of a domain,
 - ❖ we are observing an **instance** of an atomic part.
- When we describe those instances
 - ❖ we describe, not their **values**, i.e., the instances,
 - ❖ but their
 - ⊗ **type** and
 - ⊗ **properties**.

- In this section on **endurant entities** we shall unfold what these properties might be.
- But, for now, we focus on the **type** of the observed **atomic part**.
- So the situation is that we are observing a number of atomic parts
 - ❖ and we have furthermore decided that
 - ❖ they are all of “*the same kind*”.

- What does it mean for a number of atomic parts to be of “*the same kind*” ?

- ◊ It means

- ⊗ that we have decided,
- ⊗ for any pair of **parts** considered of the same kind,
- ⊗ that the kinds of properties,
 - * for such two **parts**,
- ⊗ are “*the same*”,
 - * that is, of the same **type**, but possibly of different **values**,
- ⊗ and that a number of different, other “facets”,
- ⊗ are not taken into consideration.

- That is,
 - ❖ we **abstract** a collection of atomic parts
 - ❖ to be of the same kind,
 - ❖ thereby “dividing the domain of endurants” into possibly two distinct sets
 - ⊗ those that are of the analysed kind, and
 - ⊗ those that are not.

- It is now our description choice to associate with a set of **atomic parts** of “*the same kind*”
 - ⊠ a **part type** (by suggesting a name for that **type**, for example, **T**) and
 - ⊠ a set of **properties** (of its values):
 - ⊗ unique identifier,
 - ⊗ mereology and
 - ⊗ attributes.

- Later we shall introduce **discrete perdurants** (actions, events and behaviours) whose **signatures** involves (possibly amongst others) type **T**.
- Now we can characterise “*of the same kind*” atomic part facets⁹
 - ❖ being of the same, named **part type**,
 - ❖ having the same **unique identifier type**,
 - ❖ having the same **mereology** (but not necessarily the same **mereology values**), and
 - ❖ having the same set of **attributes** (but not necessarily of the same **attribute values**),
- The “*same kind*” criteria apply equally well to **composite part facets**.

⁹as well as “*of the same kind*” composite part facets.

Example: 21 Transport Nets: Atomic Parts (I).

- The types of atomic transportation net parts are:
 - ◇ hubs, say of type **H**, and
 - ◇ links, say of type **L**.
- The chosen mereology associates with every hub and link a
 - ◇ distinct unique identifiers
 - ◇ (of types **HI** and **LI** respectively), and, *vice versa*,
 - ◇ how hubs and links are connected:
 - ⊗ hubs to any number of links and
 - ⊗ links to exactly two distinct hubs.

- The chosen attributes of

- ◆ hubs include

- ⊗ hub location,
 - ⊗ hub design¹⁰,

- ⊗ hub traffic state¹¹,
 - ⊗ hub traffic state space¹², etc.;

- ◆ and of links include

- ⊗ link location,
 - ⊗ link length,

- ⊗ link traffic state¹³,
 - ⊗ link traffic state space¹⁴, etc.

- With these mereologies and attributes we see that we can consider hubs and links as different kinds of atomic parts. ■

¹⁰Design: simple crossing, freeway “cloverleaf” interchange, etc.

¹¹A hub traffic state is (for example) a set of pairs of link identifiers where each such pair designates that traffic can move from the first designated link to the second.

¹²A hub state space is (for example) the set of all hub traffic states that a hub may range over.

¹³A link traffic state is (for example) a set of zero to two distinct pairs of the hub identifiers of the link mereology.

¹⁴A link traffic state space is (for example) the set of all link traffic states that a link may range over.

Observers for Atomic Parts

- Let the domain describer decide
 - ◇ that a **type**, **A** (or Δ), is **atomic**,
 - ◇ hence that it does not consists of sub-parts.
- Hence there are no **observer** to be associated with **A** (or Δ).

3.2.2. Composite Parts

- The domain describer has chosen to consider
 - ❖ a part (i.e., a **part type**)
 - ❖ to be a composite part (i.e., a **composite part type**).
- Now the domain describer has to analyse the types of the sub-parts of the composite part.
 - ❖ There may be just one “*kind of*” sub-part of a composite part¹⁵,
 - ❖ or there may be more than one “*kind of*”¹⁶.
- For each such **sub-part type**
 - ❖ the domain describer decides on
 - ❖ an appropriate, distinct **type name** and
 - ❖ a **sub-part observer** (i.e., a function signature).

¹⁵that is, only one sub-part type

¹⁶that is, more than one sub-part type

Example: 22 Container Vessels: Composite Parts. We bring pairs of informal, narrative description texts and formalisations.

- For a container vessel, say of type V , we have

⋄ *Narrative:*

- ⊗ A container vessel, $v:V$, consists of container bays, $bs:BS$.
- ⊗ A container bay, $b:B$, consists of container rows, $rs:RS$.
- ⊗ A container row, $r:R$, consists of container stacks, $ss:SS$.
- ⊗ A container stack, $s:S$, consists of a linearly indexed sequence of containers.

⋄ *Formalisation:*

type V,BS , value $obs_BS: V \rightarrow BS$,
type B,RS , value $obs_RS: B \rightarrow RS$,
type R,SS , value $obs_CS: R \rightarrow SS$,
type SS,S , value $obs_S: SS \rightarrow S$,
type $S = C^*$.



3.2.3. Abstract Types, Sorts, and Concrete Types

- By an **abstract type**, or a **sort**, we shall understand a type
 - ❖ which has been given a name
 - ❖ but is otherwise undefined, that is,
 - ⊙ is a space of undefined mathematical quantities,
 - * where these are given properties
 - * which we may express in terms of **axioms** over sort (including **property**) values.

- By a **concrete type** we shall understand a type, T ,
 - ◇ which has been given both a name
 - ◇ and a defining type expression of, for example the form

<ul style="list-style-type: none"> ⊗ $T = \mathbf{A\text{-set}}$, ⊗ $T = \mathbf{A\text{-infset}}$, ⊗ $T = \mathbf{A \times B \times \dots \times C}$, 	<ul style="list-style-type: none"> ⊗ $T = \mathbf{A^*}$, ⊗ $T = \mathbf{A^\omega}$, ⊗ $T = \mathbf{A \xrightarrow{m} B}$, 	<ul style="list-style-type: none"> ⊗ $T = \mathbf{A \rightarrow B}$, ⊗ $T = \mathbf{A \xrightarrow{\sim} B}$, or ⊗ $T = \mathbf{A B \dots C}$.
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 - ◇ where A, B, \dots, C are type names or type expressions.

Example: 23 Container Bays. We continue Example 22 on Slide 153.

```
type Bs = Bld  $\overrightarrow{m}$  B,  
value obs_Bs: BS  $\rightarrow$  Bs,
```

```
type Rs = Rld  $\overrightarrow{m}$  R,  
value obs_Rs: B  $\rightarrow$  Rs,
```

```
type Ss = Sld  $\overrightarrow{m}$  S,  
value obs_Ss: R  $\rightarrow$  Ss,
```

```
type S = C*.
```



Observers for Composite Parts I/II

- Let the domain describer decide
 - ◇ that a type, A (or Δ), is composite
 - ◇ and that it consists of sub-parts of types B, C, \dots, D .
- We can initially consider these types B, C, \dots, D , as **abstract types**, or **sorts**, as we shall mostly call them.
- That means that there are the following formalisations:
 - ◇ **type** A, B, C, \dots, D ;
 - ◇ **value** $\text{obs}_B: A \rightarrow B, \text{obs}_C: A \rightarrow C, \dots, \text{obs}_D: A \rightarrow D$.

Observers for Composite Parts II/II

- We can also consider the types B , C , \dots , D , as concrete types,
 - ◇ **type** $B_c = \text{TypBex}$, $C_c = \text{TypCex}$, \dots , $D_c = \text{TypDex}$;
 - ◇ **value** $\text{obs_Bc}: B \rightarrow B_c$, $\text{obs_Cc}: C \rightarrow C_c$, \dots , $\text{obs_Dc}: D \rightarrow D_c$,
 - ◇ where TypBex , TypCex , \dots , TypDex are type expressions as, for example, hinted at above.
- The prefix obs_ distinguishes part observers
 - ◇ from mereology observers (uid_ , mereo_) and
 - ◇ attribute observers (attr_).

3.3. Properties

- Endurants have **properties**.
 - ❖ Properties are
 - ⊗ what makes up a parts (and materials) and,
 - ⊗ with **property values** distinguishes one part from another part and one material from another material.
 - ❖ We name properties.
 - ⊗ **Properties** of **parts** and **materials** can be given distinct names.
 - ⊗ We let these names also be the **property type name**.
 - ⊗ Hence two parts (materials) of the same **part type** (**material type**) have the same set of **property type names**.

- **Properties** are all that distinguishes **parts** (and **materials**).
 - ❖ The **part types** (**material types**)
in themselves do not express properties.
 - ❖ They express a class of parts (respectively materials).
 - ❖ All parts (materials) of the same type
 - ❖ have the same **property types**.
 - ❖ **Parts** (**materials**) of the different **types**
have different sets of **property types**,

- For pragmatic reasons we distinguish between three kinds of properties:
 - ◇ unique identifiers, ◇ mereology, and ◇ attributes.
- If you “remove” a property from a part
 - ◇ it “looses” its (former) part type,
 - ◇ to, in a sense, attain another part type:
 - ⊗ perhaps of another, existing one,
 - ⊗ or a new “created” one.
- *But we do not know* how to model *removal of a property* from an endurant value!¹⁷

¹⁷And we see no need for describing such type-changes. Crude oil does not “morph” into fuel oil, diesel oil, kerosene and petroleum. Crude oil is consumed and the fractions result from distillation, for example, in an oil refinery.

Example: 24 Atomic Part Property Kinds.

- We distinguish between two kinds of persons:
 - ⋄ ‘living persons’ and ‘deceased persons’;
 - ⋄ they could be modelled by two different **part types**:
 - ⊗ **LP**: living person, with a set of properties,
 - ⊗ **DP**: deceased person, with a, most likely, different set of properties.
- All persons have been born, hence have a birth date (**static attributes**).
- Only deceased persons have a (well-defined) death date.

- All persons also have height and weight profiles (i.e., with dated values, i.e., **dynamic attributes**).
- One can always associate a **unique identifier** with each person.
- Persons are related, family-wise:
 - ❖ have parents (living or deceased),
 - ❖ (up to four known) grandparents, etc.,
 - ❖ may have brothers and sisters (zero or more),
 - ❖ may have children (zero or more), etc.
 - ❖ These family-relations can be considered the **mereology** for living persons. ■

3.3.1. Unique Identification

- We can assume that all parts
 - ❖ of the same part type
 - ❖ can be uniquely distinguished,
 - ❖ hence can be given unique identifications.

Unique Identification

- With every **part**, whether **atomic** or **composite** we shall associate a **unique part identifier**, of just **unique identifier**.
- Thus we shall associate with **part type** T
 - ◇ the **unique part type identifier type** TI ,
 - ◇ and a **unique part identifier observer function**, $uid_TI: T \rightarrow TI$.
- These associations (TI and uid_TI) are, however,
 - ◇ usually expressed explicitly,
 - ◇ whether they are (“subsequently”) needed!

- The **unique identifier** of a part
 - ⊠ can not be changed;
 - ⊠ hence we can say that
 - ⊗ no matter what a given **part's property values** may take on,
 - ⊗ that **part** cannot be confused with any other part.
- Since we can talk about this concept of **unique identification**,
 - ⊠ we can **abstractly** describe it —
 - ⊗ and do not have to bother about any representation,
 - ⊗ that is, whether we can humanly observe **unique identifiers**.

3.3.2. Mereology

- Mereology [CasatiVarzi1999]¹⁸ (from the Greek *μερος* ‘part’) is
 - ◇ *the theory of part-hood relations:*
 - ◇ *of the relations of part to whole and*
 - ◇ *the relations of part to part within a whole.*

¹⁸Achille Varzi: Mereology, <http://plato.stanford.edu/entries/mereology/>

- For pragmatic reasons we choose to model the mereology of a domain in either of two ways
 - ❖ either by defining a **concrete type** as a model of the composite type,
 - ❖ or by endowing the sub-parts of the composite part with structures of **unique part identifiers**.

or by suitable combinations of these.

Example: 25 Container Bays, Etcetera: Mereology. First we show how to model indexed set of container bays, rows and stacks for the previous example.

- *Narrative:*

- ❖ (i) An indexed set, $bs:BS$, of bays is a bijective map from unique bay identifiers, $bid:Bid$, to bays, $b:B$.
- ❖ (ii) An indexed set, $rs:RS$, of rows is a bijective map from unique row identifiers, $rid:Rid$, to rows, $r:R$.
- ❖ (iii) An indexed set, $ss:SS$, of stacks is a bijective map from unique stack identifiers, $sid:Sid$, to stacks, $s:S$.
- ❖ (iv) A stack is a linear indexed sequence of containers, $c:C$.

- *Formalisation:*

- ◇ (i) **type** BS, B, BId,
 $Bs = BId \xrightarrow{m} B$,
value obs_Bs: BS \rightarrow Bs
(or obs_Bs: BS \rightarrow (BId \xrightarrow{m} B));
- ◇ (ii) **type** RS, R, RId,
 $Rs = RId \xrightarrow{m} R$,
value obs_Rs: RS \rightarrow Rs
(or obs_Rs: RS \rightarrow (RId \xrightarrow{m} R));
- ◇ (iii) **type** SS, S, SId,
 $Ss = SId \xrightarrow{m} S$;
- ◇ (iv) **type** C,
 $S = C^*$.



Example: 26 Transport Nets: Mereology.

- We show how to model a mereology
 - ◇ for a transport net of links and hubs.
- *Narrative:*
 - (i) Hubs and links are endowed with unique hub, respectively link identifiers.
 - (ii) Each hub is furthermore endowed with a hub mereology which lists the unique link identifiers of all the links attached to the hub.
 - (iii) Each link is furthermore endowed with a link mereology which lists the set of the two unique hub identifiers of the hubs attached to the link.
 - (iv) Link identifiers of hubs and hub identifiers of links must designate hubs, respectively links of the net.

- *Formalisation:*

(i) **type** H, HI, L, LI ;

value

(ii) $uid_HI:H \rightarrow HI$, $uid_LI:L \rightarrow LI$,

$mereo_H:H \rightarrow LI\text{-set}$, $mereo_L:L \rightarrow HI\text{-set}$,

axiom

(iii) $\forall l:L \cdot \mathbf{card} \text{ mereo_L}(l) = 2$

(iv) $\forall n:N, l:L, h:H \cdot l \in \text{obs_Ls}(\text{obs_LS}(n)) \wedge h \in \text{obs_Hs}(\text{obs_HS}(n))$

$\forall hi:HI \cdot hi \in \text{mereo_L}(l) \Rightarrow$

$\exists h':H \cdot h' \in \text{obs_Hs}(\text{obs_HS}(n)) \wedge uid_HI(h)=hi$

$\wedge \forall li:LI \cdot li \in \text{mereo_H}(h) \Rightarrow$

$\exists l':L \cdot l' \in \text{obs_Ls}(\text{obs_LS}(n)) \wedge uid_LI(l)=li$



Concrete Models of Mereology

The concrete mereology example models above illustrated maps and sequences as such models.

- In general we can model mereologies in terms of
 - ◊ (i) sets: **A-set**,
 - ◊ (ii) Cartesians: $A_1 \times A_2 \times \dots \times A_m$,
 - ◊ (iii) lists: A^* , and
 - ◊ (iv) maps: $A \xrightarrow{m} B$,

where A, A_1, A_2, \dots, A_m and B are types [we assume that they are type names] and where the A_1, A_2, \dots, A_m type names need not be distinct.

- Additional **concrete types**, say D , can be defined by **concrete type definitions**, $D = E$, where E is either of the **type expressions** (i–iv) given above or (v) $E_i | E_j$, or (vi) (E_i) . where E_k (for suitable k) are either of (i–vi).
- Finally it may be necessary to express well-formedness predicates for concretely modelled mereologies.

Abstract Models of Mereology

Abstractly modelling mereology of parts, to us, means the following.

- With part types P_1, P_2, \dots, P_n
 - ◊ is associated the unique part identifier types, $\Pi_1, \Pi_2, \dots, \Pi_n$,
 - ◊ that is $\text{uid}_{\Pi_i}: P_i \rightarrow \Pi_i$ for $i \in \{1..n\}$,
- and with each part type, P_i ,
 - ◊ is then associated a mereology observer,
 - ◊ $\text{mereo}_{P_i}: P_i \rightarrow \Pi_j\text{-set} \times \Pi_k\text{-set} \times \dots \times \Pi_\ell\text{-set}$,
- such that for all $p:P_i$ we have that
 - ◊ if $\text{mereo}_{P_i}(p) = (\{\dots, \pi_{j_a}, \dots\}, \{\dots, \pi_{k_b}, \dots\}, \dots, \{\dots, \pi_{\ell_c}, \dots\})$
 - ◊ for $i, j, k, \dots, \ell \in \{1..n\}$
 - ◊ then part $p:P_i$ is connected (related) to the parts identified by
 $\dots, \pi_{j_a}, \dots, \pi_{k_b}, \dots, \pi_{\ell_c}, \dots$
- Finally it may be necessary to express axioms for abstractly modelled mereologies.

- How **parts** are related to other **parts**
 - ❖ is really a modelling choice, made by the **domain describer**.
 - ❖ It is not necessarily something that is obvious from observing the **parts**.

Example: 27 Pipelines: A Physical Mereology.

- Let pipes of a pipe line be composed with valves, pumps, forks and joins of that pipe line.
- Pipes, valves, pumps, forks and joins (i.e., pipe line units) are given unique pipe, valve, pump, fork and join identifiers.
- A mereology for the pipe line could now endow pipes, valves and pumps with
 - ❖ one input unique identifier, that of the predecessor successor unit, and
 - ❖ one output unique identifier, that of the successor unit.
- Forks would then be endowed with
 - ❖ two input unique identifiers, and
 - ❖ one out put unique identifier;
- and joins “the other way around”.

Example: 28 Documents: A Conceptual Mereology.

- The mereology of, for example, this document,
 - ❖ that is, of the tutorial slides,
is determined by the author.
- There unfolds, while writing the document,
 - ❖ a set of unique identifiers
 - ❖ for section, subsection, sub-subsection, paragraph, etc., units.
and
 - ❖ between texts of a “paper version” of the document
and slides of a “slides version” of the document.

- This occurs as the author necessarily
 - ❖ inserts cross-references,
 - ⊗ in unit texts to other units, and
 - ⊗ from unit texts to other documents (i.e., ‘citations’);
 - ❖ and while inserting “page” shifts for the slides.
- From those inserted references there emerges what we could call the document mereology. ■
- So the determination of a, or the, mereology of composite parts
 - ❖ is either given by physical considerations,
 - ❖ or are given by (more-or-less) logical (or other) considerations,
 - ❖ or by combinations of these.
- The “design” of mereologies improves with experience.

Example: 29 Pipelines: Mereology.

- We divert from our line of examples centered around
 - ❖ transport nets and, to some degree,
 - ❖ container transport,
- to bring a second, in a series of examples
 - ❖ on pipelines
 - ❖ (for liquid or gaseous material flow).

76. A pipeline consists of connected units, $u:U$.

77. Units have unique identifiers.

78. And units have mereologies, $ui:U_i$:

a pump, $pu:Pu$, pipe, $pi:Pi$, and valve, $va:Va$, units have one input connector and one output connector;

b fork, $fo:Fo$, [join, $jo:Jo$] units have one [two] input connector[s] and two [one] output connector[s];

c well, $we:We$, [sink, $si:Si$] units have zero [one] input connector and one [zero] output connector.

d Connectors of a unit are designated by the unit identifier of the connected unit.

e The auxiliary $sel_U_i_in$ selector function selects the unique identifiers of pipeline units providing input to a unit;

f $sel_U_i_out$ selects unique identifiers of output recipients.

type76. $U = Pu \mid Pi \mid Va \mid Fo \mid Jo \mid Si \mid We$ 77. UI **value**77. $uid_U: U \rightarrow UI$ 78. $mereo_U: U \rightarrow UI\text{-set} \times UI\text{-set}$ 78. $wf_mereo_U: U \rightarrow \mathbf{Bool}$ 78. $wf_mereo_U(u) \equiv$ 78a. $is_ (Pu|Pi|Va)(u) \rightarrow \mathbf{card} \ iuis = 1 = \mathbf{card} \ ouis,$ 78b. $is_Fo(u) \rightarrow \mathbf{card} \ iuis = 1 \wedge \mathbf{card} \ ouis = 2,$ 78b. $is_Jo(u) \rightarrow \mathbf{card} \ iuis = 2 \wedge \mathbf{card} \ ouis = 1,$ 78c. $is_We(u) \rightarrow \mathbf{card} \ iuis = 0 \wedge \mathbf{card} \ ouis = 1,$ 78d. $is_Si(u) \rightarrow \mathbf{card} \ iuis = 1 \wedge \mathbf{card} \ ouis = 0$ 78e. sel_UIs_in 78e. $sel_UIs_in(u) \equiv \mathbf{let} \ (iuis, _) = mereo_U(u) \ \mathbf{in} \ iuis \ \mathbf{end}$ 78f. $sel_out: U \rightarrow UI\text{-set}$ 78f. $sel_UIs_out(u) \equiv \mathbf{let} \ (_, ouis) = mereo_U(u) \ \mathbf{in} \ ouis \ \mathbf{end}$


3.3.3. Attributes

- By an **attribute** of a part, $p:P$, we shall understand
 - ❖ some **observable property**, some **phenomenon**,
 - ❖ that is not a **sub-part** of p
 - ❖ but which characterises p
 - ❖ such that all parts of type P have that attribute and
 - ❖ such that “removing” that attribute from p
(if such was possible)
“renders” the type of p undefined.
- We ascribe types to attributes — not, therefore, to be confused with types of (their) parts.

Example: 30 Attributes.

- Example attributes of links of a transport net are:
 - ❖ length **LEN**,
 - ❖ location **LOC**,
 - ❖ state **LΣ** and
 - ❖ state space **LΩ**,
- Example attributes of a person could be:
 - ❖ name **NAM**,
 - ❖ birth date **BID**,
 - ❖ gender **GDR**,
 - ❖ weight **WGT**,
 - ❖ height **HGT** and
 - ❖ address **ADR**.

- Example attributes of a transport net could be:
 - ❖ name of the net,
 - ❖ legal owner of the net,
 - ❖ a map of the net,
 - ❖ etc.

 - Example attributes of a container vessel could be:
 - ❖ name of container vessel,
 - ❖ vessel dimensions,
 - ❖ vessel tonnage (TEU),
 - ❖ vessel owner,
 - ❖ current stowage plan,
 - ❖ current voyage plan, etc.
- 

3.3.3.1 Static and Dynamic Attributes

- By a **static attribute** we mean an attribute (of a part) whose value remains fixed.
- By a **dynamic attribute** we mean an attribute (of a part) whose value may vary.

Example: 31 Static and Dynamic Attributes.

- The length and location attributes of links are static.
- The state and state space attributes of links and hubs are dynamic.
- The birth-date attribute of a person is considered static.
- The height and weight attributes of a person are dynamic.
- The map of a transport net may be considered dynamic.
- The current stowage and the current voyage plans of a vessel should be considered dynamic. ■

Attribute Types and Observers, I/II

- Let the domain describer decide that parts of type P
- have attributes of types A_1, A_2, \dots, A_t .
- This means that the following two formal clauses arise:
 - ◇ P, A_1, A_2, \dots, A_t and
 - ◇ $\text{attr_}A_1:P \rightarrow A_1, \text{attr_}A_2:P \rightarrow A_2, \dots, \text{attr_}A_t:P \rightarrow A_t$

Attribute Types and Observers, II/II

- We may wish to annotate the list of attribute type names as to whether they are static or dynamic, that is,
 - ◇ whether values of some attribute type
 - ◇ vary or
 - ◇ remain fixed.
- The prefix `attr_` distinguishes attribute observers from part observers (`obs_`) and mereology observers (`uid_`, `mereo_`).

3.4. Shared Attributes and Properties

- Shared attributes and shared properties
 - ◇ play an important rôle in understanding domains.

3.4.1. Attribute Naming

- We now *impose a restriction* on the naming of part attributes.
 - ◇ If attributes
 - ⊗ of two different parts
 - ⊗ of different part types
 - ⊗ are identically named
 - ⊗ then attributes must be somehow related, over time!
 - ◇ The “somehow” relationship must be described.

Example: 32 Shared Bus Time Tables.

- Let our domain include that of *bus time tables* for *busses* on a *bus transport net* as described in many examples in this seminar.
- We can then imagine a *bus transport net* as containing the following parts:
 - ◇ a *net*,
 - ◇ a *management system*,
 - ◇ a set of *busses*.
- For the sake of argument we consider a *bus time table* to be an attribute of the *bus management system*.
- And we also consider *bus time tables* to be attributes of *busses*.

- We think of the *bus time table* of a *bus*
 - ◇ to be that subset of the *bus management system bus time table*
 - ◇ which corresponds to the *bus' line number*.
 - By saying that *bus time tables*
 - ◇ “corresponds” to well-defined subsets of
 - ◇ the *bus management system bus time table*
- we mean the following
- ◇ The value of the *bus bus time table*
 - ◇ must at every time
 - ◇ be equal to the corresponding *bus line entry* in the *bus management system bus time table*. ■

3.4.2. Attribute Sharing

- We say that two parts,
 - ❖ of no matter what part type,
 - ❖ *share* an attribute,
 - ❖ if the following is the case:
 - ⊗ the corresponding part types (and hence the parts)
 - ⊗ have identically named attributes.
 - ⊗ We say that identically named attributes designate shared attributes.
 - ❖ We do not present the corresponding invariants over parts with identically named attributes.

3.5. Shared Properties

- We say that two **parts**,
 - ◇ of no matter what **part type**,
 - ◇ *share* a **property**,
 - ◇ if either of the following is the case:
 - ⊗ (i) either the corresponding **part types** (and hence the **parts**) have **shared attributes**;
 - ⊗ (ii) or the **unique identifier type** of one of the **parts** potentially is in the **mereology type** of the other **part**;
 - ⊗ (iii) or both.
 - ◇ We do not present the corresponding **invariants** over **parts** with **shared properties**.

3.6. Summary of Discrete Endurants

- We have introduced the **endurant** notions of **atomic parts** and **composite parts**:
 - ◇ part types,
 - ◇ part observers (**obs_**),
 - ⊗ sort observers, and
 - ⊗ concrete type observers;
 - ◇ part properties:
 - ⊗ unique identifiers:
 - * unique part identifier observers (**uid_**),
 - * unique part identifier types,
 - ⊗ mereology:
 - * part mereologies,
 - * part mereology observers (**mereo_**);
 - and
 - ⊗ attributes:
 - * attribute observers (**attr_**)
 - and
 - * attribute types.

- The **unique identifier** property cannot necessarily be observed:
 - ❖ it is an **abstract concept** and
 - ❖ can be objectively “assigned”.

That is: **unique identifiers** are not required to be manifest.

- The **mereology** property also cannot usually be observed:
 - ❖ it is also an **abstract concept**,
 - ❖ but can be deduced from careful analysis.

That is: **mereology** is not required to be manifest.

- The **attributes** can be observed:
 - ❖ usually by simple physical measurements,
 - ❖ or by deduction from (conceptual) facts,

That is: **attributes** are usually only “indirectly” manifest.

Discrete Endurant Modelling I/II

Faced with a phenomenon the domain analyser has to decide

- whether that **phenomenon** is an **entity** or not, that is, whether
 - ◇ an **endurant** or
 - ◇ a **perdurant** or
 - ◇ neither.
- If **endurant** and if **discrete**, then whether it is
 - ◇ an **atomic part** or
 - ◇ a **composite part**.
- Then the **domain analyser** must decide on its type,
 - ◇ whether an **abstract type** (a **sort**)
 - ◇ or a **concrete type**, and, if so, which concrete form.

Discrete Endurant Modelling II/II

- Next the **unique identifier** and the **mereology** of the **part type** (e.g., P) must be dealt with:
 - ◇ **type name** (e.g., PI) for and, hence, **unique identifier observer name** (uid_{PI}) of unique identifiers and the
 - ◇ **part mereology types** and **mereology observer name** ($mereo_P$).
- Finally the designer must decide on the **part type attributes** for parts $p:P$:
 - ◇ for each such a suitable **attribute type name**, for example, A_i for suitable i ,
 - ◇ a corresponding **attribute observer signature**, $attr_{A_i}:P \rightarrow A_i$,
 - ◇ and whether an attribute is considered **static** or **dynamic**.