

Independent Component Analysis Applied to Pulse Oximetry in the Estimation of the Arterial Oxygen Saturation (S_pO_2) - a Comparative Study

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Abstract— We examine various independent component analysis (ICA) digital signal processing algorithms for estimating the arterial oxygen saturation (S_pO_2) as measured by a reflective pulse oximeter. The ICA algorithms examined are FastICA, Maximum Likelihood ICA (ICAML), Molgedey and Schuster ICA (ICAMS), and Mean Field ICA (ICAMF). The signal processing includes pre-processing bandpass filtering to eliminate noise, and post-processing by calculating the S_pO_2 . The algorithms are compared to the commercial state-of-the-art algorithm Discrete Saturation Transform (DST) by Masimo Corporation. It is demonstrated that ICAMS and ICAMF perform up to 13% better than DST. PPG recordings are done with a reflective pulse oximetry sensor integrated in an Electronic Patch. This system is intended for patients with chronic heart and lung conditions.

I. INTRODUCTION

Pulse oximeters intended for long-term monitoring of people living an everyday life with a chronic condition offer several challenges: 1) Design and construction of small, discrete, and low-power pulse oximeter devices. 2) Digital signal processing of photoplethysmograms (PPG) which are affected by the patient's motions, a less optimal monitoring site for the purpose of discreteness and long-term compatibility, and battery powered Light Emitting Diodes (LEDs). 3) Integration of these new technologies which typically features telehealth solutions into the established health care system.

We have previously reported the design and development of an Electronic Patch with integrated reflective pulse oximetry based on a novel ring-shaped optical sensor [1], [2], [3]. The Electronic Patch is shown in Fig. 1. All PPG measurements reported in this paper are performed with the Electronic Patch.

Estimating the S_pO_2 from PPG data which are heavily distorted by noise and motion artefacts can be done by

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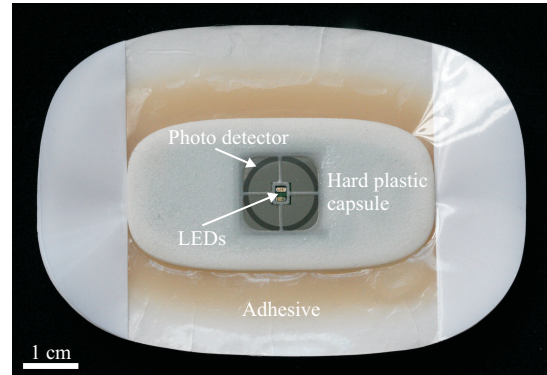


Fig. 1. The Electronic Patch. The patch contains a micro fabricated ring-shaped silicon backside photodiode with a through chip hole for commercial surface mounted LEDs. This is packaged inside a hard plastic capsule with analog, digital, and RF electronics. The capsule is embedded in adhesive material as shown in the figure. The patch measures 88 mm by 60 mm and is 5 mm thick. The weight is 15.9 grams.

advanced digital signal processing. The commercial state-of-the-art, Discrete Saturation Transform (DST) by Masimo Corporation [4], is often used in clinical pulse oximeters. To benefit most from the above mentioned category of low-power pulse oximeters algorithms which are better at noise and motion filtering are needed.

Signal processing of PPG data using independent component analysis (ICA) has been reported by several authors [5], [6] as a promising technique for motion artefact reduction. These papers do not describe the problem of estimating the S_pO_2 nor do they present a comparison with the DST algorithm. In this paper we evaluate four different ICA algorithms with respect to estimating S_pO_2 from normal PPG data (i.e. not motion distorted) but recorded with the Electronic Patch under low-power conditions (the LED driving current is 5 mA). The ICA algorithms are compared to the DST algorithm.

Most authors focus on the FastICA algorithm [7], [8], but there are several other ICA algorithms such as Maximum Likelihood ICA (ICAML) [9], [10], [11], Molgedey and Schouster ICA (ICAMS) [10], [12], [13] and Mean Field ICA (ICAMF) [14], [15]. The various ICA algorithms are based on different assumptions regarding the statistical properties of the source signals and work by optimizing different parameters such as autocorrelation and probability distributions

in the attempt to separate sources and noise signals.

The hypothesis of this paper is that the quality of the separated PPG signals and consequently the S_pO_2 prediction depends critically on the choice of ICA algorithm. Motivated by this we present a comparison of the mentioned four different ICA algorithms and the DST algorithm. We evaluate the algorithms by comparing the estimated S_pO_2 values with reference values obtained by a commercial pulse oximeter for the intensive care unit.

II. DISCRETE SATURATION TRANSFORM

DST is based on the assumption that the measured signals can be described as a sum of a desired PPG signal $s(t)$ and a noise signal $n(t)$ due to motion artifacts. Masimo [4] defines the system as

$$\begin{aligned} x_{ir}(t) &= s(t) + n(t) & (1) \\ x_r(t) &= r_a s(t) + r_v n(t) & (2) \end{aligned}$$

with $x_{ir}(t)$ and $x_r(t)$ being the signals from the infrared and red recordings respectively and r_a is the arterial ratio corresponding to the arterial saturation and r_v is the ratio of venous, or non-arterial, components. The method is based on removal of the noise term $n(t)$ by the use of Adaptive Noise Cancellation (ANC) [16]. In pulse oximetry a noise signal is not available and Masimo therefore defines a reference noise signal $n'(t)$ as a weighted difference of the normalised measured signals

$$n'(t) = x_r(t) - r x_{ir}(t). \quad (3)$$

By inserting (1) and (2) in (3)

$$\begin{aligned} n'(t) &= r_a s(t) + r_v n(t) - r(s(t) + n(t)) & (4) \\ &= (r_a - r)s(t) + (r_v - r)n(t). & (5) \end{aligned}$$

It is seen from (5) that when $r_a = r$ the reference noise signal $n'(t)$ only contains the weighted noise of the measurements. The measured signal from the red LED $x_r(t)$ is applied as the input to the ANC with the reference signal $n'(t)$ and the desired output of the ANC is the noise free PPG-signal $s(t)$. The coefficient r is found iteratively by trying all values of r corresponding to all S_pO_2 levels from 0-100% in steps of e.g. 1%. The power of the output signal from the ANC is calculated for each reference signal. This results in a power spectrum for the values of r that will have two peaks; one at $r = r_v$ and one at $r = r_a$ where the latter is the desired ratio. The implementation of DST used for this paper uses a recursive least squares (RLS) adaptive FIR filter of order 128. It is found that this order gives a desirable performance and increasing the order will only slow down the algorithm. The coefficient r is increased by a step size of 0.01 to ensure the resolution in S_pO_2 is less than 1%.

III. INDEPENDENT COMPONENT ANALYSIS

The general ICA model is formulated as

$$\mathbf{X} = \mathbf{A}\mathbf{S} \quad (6)$$

where \mathbf{X} is a matrix of observed multiple signal samples, \mathbf{A} is a mixing matrix, and \mathbf{S} is a matrix of independent source signal samples. The aim is then to estimate \mathbf{A} and \mathbf{S} .

By assuming each of the pulse oximetry recordings contains a component representing the PPG signal $s_1(t)$ and an independent noise component $s_2(t)$ the ICA model for pulse oximetry is given by the 2-by-2 linear mixing system¹

$$\begin{aligned} x_r(t) &= a_{11}s_1(t) + a_{12}s_2(t) & (7) \\ x_{ir}(t) &= a_{21}s_1(t) + a_{22}s_2(t) & (8) \end{aligned}$$

where a_{ij} are the coefficients determining the elements of the mixing matrix \mathbf{A} in (6). The optical ratio is then estimated by the ratio of the mixing coefficients of the PPG source signal

$$R = \frac{a_{11}}{a_{21}}. \quad (9)$$

A. FastICA

FastICA works by maximizing the negentropy of the independent source signals. Negentropy can be interpreted as a measure of non-Gaussianity². The main advantage of this algorithm is due to its simple fixed-point iteration scheme.

B. Maximum Likelihood ICA

ICAML separates the independent identically distributed source signals by maximizing the likelihood of the mixing matrix. To use the maximum likelihood approach the score function associated with the source prior distribution is required.

C. Molgedey and Schouster ICA

ICAMS is based on dynamic decorrelation and requires that the sources have different autocorrelation functions. The mixing matrix is estimated by maximizing the difference in autocorrelation of the source signals.

D. Mean Field ICA

ICAMF is a Bayesian probabilistic method for solving the ICA problem and is rather flexible with respect to specification of constraints and prior assumptions. The model differs from the general ICA model as it assumes the observed signals \mathbf{X} are generated with an additive white noise source \mathbf{E} . In the present context this is a reasonable assumption since it is unrealistic that the noise signals picked up in the red and infrared channels are identical except for scaling, as assumed in (7).

$$\mathbf{X} = \mathbf{A}\mathbf{S} + \mathbf{E}. \quad (10)$$

The noise \mathbf{E} is assumed to be Gaussian with zero mean and covariance Σ . The noise covariance matrix can further be constrained to be isotropic or diagonal for same noise variance on the observations or individual noise variance for each observation, respectively. It is found that a configuration with a diagonal covariance matrix gave the best results.

¹An extended model is provided in (10). See also the future work section below.

²It is well-known that white Gaussian distributed source signals can not be separated, [17].

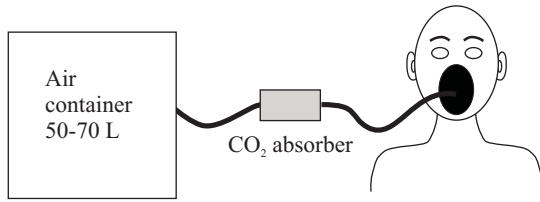


Fig. 2. To lower the oxygen saturation a closed circuit is used. The subjects re-breathe air from a container through a carbon dioxide filter of calcium hydroxide, Soda Lime (Dräger). The S_pO_2 is lowered from 100% to 75% on the average of 16 min.

TABLE I
LENGTH OF SIGNALS AND START AND END REFERENCE S_pO_2 LEVELS
FOR THE THREE SUBJECTS.

Subject	Length (s)	S_pO_2 start (%)	S_pO_2 end (%)
1	760	98	74
2	1111	100	86
3	1020	100	70

ICAMF allows one to use several prior distributions for the sources and it is found that a bi-Gauss distribution was the best choice for the PPG-signals. Beside this, the mixing matrix is constraint to be positive as the R should be positive.

IV. CLINICAL METHODS AND MATERIALS

We perform non-invasive self testing on healthy subjects. The subject is seated at rest and the oxygen saturation measured on the third digit of the right hand by a pulse oximeter, Datex-Ohmeda AS/3 Compact Patient Monitor, Pulse Oximeter. The Electronic Patch is placed on the skin over the third digit of the left hand. The PPG signal are measured continuously with the reference S_pO_2 value is read of every 30s. The sampling frequency of the PPG data is $f_s = 200$ Hz. The total length of the PPG sequences for the three subjects and the starting and ending reference S_pO_2 levels are given in Table I.

The subjects re-breathe in a closed circuit in order to lower the oxygen saturation as illustrated in Fig. 2. At the initiation of each test the circuit is filled with approximately 50 - 70 liters of atmospheric air. Carbon dioxide CO_2 is absorbed from the circuit by exhaling through a filter of calcium hydroxide, Soda Lime (Dräger). The measurements are initiated by a few deep inspirations of 100% oxygen and then the breathing is changed to the closed circuit. The subject now breath continuously in the closed circuit. A decline in oxygen saturation is measured as the oxygen concentration in the circuit decreases.

Prior to the investigations it is agreed to end the testing when the oxygen saturation reached 75% or earlier if the subject felt uncomfortable.

V. SIGNAL PROCESSING

The optical ratio R is calculated for signal windows of 30s corresponding to the reference measurements. For each window the following signal processing is done:

The PPG signals are normalized by subtracting the DC-component and dividing by the DC-component. This is done

TABLE II
BANDPASS FILTER CUT-FREQUENCIES

Algorithm	f_l (Hz)	f_h (Hz)
DST	0.9	3
FastICA	1	3
ICAML	1	2
ICAMS	1	3
ICAMF	0.8	3

to scale the recordings from each subject to the same range. To avoid high frequency electrical noise and low frequency noise components bandpass filtering is applied. It is found that the best performance is achieved by a 8th order IIR (Butterworth) filter. The cutoff frequencies are optimized for each algorithm and are given in Table II as lower cutoff frequency f_l and higher cutoff frequency f_h . To avoid distortion due to filter settling time an overlap of 4s is added to the front of the signal windows before filtering and removed again after filtering.

The signal processing can be summarized into five steps:

- 1) Normalisation
- 2) Bandpass filtering
- 3) Estimation of R
- 4) Estimation of calibration curve
- 5) Estimation of S_pO_2

A. Evaluation Scheme

To evaluate the estimates of R a calibration curve that relates the R -values to the S_pO_2 in % is needed. From the theory of pulse-oximetry [18] it is known that the calibration curve is on the form

$$S_pO_2 = \frac{a + bR}{c + dR}. \quad (11)$$

However, in the important S_pO_2 range from 70% to 100% a linear approximation to the calibration curve can be used. It follows from derivation using Beer-Lambert's law that the gradient of the linear approximation should be negative [18].

To obtain a calibration curve that does not depend heavily on the available data set a training and test set evaluation scheme is applied: The R -estimates are divided into a training and test set consisting of values from two and one subjects respectively. A calibration curve is calculated from the training set by using the leave-one-out method. One estimate is left out and a linear model is fitted to the rest of the estimates. This is repeated for all estimates in the training set and the mean of the coefficients of all fitted calibration curves is used as a final linear calibration curve for testing. The obtained calibration curve is used to predict test set S_pO_2 values from R -values. Finally, the test error is calculated as the Euclidean difference between the estimated and the reference measurement of S_pO_2 . The procedure is repeated for all three combinations of training and test set. The average error is then calculated for each algorithm.

VI. RESULTS

In Fig. 3 is shown the result for the DST algorithm as the reference S_pO_2 values versus the estimated arterial ratios,

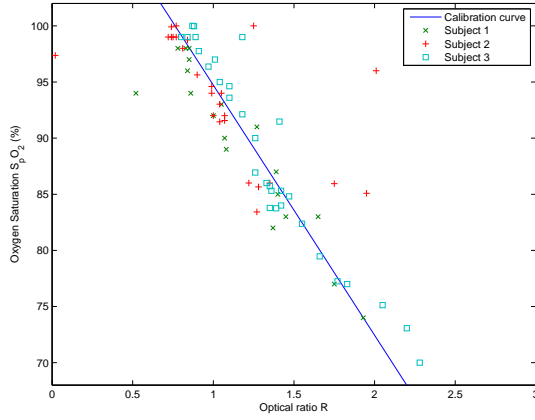


Fig. 3. Calibration curve and estimates obtained using DST. It is seen that the linear model fits most of the estimates, but some estimates could be considered as outliers.

TABLE III

MEAN ERROR FOR EACH ALGORITHM AND LOWER, f_l , AND HIGHER, f_h BANDPASS FILTER CUT-FREQUENCIES.

Algorithm	S_pO_2 error	Error relative to DST
DST	3.0	-
FastICA	21	600%
ICAML	3.4	13%
ICAMS	2.9	-3%
ICAMF	2.6	-13%

r_a . It is seen from this graph that the algorithm gives a calibration curve and that the results from the three subjects fall within the same range. The average error is found to be 3.0%.

In Fig. 4, 5, 6, and 7 are shown the results for the four ICA algorithms. From Fig. 4 it is seen that the FastICA algorithm fails to give a valid calibration curve as the best fit has a positive slope (this should be negative as previously described). The ICAML, ICAMS, and ICAMF algorithms all give a correct calibration curve. The ICAMS and ICAMF algorithms give results that are more similar to the result from the DST algorithm compared to the ICAML algorithm. For the DST, ICAMS, and MCAMF the linear fit is correct in the range 100%-80% but fails in the range 80%-70%.

The average Euclidean error and the relative error compared to the DST error is listed in Table III for the all algorithms. With respect to these measures it is seen that ICAML performs 13% worse than DST. Both ICAMS and ICAMF performs better than DST with relative improvements of 3% and 13%, respectively.

VII. DISCUSSION

The purpose of this work is to study ICA algorithms by comparing them with respect to each other and to the DST algorithm. The purpose is not to obtain a calibration curve for future use. Therefore the quality of the reference data is of less importance and we choose to use a non-invasive method that does not require a clinical protocol (by Danish law). More precise reference data could be obtained by collecting

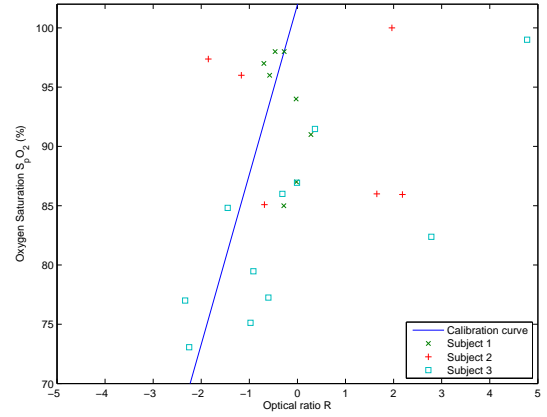


Fig. 4. Calibration curve obtained using FastICA. It is clear that this algorithm fails to estimate R as a most of the estimates are less than zero and the calibration curve has a positive slope. It should be noted that a fewer estimates are seen. This is due to the algorithm not converging for parts of the data.

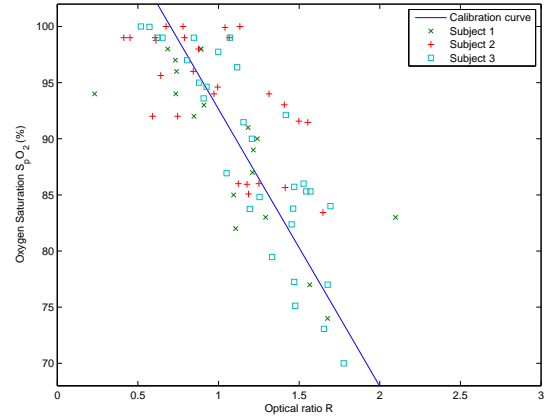


Fig. 5. Calibration curve and estimates obtained using ICAML. Compared to the DST algorithm the estimates deviates more from the calibration curve.

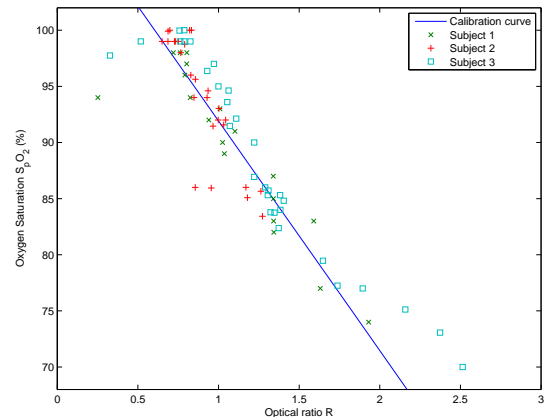


Fig. 6. Calibration curve and estimates obtained using ICAMS. The performance is similar to the DST algorithm. Notice the estimates below 80% do not fit the linear model approximation.

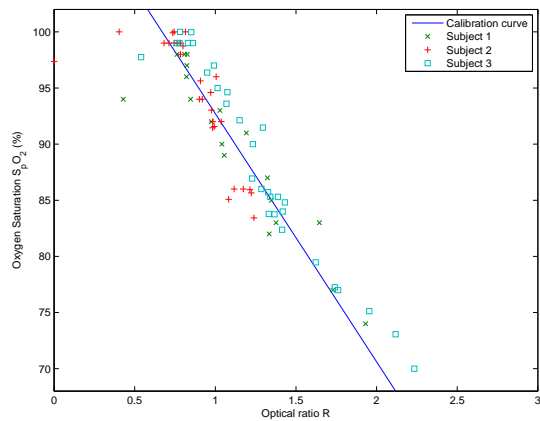


Fig. 7. Calibration curve and estimates obtained using ICAMF. The performance is similar to the DST algorithm, but the algorithm appears to be more robust when considering possible outliers.

arterial blood samples from which the oxygen saturation can be found accurately by a blood gas analyzer.

The non-invasive method we have used resulted in an error of 3.0% for the DST algorithm. A commercial pulse oximeter by Masimo Corporation has a specified accuracy of 2% [19], the obtained reference data must therefore be considered useful.

The obtained calibration curves suggest that the linear model approximation is good in the S_pO_2 range of 80% to 100% whereas below this range a nonlinear relation is a better choice.

VIII. CONCLUSION AND FUTURE WORK

A. Conclusions

We have successfully demonstrated ICA algorithms in the application of estimating the arterial oxygen saturation by pulse oximetry. Four ICA algorithms have been evaluated and compared to DST. The four algorithms did perform differently. The ICAMF is found to give the best results with an relative improvement over the DST algorithm of 13%. The FastICA algorithm did not work and failed to converge for part of the data. The ICAMS showed a relative improvement of 3% over DST and the ICAML show a decline of 13% compared to DST.

It can be concluded that ICA can be used for calculating S_pO_2 when the ICA problem is solved using the right constraints. We conclude that the difference in autocorrelation of the source signals and the bi-Gaussian distribution of the PPG signal and individual noise on the red and infrared recordings are the useful constraints.

The accuracy of the S_pO_2 values do indeed depend on the choice of ICA algorithm, and we have found that the ICAMF is the best choice.

B. Future Work

Motion artifacts are serious noise component in the recorded signals. We believe that ICA models could provide a good framework for handling such problems which is suggested by initial experiments. We consider a more general

framework using a linear state-space based model suggested in [20] which allows for more flexible mixing and prior source models. In addition, the model can handle the so-called underdetermined case, i.e. more signals than sources. This is useful for modeling different noise sources which could have very different dynamics.

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