Model Checking Geographically Distributed Railway Control Systems

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Summary (English)

The goal of this project is to investigate model checking as a verification method for analysis of distributed railway control systems wrt. safety.

To drive this investigation an engineering concept of a distributed railway interlocking system is conceived and described. The concept is distilled into an abstract generic model in a model checking language. Furthermore is a tool developed to assist in generating concrete models from the generic model, that are both valid and constrained to help reduce the state space to be searched when model checking the concrete model instances.

The outcome of the project is not only a verified engineering concept, an abstract model of the concept and a tool to assist in exploring concrete instances an abstract model, -but also an example of how an engineering concept can be modeled as an abstract model and verified through model checking. <u>ii</u>_____

Summary (Danish)

Målet med dette projekt er at undersøge model checking som metode til verificering og analyse af sikkerheden i distribuerede tog kontrol systemer.

For at motivere undersøgelsen er et konkret engineering koncept udarbejdet og beskrevet. Konceptet er derefter destileret ned til en abstrakt generisk model i et model checker sprog. Yderligere, er et værktøj udviklet til at assistere med at generere instanser af den generiske model som er korrekte og afgrænsede, således at de reducerer det tilstandsrum som skal gennemsøges af et model checker værktøj.

Resultatet af projektet er ikke bare et verificeret engineering koncept, en abstrakt model af konceptet og et værktøj til at hjælpe med at udforske modelen gennem konkrete instanser, men er også et eksempel på hvordan et konkret engineering koncept kan modeleres som en abstrakt model og verificeres gennem model checking. iv

Preface

This thesis was prepared at DTU Compute in fulfilment of the requirements for acquiring an M.Sc. in Computer Science and Engineering.

The thesis deals with the investigation of use of model checking as a means of verification of safety properties in railway interlocking systems.

The thesis has been written in the period from April 1 2016 to October 21 2016 under supervision of associate professor Anne Elisabeth Haxthausen and professor Alessandro Fantechi, and is worth 35 ECTS credits.

The thesis consists of the following report and an associated CD that contains source code files of a tool generated as part of the project, a compiled executable version of the tool and samples of generated models and XML files which can be used in the process of generating models.

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CHAPTER 1

Introduction

Our world is becoming increasingly more automated, improving our living conditions and providing comfort and safety. Today, difficult tasks such as, for example, controlling an aircraft is by large either controlled by or assisted by automation, and currently tech companies and car manufacturers are pushing the limits for autonomous car driving. As we apply automation to more areas and expand responsibilities of already automated systems, -the complexity increases. This increasing complexity becomes a huge task to handle for the engineers designing the systems. Often systems are so complex that it is impossible for the engineers to get a full overview of the given system and confidently predict its behavior.

Model checking is a methodology which was invented to help analyse such complex systems, and has been successfully applied, for example, in the analysis of concurrent systems.

Trains has become an essential part of many peoples life. In big cities millions of people commute daily to school or jobs by different variations of train systems, such as inter city trains, urban railways, streetcars, subways or light railways. Every day goods and people are transported within and across borders all over the world by trains. And in some places high speed trains are means of transportation which is competitive with other typical ways of fast transportation such as airplanes. When designed and utilized properly, railway transportation has potential to out-compete many other means of transportation in regards to efficiency. As focus on energy consumption increases around the world, it is very likely that railway transportation will get even more attention in the future.

Even though transportation by train is one of the safest means of transportation today, fatal accidents still happens. In 2016 alone, at least three major train accidents has occurred.

Early 2016 a fatal accident happened in Germany where two trains ended up in a frontal collision on a two-way track. The cause for this incident has been revealed to be a human error caused by a track operator, who accidentally sent warning signals to the wrong recipients instead of the two trains that were on a collision course[mInB16]. Later on in 2016, again two trains ended up in a headon frontal collision in Italy, and yet again the investigations seems to point to a human track operator error. Yet again later on in 2016 another train accident happened in New Jersey, where a train ran through an end-of-track-barrier and into a wall at high speed, once again a human error happened and there was no fail-safe technology to take over and prevent the accident.

Railway systems are in general very safe and the probability of a train being involved in an accident is quite small compared to other means of transportation. However, guarenteing safety in huge railway systems with many intersections and lots of traffic can be very challenging. Thus the invention of, so called, *interlocking systems* which are systems that serve to ensure safe operations of the trains.

There are many other challenges in railway systems, such as scheduling and liveness of trains, and sometimes solutions to these challenges interfere with how the interlocking system operates. This leads to an interest in optimizing the interlocking systems, which in the end possibly makes them even more complex.

Given that so many people rely on trains for transportation, it is naturally important that an effort is put into ensuring safety, availability and reliability. Railway interlocking systems has indeed been analyzed many times before with regard to both safety and liveness.

In this thesis work an engineering concept of a geographically distributed interlocking system, sporting a sequential release mechanism for increased utility of the given railway network, is explored and analyzed through model checking. The work has been done in the context of the RobustRailS research project[Col, Hax] in which research on formal verification of railway control systems is pursued. An important motivating factor for using model checking, is that it is a verification method recommended in railway signalling safety guidelines for software, specified by the European Committee for Electrotechnical Standardization [CEN11]. The work in this thesis is especially inspired by the work described in [Fan12] and [Pao10], where the idea of a geographically distributed interlocking system using a two-phase commit protocol for route reservation, -is presented and modeled. Furthermore does the work presented in this thesis draw a lot of inspiration from the work in [VHP16], where formal methods are applied to verify safety properties of a new Danish interlocking system that features a sequential release mechanism for increased utility of railway network capacities.

1.1 Content of the thesis work

This section describes the chapters of the thesis work that are to follow this chapter.

chapter 2 - Railway Domain

Briefly explains the basic concepts and terminology of the rail way domain. The chapter serves to prepare the reader for the rest of the thesis work where the terminology will be used extensively.

chapter 3 - Formal Specification and Verification of Software Systems

Gives a brief outline of common methods of ensuring correctness in software systems, and ends up briefly explaining the concept of model checking which is the method used in this thesis work.

chapter 4 - The UMC modeling language

Introduces the modeling language utilized for this project.

chapter 5 - An Engineering Concept of a Geographically Distributed Interlocking System

Describes an engineering concept for a distributed railway interlocking system conceived as part of this project.

chapter 6 - Modeling the Geographically Distributed Interlocking System in UMC

Describes the translation of the engineering concept into an abstract generic model that can be used for model checking.

chapter 7 - Model generating tool

Describes an implementation of a tool for generating concrete model instances based on the generic model.

chapter 8 - Experiments

Presents and elaborates over a set of model checking experiments performed with different concrete model instances.

chapter 9 - Future work

Elaborates over ideas for extensions to the tool and improvements for the abstract generic model are presented.

chapter 10 - Conclusion

Sums up the work and yields conclusions in relation to the project.

Chapter 2

Railway Domain

What cannot be imagined cannot even be talked about.

Ludwig Wittgenstein

2.1 Terminology and Components of Railway Systems

The railway domain is almost two centuries old, and thus it makes sense that a distinctive terminology for talking about railway systems has developed. Fortunately the English terminology has evolved differently in Europe and America. In this thesis work, the European terminology will be used.

The basic elements that make up a railway system, are *points*, *signals*, *interlocking systems*, *track circuits*, *main tracks* (linear tracks), loops and sidings. A point (switch in American terminology) is a branching from the main track with a mechanical functionality to switch between the main track and the branch. In old systems points required a human operator to manipulate a hand-operated lever, however in modern railway systems the points are operated by

a point machine which is an electric device that can perform the switching and can be operated from afar.

In context of a railway layout a point can be described as a straight path with a branch into a diverging path, they do however have many different shapes and multiple points can be composed into complex intersections. Generally speaking, a point can be in one of two states (or *positions*) which are referred to as *plus* and *minus*, where plus denotes that the point is positioned such that the the point connects in a straight line, and minus denotes that the point connects to a diverging path.

Following drawings illustrate the described elements.



Figure 2.1: Illustration of a point switched to a minus position, a loop, a siding and a track circuit sensor.

A signal can either be a physical signal light which, for example communicates the occupation status of the coming track segment. A signal can also be a virtual signal communicating speed limitations or wait and go messages directly to the operator through an electronic interface in the train, or communicated directly to an autonomous train control system. What is general for the term signal is that it represents a way of communicating things such as stop and go messages or speed up and slow down messages to trains operating on a railway network.

The main tracks (linear track) are the regular train tracks, and the term loop describes a track which branch out from the main tracks and rejoins them again at a later point. The term siding refers to a branching track with a dead end which often is used for maintenance of the trains. A track circuit is an electrical sensor which can detect the absence or presence of a train on a track segment. Finally an interlocking system, is a control system which is responsible for safe operation of the trains, which at the most basic level involves controlling the signals to avoid conflicting train movements and controlling the points positioning so they are set accordingly for a passing train.

2.1.1 Recent Developments

As communication devices like GSM (Global System for Mobile Communications) become more reliable and cheaper, and other micro processors likewise, it naturally becomes more relevant to use such technologies in systems like railway control systems.

The railway industry is already in progress of moving from *physical light signals* to *virtual signals* in the form of *cab signaling systems*. In a cab signaling system, virtual signals send to the trains are communicated directly to the train operator by some kind of interface.

Another advancement is the automation of train systems, and especially metro systems in big cities. In these systems the trains are made completely autonomous and so is all signaling and point switching. Autonomous systems requires more and advanced sensors, but could potentially factor out some of the human errors that often lead to fatal accidents. As of now, train automation is mostly seen in metro railway systems, because such railway systems are smaller and more confined from the surroundings than typical railway systems are.

2.2 Safety Measures and Interlocking Systems

Train operation is in general a safe way of transportation relative to other means of transportation, which by large is because of the confined nature of trains, since the movement of a train is limited to the given railway track layout. This reduces the safety concerns for operation of individual trains to concerns such as avoiding derailing accidents. This is done by making sure points remain in stable and correct positions, and by making sure the train is operating within the speed limits. However, safety becomes an even bigger concern when multiple trains are utilizing the same railway tracks as collisions becomes possible.

Many measures both in the large and in the small are taken to minimize the risk of accidents. In the small, *track circuit* sensors are for example designed such that they will constantly indicate presence of a train when there is a failure in the sensor.

In the large safety is ensured through an interlocking system. Railway systems are often composed of a central operation control center, an interlocking system and a signaling system which is either fully or partially controlled by the interlocking system.

At the central operation control, the itinerary plan is created and the execution of the plan is carefully monitored by observing the states of signal lights and sensors on the railways. The light signals can be controlled from the central control center, however the control usually goes through an interlocking system which ultimately is responsible for maintaining safety while executing the plan.

The interlocking system will constantly monitor sensor readings and location data for the trains and take actions to ensure that accidents are prevented. It does so by keeping a record the current train routes and by controlling the points and signals, where the signals constitutes of stop and go signals and signals to speed up or slow down. Traditionally the train routes were registered in interlocking control tables, and then the interlocking system would generate a proper execution order for the routes.

In order to guarantee the safety of the trains in the railway system, following requirements must be met.[TV09]

- Track sections in front of the train must be clear from other trains until it has passed.
- Points on the route of the train must be set to the correct positions.
- Speed changes of a train must be applied in sufficient time in order to slow down or speed up to reach permitted speed.

The noble task of the interlocking system is to avoid following situations at all times.

- Head to head collision, which can happen if two trains coming from opposite directions are able to occupy the same track segment. This is probably the most fatal type of error.
- Head to tail collision, this can again happen if two trains are able to occupy the same track segment at the same time.
- Derailment, a derailment of a train can happen if the train traverses a point which is switched to the wrong direction or if the point is performing the mechanical switching while the train is traversing it.

There are multiple ways for interlocking systems to ensure that the above situations are avoided. The simplest way, is to require routes to be fully reserved before permitting a train to traverse it, and not allowing other trains to traverse routes reserved by other trains.

In the case of trains operated by humans, there is still a risk of trains violating reserved routes. To counter this, some interlocking systems uses flank protection, which means that points neighboring other points on the reserved route, will be locked into a positioning such that they are disconnected from the point on the reserved route. This will effectively divert foreign trains from over-running the reserved route.

2.3 Route Reservation Methods

One of the most common methods of ensuring safety along the route of a train, is to fully reserve the whole route and marking it as locked such that no other trains can use it. However, to ensure liveness it is necessary to release the route again at some point. One approach, called *sequential release*, is to release a track segment as soon as the train which reserved it has left it. Another approach is to, strictly, not release anything on the reserved path until the train has completely finished its route. The latter approach is the simplest approach to making the system safe, however it also leads to a poorer utilization of available resources than what can be achieved with sequential release.

Another more extreme version of sequential release, is to define so called *moving* safety distance blocks around the trains based on their braking distance. This approach requires very precise sensory data input, but can in theory optimize the utilization of resources. One problem with this approach is that the moving block is more of a continuous event rather than discrete and this makes it more difficult to model check.

Chapter 3

Formal Specification and Verification of Software Systems

Program testing can be a very effective way to show the presence of bugs, but it is hopelessly inadequate for showing their absence.

Edsger W. Dijkstra

Automation has an increasing important role in modern society. From simple tasks such as dispensing sodas to thirsty customers, to more important tasks such as handling money transactions, to more complex tasks such as ensuring safety on railways, in airplanes or even controlling cars autonomously.

The automation is implemented by engineers and software developers who are nothing but humans, and humans tend to make errors. Given the continuous increase in complexity, these systems are bound to contain at least a few errors. We have already experienced many incidents through history where a bug or faulty implementation manifested itself and led to disasters such as fatal overdoses of radiation¹ or huge loss of money and wasted effort².

3.1 Common Methods for Ensuring Corectness in Software Systems

Given that the consequences of a faulty implementation can be so severe and have such awful consequences, it is very important that engineers and software developers are able to guarantee the safety of the systems they develop. Thus ensuring correctness and safety in software systems is an important pursuit, and many techniques and methodologies has been investigated and utilized with varying degrees of success through time.

3.1.1 Type Checking

Back in the 1970's, the American military were increasingly concerned about safety, correctness and composeability of the software they produced, and as a result they ended up sponsoring the development of the strongly typed programming language Ada. The strong typing system and the type checker, assisted developers to construct more safe and correct software. Ada quickly came to be one of the preferred languages to be used when developing safety critical software, -not only for the American army but also in industries such as the aerospace industries.

Recently a dependently typed programming language Idris[BRA13] has been developed facilitating types as first-class language constructs and with the goal of making dependent types and proof assistant features more accessible for software developers.

 $^{^1\}mathrm{Between}$ 1985 and 1987 patients were given an overdoses of radiation due to a concurrent programming error.[Wikc]

²In 1999 a mars orbiter probe crashed uncontrollably into the atmosphere of Mars. Investigation later revealed that two communicating sub-systems were implemented with different units of measures in mind.[Wika]

3.1.2 Testing

Perhaps the most common approach to ensuring safety and correctness in software systems is testing, where especially unit-testing has catched on in popularity. Unit testing is used for both black box and white box testing systems, and has been very popular in the industry since its fairly easy to understand and apply. The popularity of software testing, has even lead to new software development methodologies such as Test Driven Development (TDD), where tests are specified before the actual functionality is implemented.

However, as Edsger Dijkstra famously stated in 1969, testing can only reveal the presence of bugs and not the absence. This drawback is attempted tackled with methods such as property-based-testing, where test oracles are defined as a set of generalized properties, and used together with a randomized testing strategy that gradually attempts to narrow down the randomization to find errors that break the properties.[CH11].

3.1.3 Peer Reviews and Pair Programming

Another commonly applied method of verifying software, is through peer reviews or pair programming. Peer reviews, also known as code reviews, is a simple methodology where code written by one programmer is reviewed by another more experienced programmer who analyses the code for errors and maintainability. Pair programming, involves two programmers sitting together while developing the actual code.

The rationale behind both of these methods, is that drawing from the experience of more than just one developer when producing code will lead to more correct and maintainable software.

However, human verification is costly compared to automated verification, and is rarely enough to fully guarantee correctness in a system.

3.1.4 Model Checking

The last but not least important method of verification to be mentioned here, is model checking. Model checking first started out as a technique for verifying correctness in hardware systems, however it has slowly spread to the domain of software verification as well. Model checking is essentially about verifying a set of *temporal logic properties* by rigorously exploring the state space of a modeled system.

Model checking requires careful modeling of the subject system, since even a normal 32-bit integer in a program will expand the state space to search with a factor of 2^{32} , which quickly becomes very costly to verify. Therefore, to model check a system, it is necessary to distill and abstract the system into a simple model which still reflects the subject system but does so in a way that drastically limits the increase in state space to verify.

Model checking is the type of verification which is studied and described in this thesis work, with one of the motivations being that it is a verification method that promises a complete rigorous verification of the subject modeled system.

3.2 Model Checking

As previously mentioned, model checking is about verifying a set of properties in a system by exploring the state space of the given system. The challenge, however, is to derive a model which represents the behavior of the subject system but with less state space to explore.

Exploring the state space of most systems as they are, is in most cases infeasible. For example, verifying a program dependent on three 32bit integers, would alone require exploration of 2^{96} states. Even by using a computer system capable of exploring 93×10^{15} states per second, the endeavor of checking all these states would take more than 27000 years.³ To model check a system, it is therefore necessary to distill the behavior of the subject system into an abstract model which is able to represent the system with fewer states.

3.2.1 Deriving and Specifying Formal Models for Model Checking

In general there are two common methods of deriving such a model. One way is to use the informal description of the system requirements and behavior and formulate it in a formal language. And the other common way is to either automatically extract the model from an existing Software or Hardware implementation or manually derive a formal model through reverse engineering.

The model is typically specified in a formal model checking language as a set of functions, data types and a transition system which describes the behavior of the system and utilizes the defined functions and data types.

 $^{^3{\}rm The}$ Chinese super computer Sunway TaihuLight, has been bench marked to be able to perform 93 peta FLOPS (floating point operations per second).

3.2.2 Temporal Logic and Verification of Properties

A temporal logic language constitutes of the normal propositional description language (conjunctions, disjunctions and negations) which are used in describing the properties of a given state, and furthermore a set of temporal operators which are used in describing the transitions between the states. The most commonly used temporal languages used in model checking are LTL (Linear Temporal Logic), CTL (Computational Tree Logic) and CTL* which is a less restrictive superset of CTL.

The two most defining operators in temporal logic is the *eventually* operator typically denoted F and the *global* operator which is typically denoted G. The F operator is used to assert that a given property will hold true in some future state, while the G operator specifies that a given property must hold true in every state on a path.

The specified properties are often categorized into one of two categories, where the first is a type of safety property, and the second is a type of liveness property. Safety properties must hold true at all times, so those properties uses the Goperator, while the liveness properties must ensure some state eventually is obtained and thus uses the operator F. Since G is used to specify that something must hold true along all states in a path, it can be used specify that a set of properties which are critical for safety, must hold true at all times. Since the F operator is used to specify that some property eventually will become true, it can for example specify that some locked resource will be free again in the future such that a given process wont be waiting forever, and thus the property can be used to specify liveness.

3.2.2.1 Linear Temporal Logic (LTL)

LTL is the simplest of the three above mentioned temporal logic languages. It constitutes the temporal connectives G and F mentioned above and furthermore the connectives X ("next") and U ("until"). The next operator X specifies that the given proposition must hold true in the state following the current. The until operator U is an infix operator written as pUq where p, q are propositions, the until operator states that p must hold true in all states on the path until q is satisfied. LTL is called linear because the properties must hold over a linear path.

3.2.2.2 Computational Tree Logic (CTL)

The logic language of CTL consists of the same operators as in LTL, however CTL is a branching tree logic which means that it is possible to reason about the branches in the tree that unfolds when iteratively expanding all possible states from the transition model to a tree with the initial state as root. CTL therefore also specifies an existential quantifier E and an universal quantifier A. The existential quantifier E is used to specific that the given property hold true along at least one path in the unfolded state space tree, whereas the universal quantifier A specifies that the property must hold true along all branches. CTL is restricted such that any of the other temporal operators in the language must be preceded by a quantifying operator.

Following are illustrations of the various combinations of CTL operators in use.



Figure 3.1: EX(black) describes that there exists a path where the next state must be black. EG(black) describes that there exists a path where all the states must be black. AX(black) describes that for all paths the next state must be black. AG(black) describes that for all paths all the states must be black.



Figure 3.2: EF(black) describes that there exists a path where some future state must be black. $E(gray \cup black)$ describes that there exists a path where all states must be gray up to a black state. AF(black) describes that for all paths there exists some future state which is black. $A(gray \cup black)$ describes that for all paths all states must be gray up to a black state.

Chapter 4

The UMC modeling language

This chapter gives a brief introduction to the UMC modeling language[Maz09] and tool-set, which has been used in this project for modeling and verification. It might be useful to refer to Appendix B to get a complete picture of the grammar of the language, and to refer to Appendix C and Appendix D to see a concrete specification made with the language. This chapter solely aims at introducing the subset of the language which has been utilized in this project.

4.1 About UMC

UMC is a modeling language that seeks to make model checking more approachable to non-expert users. The language essentially enables a user to specify textual representations of UML state diagrams, and lends a part of its syntax to the way transitions are described in UML state diagrams.

The language has been designed to be a target language for a more high level language or graphical tool to generate. Therefore, the language itself has been implemented with very limited static type checking capabilities. This also means that the language, for example, doesn't have generalizing functions. The language is object oriented and enables the user to specify a set of generic classes and a set of object instantiations of the given classes. The classes encapsulates all mutation, such that the only way for objects to manipulate the state of another object is by means of synchronous *operations* or asynchronous *signals* which are queued up in an event queue for each object.

4.2 Structure and Semantics

A full UMC model description consists of a set of class definitions, a set of object instantiations and a set of abstractions. And an abstract skeleton of an UMC model looks as follows.

```
Class classname_1 is
...
end classname_1;
Class classname_n is
...
end classname_n;
Objects
objectname_1 : classname ...;
objectname_n : classname ...;
...
Abstractions {
   Action ... -> ...
   State ... -> ...
}
```

Following subsections describes the components presented above.

4.2.1 Class definitions

A class definition describes a set of synchronous *operations*, a set of asynchronous *signals*, a set of *variables*, a set of *states* and a set of state *transitions*. The skeleton of a class in UMC looks as follows.

```
Class classname is Signals
```

```
Operations

...

Vars

...

State ... = ...

Transitions:

State1 -> State2 { ... }

...

end classname;
```

The *signals* defines a set of asynchronous messages that can be send to the event queue of an object of the given class that defines the *signals*. A *signal* has a name and an arbitrary number of arguments that it caries along from the sender to the recipient. It is possible to define the types for the arguments, however, they are not statically type checked. The arguments carried along with a signal are simply treated as immutable values making it impossible for a recipient of a signal to manipulate variables of a sender.

The operations defines a set of synchronous operations to be invoked on an object of the given class. Just like the *signals*, the operations also defines a set of arguments, but furthermore does the operations also define a return value to be returned from the *transition* in the object they are invoked upon. Just as with the *signals*, the arguments carried along with an operation are treated as immutable values such that the recipient cannot mutate the state of variables on the sender object.

The *vars* defines a set of variables which are used to keep an internal state in an object of the given class. The variables can be integers, booleans, object references or arrays.

The *state* describes a set of modes that an object of the given class can be in. It is possible to define nested states and multiple nested states, however in this project only one layer of states has been used in each of the classes. Note that the first listed state automatically defines the initial starting state of the given class.

The *transitions* describes a set of transitions between the defined *states*. The *transitions* are described with a syntax similar to the syntax used to describe state transitions in UML state diagrams. The syntax for a *transition* looks as follows.

eventName[guardExpression]/action

Where the *eventName* is either an operation or a signal, which are said to, essentially, trigger the transition. The *guardExpression* is an expression that evaluates to a boolean value, where the expression can be composed of any of the class variables and arguments carried along with the triggering *signal* or *operation*. At last, the *action* is the action carried out when the *transition* is fired. An *action* in this context can be any composition of statements and typical imperative constructs such as if statements, for loops and while loop. The statements permit mutation of the state of the class variables, or sending out *signals* or invoking *operations* upon other objects. Note that if the triggering event is an *operation*, the action will end with a return statement returning whichever type the *operation* defines as return type. Even if the *operation* does not specify a return type, it will still have an implicit return value of zero. It is however valid to omit the return statement in the action, but in that case an implicit return statement returning zero will be executed at the end of an action when model checking the model.

In the expressions used as part of the statements or in the guards, it is possible to use the typical binary operators such as +, -, <, > and = for integers and logical and and logical or for booleans. Signals and operations are simply invoked on objects by suffixing the given object reference with .eventName where eventName is the name of the operation or signal to be invoked on the given object. Array indexes can be accessed and mutated through the classical square bracket notation array[index], however they can also simply be treated as lists by using the .head and .tail operations.

4.2.2 Object declarations

Once the classes has been defined, a set of *objects* can be declared from the classes. These *object* declarations essentially defines a concrete model, while the classes alone defines the generic model behavior.

The object declarations looks as follows.
Here the *object* attributes refers to the local *variables* declared on the given class. Note that it is possible to define default initial values for *variables* in classes, and in that case it is not necessary to specify any initial value for the given *variable* in the *object* instantiation.

4.2.3 Abstraction rules

An *abstraction* is essentially a construct that captures a given situation for the whole model. For example the situation where a variable on a specific object has a certain value, or the situation where a specific object is in a particular *state*.

The abstractions can be defined either as a state-abstraction or as an actionabstraction. State-abstractions captures a certain type of state in the model based on a conjunction of propositions that tests the variables or states of one or more of the defined objects. Action-abstractions captures the situation in the model where an operation or a signal are invoked or emitted. In this project only one action-abstraction has been defined, and that is an abstraction that captures the situation where the UMC model checker determines that a recipient of a signal or operation, has no handling for the given signal/operation for the current state of the receiving object. When the UMC model checker encounters such a situation, it will emit a lostevent signal on an implicit object called ERR. This particular action-abstraction has been very useful in the modeling process, where it helped track down states for which a given signal was not handled.

Note that the *state-abstractions* can only be defined as conjunctions. So if the user prefers to use a disjunction, he must exploit De Morgan's Law and specify the *abstraction* as a negation of a conjunction where all the conjunct propositions inside the conjunction are negated.

4.3 UCTL properties

Independently of the actual model, a set of *properties* can be specified in a UMC tailored modal logic syntax called UCTL, which defines the same modal logic operations as defined in CTL.

What is special for UMC and UCTL, is that the previously mentioned *abstractions* are used in the definition of *properties*.

The UMC modeling language

Chapter 5

An Engineering Concept of a Geographically Distributed Interlocking System

This chapter describes the engineering concept of the railway interlocking system which is to be modeled.

The system described is inspired by the idea of an interlocking system where the trains need to reserve their intended route before being permitted to traverse it and, with a distributed communication setup which is dependent on the geographical layout of the railway track circuits.

5.1 The overall idea

The fundamental purpose of the system, is to ensure that no two trains ever end up in a dangerous situation where they both occupy the same track. This situation is avoided by requiring that trains reserve their route before traversing it. To reserve a route, the train must gather *consensus* about the reservation from all the track elements which constitute the route.

In the described railway interlocking system, the network is composed of track elements, consisting of linear track segments and point segments which all are equipped with a track circuit type sensor.

The concept evolves around trains reserving routes through a two-phase commit protocol that attempts at collecting a consensus between the elements that composes a given route. Furthermore does the concept involve a sequential release mechanism for releasing reserved routes as they are traversed by the reserving train.

In the view of the consensus gathering protocol, the track elements assume the role of communication nodes which can be queried for reservation. Each node maintains a local state and is informed about relevant neighboring nodes as a route is reserved. The system is a distributed system, with all communication being propagated through the nodes based on their geographical relationships.

The following sections describes the two-phase commit protocol and the sequential release mechanism.

5.2 The Communication Scheme - Two-phase Commit Protocol

A two phase commit protocol, is a distributed consensus algorithm which coordinates a set of processes that all participate in the same distributed transaction. The protocol helps determine whether to *commit* or *cancel* a given transaction across a set of distributed processes. In the case of the geographically distributed interlocking system, the processes corresponds to the nodes in the railway network, and the agreed transaction is a route reservation for a given train.

The protocol requires an assigned coordinator responsible for initiating the commit, which for the given type of railway interlocking system corresponds to a train.

The protocol has two phases of message correspondences, each consisting of a *request* message being send out to all participating nodes and a *response* message being communicated back to the coordinator. In the case of the geographically

distributed interlocking system, the nodes are linked either virtually or physically in a sequential fashion corresponding to the given route. A request message is propagated through all participating nodes, and as the request reaches the very last node, the given node will initiate a *response* message to be propagated back through all the participating nodes.



Figure 5.1: Illustrating the concrete two-phase commit protocol used for route reservations. The *First Node*, *Intermediate Nodes* and *Last Node* represents the track elements in the system.

The **first phase**, commonly referred to as the "voting phase", starts with the coordinator sending out a *query* message which then is propagated through the network of nodes. The initial *query* message will contain details and data of what is to be committed. If all nodes *agree* to the *query*, the last node will initiate an *acknowledgment* message to be propagated back through the network. If, however, one of the nodes *disagrees* to the query, the disagreeing node will initiate a *negative acknowledgment* message to be propagated back to the coordinator.

In this phase, a node might choose to disagree if it detects the presence of a train on the track element, which is not the train that initiated the reservation request, or it might disagree simply because the given node already is involved in a reservation request initiated by another train.

The **second phase**, commonly referred to as the "completion phase", is usually initiated by the coordinator after receiving the *positive acknowledgment* message from the first phase. However, in the case of the geographically distributed interlocking system, the nodes are connected in a sequential fashion and the coordinating train has nothing new to add to the communication. Thus the immediate node following the train in the communication chain, will act as coordinator. Had the system been communicating in a distributed fashion without regards to geographical relationships between the nodes, then the messages would need to be communicated back to the original coordinator (the train). When the first node in the communication chain receives a *positive acknowledgment* message from the first phase, it immediately initiates a *commit* request, which informs the nodes to commit the awaiting transaction.

As each node receives the *commit* request it will prepare to enforce the transaction. If any node fails the conditions for performing the transaction it will emit a *disagree* message which is to be propagated out to all the nodes involved in the transaction. Upon receiving a disagree message, the nodes which have already committed the transaction will attempt a *rollback* to their previous states, and the nodes which have yet to commit will abandon the pending transaction.

In the case of the geographically distributed interlocking system, the *commit* message will cause the points on the route to apply the positioning requested for the given route. A *disagree* event will simply cause the nodes to abandon the pending reservation and go back to a non reserved state that indicates they are ready to receive new requests.

When the last node in the system has received the *commit* message, it will initiate an *agree* message to be propagated back through the nodes. When the first node, on which the train is located, receives the *agree* message, it will communicate an ok message back to the train.

5.3 Route Reservation

The individual nodes need not know the details of the track layout, instead the knowledge of the track layout can be either centralized and/or be known by the trains. In the conceived concept, the nodes are informed of their neighbors with regards to a specific route reservation. The initial route reservation request, which the train sends out, will contain an ordered list of the nodes involved in the route. As the reservation request is propagated through the network to the involved nodes, each node will record its neighbors for the given route.

However, the knowledge about routes in the system is not entirely enough, an overview of the railway network layout must still be duly maintained, and it is assumed that all routes has been verified against the current layout of the railway network.

Alternatively could the nodes be initialized or bootstrapped with knowledge about their immediate neighbors. This configuration would serve the purpose of rejecting impossible routes. However if the routes has already been verified against the concrete track layout prior to even attempting the reservation, then this interconnection check performed in the nodes is redundant and perhaps unnecessary.

One benefit of defining the interconnections between the nodes using routes instead of defining the interconnections statically and locally on the nodes themselves, is that it is easier to change the software representation of layout of the railway network, as the physical network changes over time, as an effect of maintenance work and extensions of the physical railway network.

5.4 Releasing the Reserved Track Segments - Sequential Release

To increase the usage and utility of the given railway track system, a sequential release mechanism can be implemented. The purpose of such a mechanism is to make reserved nodes *available* for other trains to reserve and use, as they are no longer needed by the original train which reserved them. As the individual track segments reserved for a given route, detects first the presence and then the absence of a train -they will go back into a state that defines them as available for new reservations.

The alternative to a sequential release mechanism would be to hold all nodes in a reserved state until the reserving train has reached its route destination. This, however, would reduce the availability of the track elements resulting in a poor usage of the network as a whole as the nodes will be held in a reserved state for a longer time than if they were released immediately after use.



Figure 5.2: Illustration of the sequential release mechanism for a train located at P1 and L2 with an original route from L1 to L2. Since the train is no longer occupying L1, the track is released.



Figure 5.3: The state transitions happening as the presence of a train is detected at a track element by its track circuit sensor, followed by detection of the absence of a train.

5.5 A Practical Implementation of the System

The linear track segments and points in the system would be equipped with track circuit sensors to detect presence or absence of trains. Furthermore can each of the linear segments and points be equipped with radio communication hardware to enable wireless communication with each other, and small processing units for maintaining state wrt. reservation status in the system and handling of the reservation negotiation protocol.

The train can likewise be equipped with radio communication hardware and a processing unit for handling the reservation negotiation protocol. At last, can the train processing unit be responsible for communicating the result of a reservation to the train operator.

For an implementation of the given system to be safe, it would have to somehow rule out human errors. A human train operator could accidentally miss a signal to stop and potentially create a dangerous situation by violating an already reserved route. The obvious way to counter this problem, would be to make the trains fully automated. However, the system could also be implemented with a mechanism in the trains that automatically breaks if it detects that it is about to violate a reserved track section. The protection against human errors could furthermore be enhanced by implementing flank protection, such that points neighboring a reserved route will position themselves to divert trains away from the reserved route.

At the software level, the overall implementation architecture would be a distributed system consisting of isolated processes, each with the responsibility of handling route reservation requests. At least three types of processes would be needed, one for the train, one for the linear track nodes and one for the point nodes.

5.6 Discussion

The core idea behind the presented concept, is that a route must be fully reserved before a train can traverse it, and since it is not possible for other trains to reserve segments of an already reserved route, this should very much prevent collision between trains. This, however, only holds true if either the trains are fully automated or if they implement some sort of fail-safe brake, since human operators potentially still can violate reserved routes.

An important motivation for making the interlocking system distributed instead

of centralized, is that it allows on of smaller subsets of the network to be verified independently, as also discussed in [Fan12]. In contrast, changes made to a fully centralized system where everything is highly interdependent, requires the whole network to be verified, which can be quite costly with regard to computational resources, -especially for large networks.

The concept could be extended to support reservations of partial routes or even moving block reservations. However this would require a lot more work to be done with regards to ensuring liveness in the system, in order to avoid trains ending up in deadlock situations. By fully reserving a route and only permitting trains to traverse they have reserved, it is trivial to check the system with regards to liveness.

Chapter 6

Modeling the Geographically Distributed Interlocking System in UMC

This chapter describes the modeling of the Geographic interlocking system described in the previous chapter. The model specifically models the two-phase commit protocol for reserving train routes, and the physical movement of the trains over their respective routes in the railway network layout.

6.1 Defining the Model in UMC

The geographically distributed interlocking system has been specified in the UMC modeling language with initial inspiration drawn from a model originally specified by the student Marco Paolieri from University of Firenze[Pao10].

The model consists overall of the three types of components modeled in UMC classes. The classes constitutes a Train class representing trains, a Linear class representing linear track segments and a Point class points. Each of the UMC classes contain a set of variables, a set of incoming signals, a set of class-states

and a set of state transition definitions. Essentially, it is the state transitions which reflects the behavior of a given component.

The Point class and Linear class each basically models a track element communication node and a physical track circuit sensor, while the Train class models the communication node in a train and the trains physical movement across its route in the railway network.

All the components are modeled such that it is possible to define physical lengths as abstract discretized length units. The purpose of this, is to be able to model situations where a train overlaps multiple track elements, and specifically model train movement transitions over neighboring track segments. All elements use the same abstract unit length, and the train movement is modeled such that a train moves in discretized steps of one unit in each movement step. At all times, the model keeps track of the location of each section that makes up the length of each train in order to model the movement of the trains across multiple segments in the railway network.

The actual use of the classes is described in the next chapter, which describes a tool for instantiating the objects to compose a full model based on the classes.

This section informally describes the specification details of the generic classes and their signals, variables, state transitions and behavior.

Note that the full source code for the following described classes can be found in Appendix C.

6.1.1 The Train Class

The Train class models the behavior of a train in a railway system with a geographically distributed interlocking system. The train is responsible for reserving its own route by sending out a reservation request message, and simulates moving through its route by keeping track of its own position on the route and invoking operations on the track element nodes that it passes on its route.

The Train class supports trains of varied lengths and models the movement of the train such that it is possible for a train to partially cover a track element or even cover multiple track elements.

6.1.1.1 Variables

The train contains *variables* describing its route and for keeping track of its exact position on the route.

- *requested_point_positions* is an array of Boolean values that describes the required position of each point on the route of the train.
- *train* length is an integer value that determines the length of the train.
- *route_segments* is an array of object references containing references to the track element nodes constituted by communication nodes representing the linear track segments and point segments.
- *route_index* is an integer that indicates how far in the route the train has traveled. The value corresponds to an index in *route_segments*.
- *occupies* is an array of object references. The array has same length as the train and contains references to the nodes which the train currently covers with its length.
- *front_advancement_count* is an integer variable which describes the current location of the front of the train within the track segment that the train currently occupies.
- track_lengths is an integer array which describes the lengths of the track segments contained in route_segments. The two arrays track_lengths and route_segments corresponds index-wise.

6.1.1.2 Incoming signals and outgoing signals

The Train class exposes two signals which can be send to the instantiated train objects.

- a no signal indicating rejected reservation of its route.
- an *ok* signal indicating successful reservation of its route.

Only one signal is ever emitted from the objects of the Train class, and that is the initial reservation request signal denoted *req*. The *req* signal has the signature

req(sender, route_index, route_segments, req_point_configurations)

where the variables are described as

- *sender* which is a reference to the train itself.
- *route_index* which is used as an index for the *route_segments* array, and is set to a value of zero with the initial request from the train to refer to the first element of the route.
- *route_segments* which is an array containing references to the track elements and points on the route of the train, which constitutes of linear track segments and point track segments.
- *req_point_configurations* which is an array of boolean values indicating the required position of each of the points along the route.

Besides sending and receiving signals, the train also invokes *sensorOff* and *sensorOff* operations on objects of the *Linear class* or *Point class*.

The received and emitted signals and operations of the objects of the *Train* class, are illustrated below.



Figure 6.1: The incoming and outgoing signals and operations of objects of the *Train class*.

6.1.1.3 States

The train class has following *states*

- *READY* which denotes that the train is ready to perform a reservation.
- WAIT_OK which denotes that the train has send out reservation request for a route and is awaiting response.
- *MOVEMENT* which denotes that the train is currently moving over its route in the network.
- ARRIVED which denotes that the train has arrived at its destination.

6.1.1.4 State transitions

Below is a state diagram illustrating the *states* and *transitions* between the *states*. In the diagram, the *transitions* has been simplified as much as possible to improve readability, notably a set of aliases has been declared at the bottom. After the diagram follows a set of high level descriptions of the *state transitions*.



Figure 6.2: State diagram for the *Train class*. The diagram follows the UML convention for state diagrams, where each transition is labeled with "eventName [guardExpression] / action", where eventName in this case is an incoming signal, guardExpression, is the requirement to be able to take the transition and action is the action performed when the transition is taken. The symbol - signifies absence or empty statement.

READY -> WAIT OK

Requires: -

Effect: Sends the initial request to the first node in the route of the train.

WAIT $OK \rightarrow READY$

Requires: The train has received the signal *no*. **Effect:**

The train has received a rejection signal for its reservation request and goes back to its READY state.

WAIT OK -> MOVEMENT

Requires: The train has received the signal *ok*.

Effect:

The train has received the final acknowledgment which indicates that the full reservation of its route has been completed successfully, and therefore transitions into the MOVEMENT state.

MOVEMENT -> MOVEMENT

Requires: The train has not reached the end of the final node on its route. **Effect:**

The train is traversing the track elements on its route and is triggering track circuit sensors as it traverses over the track elements on the route. At each transition the train determines if it has reached the end of a track, by evaluating whether or not the front of the train has reached the end of the length of the current track it occupies. When the front of the train moves into a new track segment, it triggers the the track circuit by invoking the *sensorOn* operation on the given track element. When the rear of the train leaves a track segment, it triggers the track circuit sensor off, by invoking the *sensorOff* operation on the given track element.

At each transition the *occupies* array is updated to reflect which track segments the train covers. The head of the *occupies* array represents the rear of the train and the last element of the array represents the front of the train.

The algorithm used for train movement is presented below in the UMC language with comments in *italics*. Furthermore, to understand the flow of the movement better, it might be beneficial to refer to the Scenario section later in this chapter, where a concrete example is explained in details.

Listing 6.1: Train Movement Transition

$MOVEMENT -> MOVEMENT \{$

```
[not (route index = route segments.length -1 and
 track lengths [route index] -1 = front advancement count)] /
    - - determine if we have reached the end of the current track
    at end of track: bool :=
      track lengths [route index] - 1 = front advancement count;
    if at end of track = true then {
      front advancement count := 0;
       - - if the route index is not the last of the route segments array
      if route index < route segments.length -1 then {
        - - the train enters the next track on the route
        route index := route index + 1;
        - - modeling that the track circuit sensor on the next track detects the train
        route segments [route index].sensorOn(self);
      };
    } else {
      front advancement count := front advancement count + 1;
    };
    - - update the occupies array
    rear: obj := occupies.head;
```

```
next_rear: obj := occupies.tail.head;
occupies := occupies.tail + [route_segments[route_index]];
- if the rear of the train has left a track segment
if rear != next_rear then {
    - modeling that the past track circuit sensor detects absence of the train
    rear.sensorOff(self);
};
```

MOVEMENT -> ARRIVED

Requires: The train has reached the end of the length of the final track element on its route.

Effect: The train has successfully traversed its route and has reached its destination.

6.1.2 The Linear Class

The *Linear class* models the behavior of a *node* representing a linear track segment equipped with a track circuit sensor. The class models the receival and forwarding of of route reservation negotion messages, and models track circuit sensor responses to a train that's moving across its length.

6.1.2.1 Variables

The *Linear class* contains *variables* describing its immediate neighbors relative to a reserved route, a reference to the train currently occupying the linear track segment, and the length and amount of free capacity of the linear track segment.

- *next* is an object reference to the next neighboring track segment or point on a reserved route. The variable is *null* when the node is in the non reserved state.
- *prev* is an object reference to the previous neighboring track segment or point on a reserved route. The variable is *null* when the node is in the non reserved state.
- *train* is an object reference to the train which is currently occupying the node. This variable is *null* if no train is occupying the node.

6.1.2.2 Incoming and outgoing signals and operations

Incoming signals

The *Linear class* describes a set of *signals* involved in negotiating a full route reservation between the nodes representing the track segments in the network. These signals are:

- *req* which is a reservation request, with the same parameter signature as the *req* signal described under the *Train class*.
- *ack* which is an acknowledgment signal send in response to a request.
- $\bullet\ nack$ which is a negative-acknowledgment signal send in response to a failed request.
- *commit* which signifies a request for the current reservation to be enforced.
- *agree* which is an acknowledgment signal send in response to a commit signal.
- $\bullet\ disagree$ which is a negative-acknowledgment signal send in response to a failed commit.

Operations

The class specifies two *operations* which are invoked by other objects:

- *sensorOn* which is an *operation* invoked by a *Train class* object. This *operation* models that a sensor has been triggered on by a train when it moves onto the track.
- *sensorOff* which is an *operation* invoked by a *Train class* object. This *operation* models that a sensor has been triggered off by a train when it leaves the track.

The sensorOn and $sensorOf\!\!f$ operations, essentially models the triggering of a track circuit sensor.

Outgoing signals

The outgoing signals are the same as incoming signals, but also includes the train $signals \ ok$ and no.

The incoming and outgoing signals and operations are illustrated below.



Figure 6.3: The incoming and outgoing signals and operations of objects of the Linear class, with signals colored black and operations colored blue.

6.1.2.3 States

The *Linear class* contain following states:

- NON RESERVED which denotes that the given node is currently free.
- WAIT_ACK which denotes that the node has received a reservation request and now is awaiting an *ack* response message from the first acknowledgment phase of the two-phase commit protocol.
- WAIT_COMMIT which denotes that the node is awaiting a *commit* request message from the second phase of the two-phase commit protocol. In this state, the node is ready to prepare the enforcement of the reservation.
- WAIT_AGREE which denotes that the node is awaiting an *agree* response message from the second acknowledgment phase of the two-phase commit protocol. In this state the node is ready to enforce the reservation in the case of consensus among all the nodes.
- *RESERVED* which denotes that a reservation has been enforced, and therefore the node is currently reserved. The node is thus ready for the reserving train to traverse over the track segment associated with the node.
- *TRAIN_IN_TRANSITION* which denotes that a train is currently moving on the track segment associated with the node.

6.1.2.4 State transitions

The set of state transitions involving the states NON_RESERVED, WAIT ACK, WAIT COMMIT, WAIT AGREE and RESERVED, triggered

by the signals *req*, *ack*, *commit* and *agree*, basically describes the behavior of the two-phase commit protocol. In these transitions, an incoming signal is either passed along to a neighboring node, or a new phase of the two-phase commit protocol is started when the node is either first or last on the route.

The transitions involving the states NON_RESERVED, WAIT_ACK, WAIT_COMMIT, WAIT_AGREE and RESERVED, triggered by the signals nack and disagree, describes the behavior of the two phase protocol when a route reservation fails. A route reservation is successful if no other trains are occupying any of the track segments along the route, and when all the track elements on the route are involved in the same two-phase commit protocol. On the other hand, a route reservation fails if another train is occupying one of the track elements on the route, or when another train has already engaged one of the track element nodes in a reservation request.

The transitions involving the states *TRAIN_IN_TRANSITION*, *RESERVED*, and *NON_RESERVED* triggered by the operations *sensorOn* and *sensorOff*, describes the movement of a train over the track segment. The transitions also models the *sequential release behavior* of a track segment, where a train first enters a reserved track segment triggering the track circuit sensor on, and then leaves the track segment triggering the track circuit sensor off causing the given track element to be free and non-reserved again.

To give an overview of the state transitions, a state diagram of the *Linear class* is presented below.

Following the diagram, are the individual state transitions described informally.



Figure 6.4: State diagram for the *Linear* class. The diagram follows the UML convention for state diagrams, as also described in the figure for the Train state diagram. Furthermore is it important to note that the diagram omits descriptions of the actual performed actions for brevity.

NON RESERVED -> WAIT ACK

Requires: a received request where the sender must be the train currently occupying the track segment.

Effect:

The current track element node has received an initial route reservation request. The *next* variable is updated based on the route information and the request is forwarded to the track element node on the route.

NON RESERVED -> WAIT ACK

Requires: a received request with a route where the current track element is not the first or last.

Effect:

The *next* and *prev* fields are updated in the current node based on the route information provided with the reservation request. The request is forwarded to the next track element node on the route.

NON RESERVED -> WAIT COMMIT

Requires: a received reservation request with a route in which the current track element is the last.

Effect:

The prev variable is updated with the route information, and an ack signal is send to the previous track element node on the route.

WAIT ACK -> WAIT COMMIT

Requires: an *ack* signal has been received, and the current node is not the first track element node on the route, which is verified by checking that the *prev* variable is *not null*.

Effect:

An *ack* signal is passed on to the previous track element node on the route.

WAIT ACK -> WAIT AGREE

Requires: an *ack* signal has been received and the track element node is the first on the route, which is verified by checking that the *prev* variable is *null*. **Effect:**

A *commit* signal is passed on to the next track element node on the route.

WAIT COMMIT -> WAIT AGREE

Requires: a *commit* signal has been received and the track element node is not the last on the route, which is verified by checking that the *next* variable is *not null*.

Effect:

A commit signal is passed on to the next track element node on the route.

WAIT COMMIT -> RESERVED

Requires: a *commit* signal has been received by the current node, and the track segment it represents is the last element on the route, which is verified by checking that the *next* variable is *null*.

Effect:

An agree signal is send to the previous track element node on the route.

WAIT AGREE -> RESERVED

Requires: an *agree* signal has been received by the current node, and the track segment it represents is not the first on the route, which is verified by checking that the *prev* variable is *not null*.

Effect:

An agree signal is send to the previous track element node on the route.

WAIT AGREE -> TRAIN IN TRANSITION

Requires: an *agree* signal has been received by the current node, and the track segment it represents is the first on the route, which is verified by checking that the *prev* variable is *null*.

Effect:

An ok signal is send to the train, indicating that the route has now been successfully reserved.

RESERVED -> TRAIN IN TRANSITION

Requires: a sensor on registration which is triggered by a train object invoking the *sensorOn* operation on the current track element, modeling the triggering of a track circuit.

Effect:

The train variable is set to the value of the sender of the operation.

TRAIN IN TRANSITION -> NON RESERVED

Requires: a sensor off registration which is triggered by a train object invoking the *sensorOff* operation, modeling that the track circuit sensor goes from registering presence of a train to registering absence.

Effect:

This transition models the sequential release functionality, releasing the node as the train leaves it by setting its *train* variable to *null*.

WAIT ACK -> NON RESERVED

Requires: a *nack* signal has been received. **Effect:**

Enect:

If the represented track segment is the first on the route, then a *no* signal is send to the train which is occupying the track segment, else a *nack* signal is send to the previous track element node on the route.

Since the node was awaiting an ack signal, and since ack signals are send in the direction of the *prev* node, the current node only need to forward the *nack* signal in that direction.

WAIT COMMIT -> NON RESERVED

Requires: a *disagree* signal has been received.

Effect:

If the represented track segment is not the last on the route, then a *disagree* signal is send to the next node on the route.

Since the node was awaiting a *commit* signal which are send in the direction of the *next* node, it must forward the *disagree* signal in that direction. It is furthermore, only possible for *disagree* signals to occur in the second phase of the two-phase commit protocol, and therefore the *disagree* signals only need handling for the transitions relevant to this part of the phase.

WAIT AGREE -> NON RESERVED

Requires: a *disagree* signal has been received. **Effect:**

If the current node represents the first track segment on the route, then a *no* signal is send to the train which is occupying the track segment represented by the node, else the *disagree* signal is forwarded to the previous track element node on the route.

RESERVED -> **NON_RESERVED**

Requires: a *disagree* signal has been received. **Effect:**

If the node represents a track segment which is not the last, then a *disagree* signal is send to the next node on the route.

NON RESERVED -> NON RESERVED

Requires: a *req* signal has been received, but a train is already occupying the track segment, and the sender of the request is different from the train which is occupying the track segment.

Effect:

A nack signal is send to the sender of the request signal.

WAIT_ACK -> WAIT_ACK, WAIT_COMMIT -> WAIT_COMMIT, WAIT_AGREE -> WAIT_AGREE, RESERVED -> RESERVED, TRAIN_IN_TRANSITION -> TRAIN_IN_TRANSITION Requires: a request signal has been received. Effect:

The node is already in the process of being reserved, so it sends a nack signal to the sender of the request.

6.1.3 The Point Class

The *Point class* is very similar to the *Linear class*. However, the *Point class* deviates from the *Linear class* because points only can be intermediate nodes on a route, and also because they model the track switching behavior of a point in a railway system. Although the nodes representing points are very similar to the nodes representing linear track segments, the points are required to be in correct position before they can agree to a given reservation. If a positioning of a point *fails* it will emit *disagree* signals to both its neighbors to communicate that the reservation has *failed* and that the current reservation should be canceled.

6.1.3.1 Variables

The $Point\ class$ defines the same variables as the $Linear\ class,$ but with two additional variables which are

- *requested_position* which is a Boolean variable that indicates a requested position for the point for a specific train route.
- *current_position* which is a Boolean variable that indicates the current positioning of the point. A value of True is to be interpreted as a *plus* positioning, and a value of False as a *minus* positioning.

6.1.3.2 Incoming signals, Operations, Outgoing signals

The incoming signals, operations and outgoing signals are the same as for the *Linear class*, with the only exception being that no point will ever communicate directly with a train in the reservation process, so no *ok* or *no* signals are ever sent from points.



Figure 6.5: The incoming and outgoing signals and operations of the objects of the Point class. With signals colored black and operations colored blue.

6.1.3.3 States

The states are the same as for the *Linear class* including an additional state POSITIONING, which indicates that a point is currently performing a positioning switch between tracks, and a state *MALFUNCTION* which indicates that the current point has malfunctioned.

6.1.3.4 State transitions

The set of state transitions are almost identical to the state transitions in the *Linear class*, besides the fact that only transitions relevant for intermediate nodes on a route are implemented, and additional state transitions for the *PO-SITIONING* state are defined, and a transition for the *MALFUNCTION* state has been added.

To give an overview of the state transitions for the *Point class*, a UML state diagram is presented below. The additional transitions for *Point class* are informally described after the diagram.



In_position := current position = requested position

Figure 6.6: State diagram for the *Point* class. The diagram follows the UML convention for state diagrams, as described under the Train class state diagram. Furthermore does the diagram abstract away the actual actions taken in the transitions, and defines an alias In_position of a proposition that tests the current positioning of the point against the requested positioning.

WAIT AGREE -> POSITIONING

Requires: the node representing the point has received an agree signal, but

the requested positioning is different from the current positioning of the point. **Effect:** The point goes into the *POSITIONING* state.

POSITIONING -> **RESERVED**

Requires: -

Effect: The positioning is successfully performed. The point sends an *agree* signal to its previous neighbor.

POSITIONING -> **MALFUNCTION**

Requires: -

Effect: The point malfunctions while performing the positioning. It emits *disagree* signals to both its neighbors indicating that the current reservation should be canceled.

POSITIONING -> **POSITIONING**

Requires: the node representing the point has received a *req* signal. **Effect:**

The point is currently busy performing its positioning, and therefore the reservation request must be rejected. The node representing the point, sends a *nack* signal to the sender of the request.

6.2 Model Properties

The whole purpose of formally specifying the system, is such that it can be model checked for certain relevant properties. In the case of an interlocking system, the properties of main interest are safety properties. These properties specifies the most critical situations that must be be avoided in the system, no matter what scenarios it is exposed to over its operational time. The two most important safety properties to verify for an interlocking system, is the *no derailment property* and the *no collision property*.

It can also be relevant to check the system for *liveness* or *progress* to verify the absence of deadlocks between trains or messages. However, the modeled system in this project also models possible malfunctions of points, and thus a simple global check for progress in the model would fail, since a malfunction would prevent the trains from passing the malfunctioning point. However, it is still relevant to verify that the system allows the trains to reach their destinations when no malfunctions occur, and thus a *progress* property is defined which verifies the arrival of trains for the state path branches where no malfunction has occurred.

Properties can also be used as a debugging tool and for verifying the consistency of a model. A property which checks for consistent handling of all signals in the model, is an example of such a property. This type of property is mainly of interest as a tool to spot modeling mistakes while deriving the generic model, and to verify modeling assumptions.

Following sub sections describes the individual properties which are verified for a concrete model. Specifically when using UMC as modeling tool, it is possible to define *abstractions* which is a language construct for captures a given situation in the system. These abstractions are core components when specifying model properties in UMC. In this section, each property is formally described together with its associated abstractions.

6.2.1 No Collision

The *no collision property*, is a safety property specifying that no two trains must ever be able to occupy the same space on the modeled railway network. For the modeled trains with discretized lengths, this means that no parts of any two trains must ever be present at the same track segment at the same time.

The *Train class* specifies an array *occupies* which has the same length as the discretized length of the train, and is maintained with references to the track elements which the train occupies when traversing its route. The *occupies* array thus keeps track of the full location at all times for the given train. To verify that no parts of any two trains are ever at the same track segment, it is necessary to check that there is no intersection between the track segments which the two trains occupies.

The no collision property uses an abstraction trains_at_diff_positions, which captures the situation in the model where there is no intersection between any two trains.

The trains_at_diff_positions abstraction can be formally described with the following predicate, which is a conjunction over all pairs of trains (t1,t2) in the system.

$$\bigwedge_{(t1,t2)\in TrainPairs} \left(\bigwedge_{i\in I, j\in J} t1.occupies[i] \neq t2.occupies[j]\right)$$

where $I = \{i | 0 \le i < t1.length\}$ and $J = \{j | 0 \le j < t2.length\}$, and TrainPairs

is the set $\{(t1, t2)|t1 \in trains \land t2 \in train \land t1 \neq t2\}$ where trains is the set of all trains in the system.

The *no collision* property simply verifies that the above abstraction is valid globally over all paths.

no collision

AG (trains_at_diff_positions)

6.2.2 No Derailments

The *no derailment property*, is a safety property which specifies that no train must occupy a point which is in progress of performing a mechanical positioning between track segments. In a real life situation if a train were to traverse over a point while the point were performing the mechanical switch, a derailment of the train might occur.

This property requires two types of abstractions. It uses a set of abstractions that specify that a given point is in its positioning state, and a set of abstractions that specify detection of a train on the individual points.

A set of abstractions specifying the absence of trains at points is defined as follows:

For all points p, an abstraction $no_train_on_p$ is defined as follows:

State p.train = null

The set of abstractions capturing the situations where a point is positioning is formally expressed as follows:

For all points p, an abstraction *positioning* p is defined as follows:

```
inState(p.POSITIONING)
```

The property can now be defined using the $no_train_on_p$ and $positioning_p$ abstractions:

no derailment

$$\operatorname{AG}(\bigwedge_{p \in points} positioning_p \implies no_train_on_p)$$

where *points* is the set of all points in the system.

When checking this property, a claim could be made that the given property only checks whether or not a train is *detected* on a point while its positioning. To strengthen the claim of the property, another property can be defined to validate that at all times when a train is present on a point it is correctly detected by the point.

To create this property, an abstraction capturing the state where a given train is occupying a specific point, must be specified. The abstraction can be defined as a disjunction over the train parts, where each predicate component checks if the given train part is equal to the given point.

For each pair (t, p) in the set $\{(t, p)|t \in trains \land p \in points\}$ where trains is the set of all trains and points is the set of all points in the system, the abstraction t on p is formally defined as follows:

$$\bigvee_{i \in \{0...t.\text{length}-1\}} t.\text{occupies}[i] = p$$

Using the abstractions $no_train_on_p$ and t_on_p , the property for verifying the triggering of sensors on points, can now be formally defined as:

$$\begin{array}{c} \text{Trains correctly detected at points} \\ \text{AG} \left(\bigwedge_{(t1, t2, p)} (t1_on_p \lor t2_on_p) \implies \neg no_train_on_p \right) \end{array} \right)$$

where (t1, t2, p) is a triple from the set $\{(t1, t2, p) | t1 \in trains \land t2 \in trains \land t1 \neq t2 \land p \in points\}$ where trains is the set of all trains and points is the set of all points in the system.

This property essentially validates the claim that the points always detects the presence of trains.

In the current model, the trains are always detected, but if the model were to be extended to also model sensor failures, then the *no derailment* property would have to use the $t_{on}p$ abstraction.

6.2.3 Progress property - arrival of all trains at their destinations

It is not enough to verify that a model is safe. For the model to be of any use, it should also be verified that the trains will progress to reach their destinations in the modeled network. This is both to verify that the generic model is specified correctly, and to verify that the trains in a concrete model doesn't just end up being stuck in a deadlock preventing them from reaching their destinations. Since the generic model models the event that a point may malfunction during the run, the property for verifying arrival of trains must disregard these states.

A simple property can be defined for checking if there is any possibility that the trains will arrive at their destinations. This property simply uses a set of abstractions that captures the situation where each of the trains has changed state to ARRIVED.

A set of abstractions $t_{arrived}$, specifying the arrival of a train t at its destination, can be formally defined as follows:

For each train t in *trains* an abstraction t arrived is defined as

State: inState(*t*.ARRIVED)

where *trains* represents the set of all trains in the system.

The property can now be defined formally as

Will arrive

$$EF \ AG\left(\bigwedge_{t \in trains} t_arrived\right)$$

With this property it is possible to show that there eventually exist a state in the system in which all the trains have arrived.

However of interest to know in which cases the trains doesn't arrive. The malfunctioning of points is supposedly the only thing that should be stopping the trains from arriving, -disregarding the specification of models with routes that creates deadlocks.

To prove that the malfunction is the only thing stopping the trains from arriving, abstractions for capturing the malfunction states are needed.

For each point p, an abstraction p malfunction is defined

State: inState(*p*.MALFUNCTION)

For the property, what informally needs to be verified, is that there do not exist a state-path to a *final* state where it is *not* the case that both of the trains have *not* arrived and *until* (up to) this final state there has been *no* malfunctions in the points.

Defining the property for verifying the claim, can be done using the CTL construct "until" (U) and the special UMC language construct "final" which denotes a state from which there are no more possible transitions to take.

no malfunctions when trains hasn't arrived $\neg E \left[\neg \left(\bigvee_{p \in points} p_malfunction \right) U \left(final \land \neg \left(\bigwedge_{t \in trains} t_arrived \right) \right) \right]$

6.2.4 No message loss

Messages are an important part of the modeled distributed system, and it is therefore of interest to know whether or not all messages are handled for all possible cases. Being able to verify this, has been a great help when defining the generic model, and has helped in tracking down unhandled signals.

The UMC model checker triggers a special *lostevent* action on a special *ERR* object, when an object is incapable of handling an incoming signal in its current state. This action can be captured with an *Action* abstraction *discarded message*, and can be defined directly in the UMC language as follows

Action: lostevent -> discarded_message

The property for checking for lost messages, can be defined using the UCTL "next" construct. With this construct, a property can be defined which verifies that for all state-paths it will never hold that a message is discarded during a transition from a state to a next state.

The property can be directly specified in UMC as follows

no message loss

AG not (EX discarded message true)

6.3 Scenarios

To give an idea of how the system functions with regards to movement of the trains and the reservation through the two phase commit protocol, a set of scenarios are described and illustrated in this section.

Each scenario is illustrated with a drawing indicating the intended routes of one or more trains, next the events playing out during the scenario are illustrated through a sequence diagram with state transitions indicated at the relative time they occur.

6.3.1 A Successful Route Reservation

A successful reservation involves a train which sends out a request to reserve a specific route in the railway network. In the following scenario, the train *train1* sends out a request to reserve the route composed of the track segments L1, L2 and the point P1. In this scenario the point P1 is already positioned correctly in relation to the route reservation. A simple drawing of the scenario setup is presented below.



Figure 6.7: A scenario of a successful reservation of a route composed of the linear track segments L1, L2 and the point P1. Both the linear elements have a length of two, the point have a length of one and the train a length of two.

The full two phase commit reservation is illustrated in the sequence diagram below.



Figure 6.8: Sequence diagram of a successful reservation of a route composed of the linear track segments L1, L2 and the point P1.

6.3.2 A train traversing its successfully reserved route

In the current scenario the traversal of the route reserved in the previous scenario, is illustrated and described.

The movement of a train when it traverses its route in the model is rather involved, and a lot of things is going on, therefore the sequence diagram for the movement is followed up by a textual description commenting on the events playing out.


Figure 6.9: Sequence diagram of the events playing out as train1 traverses its reserved route composed of the linear track segments L1, L2 and the point P1.

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```
1. train1: WAIT OK -> MOVEMENT
```

The train object initializes its $front_advancement_count$ variable to reflect where the front of the train is located on the sub-segments of the current linear track (L1). The $front_advancement_count$ counts index values from zero and the the train has a length of 2, and thus the $front_advancement_count$ is initialized to a value of one.

2. train1: MOVEMENT -> MOVEMENT

The front of the train enters the next track segment on its route, which is P1. During this transition, a *sensorOn* operation is invoked on P1.

It is determined by the value of the $front_advancement_count$ that the train has reached the end of L1, and therefore the variable $route_index$, which reflects the trains position in relation to its route, -is incremented to a value of one.

Since the train has entered a new track segment and the front of the train now is located at the beginning *P1*, the *front_advancement_count* variable is updated to a value of zero to reflect this.

The sensor On operation on the point P1 is invoked, and when the operation returns, the *occupies* array is updated to [L1,P1] such that it now reflects that *train1* is occupying L1 and P1.

3. P1: RESERVED -> TRAIN_IN_TRANSITION train1 is detected at P1, which is emulated by the invoked sensorOn oper-

train 1 is detected at P1, which is emulated by the invoked sensor On operation. P1 updates its train variable to reflect that train 1 now is occupying the point.

4. train1: MOVEMENT -> MOVEMENT

The front of train1 enters L2 and the rear of train1 leaves L1. During this transition, operations are invoked by train1, on L2 and on L1.

Since the front of the train has entered a new track segment, the *front_advancement_count* variable is updated to a value of zero. Likewise, the *route_index* variable is incremented to a value of two which, through its route array, reflects that the train now is at *L2*.

train1 invokes the sensorOn operation on L2, and when the operation returns, the occupies array is updated to reflect that train1 now covers P1 and L2. After that, train1 invokes the sensorOff operation on L1.

- 5. L2: RESERVED -> TRAIN_IN_TRANSITION train1 is detected at L2. The train variable is updated to reference train1 to reflect that a train is now occupying L2.
- 6. L1: TRAIN_IN_TRANSITION -> NON_RESERVED The absence of train1 is detected, emulated by the invoked sensorOff operation on L1. Since the model models a system with sequential release, L1 is released by setting the variable train to null and by entering a NON RESERVED state.

- 7. train1: MOVEMENT -> MOVEMENT The front of train1 advances over L2 and the rear of train1 leaves P1. During this transition, an operation is invoked by train1, on P1. The advancement of the front of the train on L2, is reflected in the model by incrementing the front_advancement_count variable to a value of one. The occupies array is updated to a value of [L2,L2] to reflect that train1 now only occupies L2.
- 8. P1: TRAIN_IN_TRANSITION -> NON_RESERVED The absence of train1 is detected, emulated by the invoked sensorOff operation on P1. P1 is released, which is reflected in the model by setting the train variable to a value of null and by entering a NON_RESERVED state.
- 9. train1: MOVEMENT -> ARRIVED The train has arrived at its final destination.

6.3.3 Point positioning during reservation

During a reservation of a route, points must be positioned correctly in relation to the reserved route, before the route can be fully reserved. In the following scenario, the point P1 is positioned such that it connects L1 and L2, however the wished route requires the point to be positioned such that it connects L1 to L3. A simple drawing of the scenario setup is presented below.



Figure 6.10: A scenario of where a positioning of the point P1 occurs during reservation a route composed of the linear track segments L1, L3 and the point P1.

To simplify the diagram, only the second phase of the two phase commit protocol has been drawn, since this is where the positioning occurs.

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Figure 6.11: Sequence diagram of a scenario where a positioning of the point P1 occurs during the reservation of a route composed of the linear track segments L1, L3 and the point P1.

6.3.4 Point malfunction during reservation

During the reservation of a route, a point might malfunction which consequently causes the route reservation to *fail*. In the following illustrated scenario, the train *train1* attempts to reserve a route consisting of the track segments [L1, L2] and the point P1, however the point P1 is positioned such that it doesn't connect to L2 and therefore it must first be positioned, before the route can be *successfully* reserved. The point therefore enters its positioning state during

the reservation process, but fails to perform the mechanical track switching and therefore emits disagree signals to its neighbors to signal that the reservation should be aborted. A simple drawing of the scenario setup is presented below.



Figure 6.12: A scenario of a malfunctioning point P1 during reservation a route composed of the linear track segments L1, L2 and the point P1.

To simplify the diagram, only the second phase of the two phase commit protocol has been drawn, since this is where the malfunctioning can occur.

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Figure 6.13: Sequence diagram of a scenario where the point P1 malfunctions during the reservation of a route composed of the linear track segments L1, L2 and the point P1.

6.3.5 Attempt to reserve a route intersecting with an already reserved route

If a requested route reservation intersect with an already reserved route, the requested route reservation must be aborted. In the following illustrated scenario, the train train2 has successfully reserved a route composed of the linear track segments L1, L3 and the points P1, P2. The train train1 now attempts to reserve the route consisting of the linear track segments L2, L4 and the points

P1, P2, however the route intersects with the already reserved route at P1 and P2, and must therefore be aborted.



Figure 6.14: A scenario of an attempt to reserve a route that intersects with an already reserved route, where the attempted reservation is a route composed of the linear track segments L1, L3 and points P1, P2, and the already reserved route is composed of the linear track segments L2, L4 and the points P1, P2.

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Figure 6.15: Sequence diagram of a scenario of an attempt to reserve a route that intersects with an already reserved route, where the attempted reservation is a route composed of the linear track segments L1, L3 and points P1, P2, and the already reserved route is composed of the linear track segments L2, L4 and the points P1, P2.

6.4 Discussion

The developed model, does a good job at modeling the conceived engineering concept presented in the previous chapter, by itself. But improvements can still be made to make the model reflect a real implementation better and to make the model checking more efficient. Especially can constraints be enforced on the model to improve model checking efficiency.

Following is a set of discussions of different aspects of the model that was presented in this chapter.

6.4.1 Train lengths and movement on track segments

In the model, it is possible to specify any length of trains, linear track segments and points. This gives a lot of freedom wrt. modeling choices, for example does it allows modeling of tracks that are physically longer than the trains. This is essentially fine if one wants to model that the trains traverse over very long tracks. However, with respect to how the state tree expands and unfolds during the model checking, the tracks which are longer than trains becomes quite meaningless and generates unnecessary state expansion since, the train has to move in discrete steps over the long track. As illustrated below, a train of length two moving over a linear track segment of length five requires four movement steps which all occur within the given track segment.



Figure 6.16: A train of length 2 moves over a linear track segment of length 5. This kind of model does not add anything meaningful since the train just will stay in the same movement to movement transition for a few more states.

Yet another complication that can arise as consequence of non-constrained lengths of especially trains and linear track segments, is deadlocks. If a train is much longer than the track segment at its destination, the rear of the train will be located at another track segment or point making it impossible for other trains to pass.

To lessen the state expansion due to trains moving over very long tracks and to avoid obvious deadlocks, a constraint could be made for the length of the track segments such that no track segment can be longer than the train that traverses it.

In the case where a track segment is exactly the same length as the train that traverses it, the model essentially models that the train is in transition over a long track segment, because the train only occupies sections of the given track segment.

The generic model already supports having different length representations of the same track segment between the individual trains, since each *Train class*

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contains an array *track_lengths* which defines lengths of each of the track segments on its route. However, it is not possible to define constrains directly in UMC for these lengths, so the verification that routes obey these constraints is left over to a tool described in the next chapter.

6.4.2 Point Lengths

In the current model, it is possible to create points of any lengths one desire, however, one could argue that points of lengths higher than one, would be quite meaningless since a point only really represents a track segment containing a branch to two other track segments.

In all experiments conducted in this project based on the model, points of length one has solely been used.

6.4.3 Point Machine

The point has been modeled such that the mechanical action is performed in a synchronized manner. If the model were implemented in a real life system, exactly as specified, the points would block the propagation of the agree message of the two phase commit protocol. In a real system, it would be ideal to let the point node delegate the action of performing the mechanical switching between tracks, to a point machine asynchronously. In a better designed system, the point node would send a request to perform the switching to its point machine asynchronously as soon as the point has received the commit request from the second phase of the two phase commit protocol. This would make the communication in the system faster, since the commit requests wouldn't have to wait at each point for it to perform the mechanical positioning.

6.4.4 Repairment of malfunctioning points

The system get locked down into an impossible state when a point malfunctions, because there is no way for the points to go back into a non reserved state from a malfunctioning state. This makes it less trivial to verify the progress of the system, since the malfunctioning state of a point locks down reservation of any route in the model that includes the given point. So when model checking the model for progress, the malfunction states must be ignored. To fix this problem, a simple state transition could be added to the point, simulating that it has been repaired and is now available for reservation again.

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Chapter 7

Model generating tool

Model checking languages, are often made to be target languages for other languages or tools to translate into, and this is also the case for UMC. UMC is great for specifying the generic behavior of components that make up a system, but creating concrete models by instantiating objects from the generic components, can however be cumbersome and can easily result in a wrongly specified model which leads to false model checking results. Furthermore is it easy to specify a model that results in inefficient model checking.

In the case of the model presented in the previous chapter, there are multiple things the user would have to verify manually if specifying a concrete model himself / herself. For example, there is an important relationship between the objects, such as the relationship between overlapping train routes. The model is furthermore very generic, and makes it possible to specify some very inefficient models.

To deal with these issues and making the process of creating models simpler, a model generating tool has been developed in the F# programming language. This chapter describes the goals, workings and implementation of the tool.

7.1 Functionality of the Tool

When manually specifying a geographic interlocking model based on the generic components in UMC, the user must specify initial values such as the routes, track lengths of all the track components, the correct location of the train and the required positioning of the points on the routes. All these values need to be specified correctly when creating the model. If not specified correctly, the model will either not work or give false results. Furthermore is there performance to be gained in the model checking, by enforcing constraints on the models.

The primary goal of the tool is to assist the user in composing and generate a valid model. This is achieved by enabling the user to specify a model in a tiny DSL (Domain Specific Language) in a F# script, or by loading an existing railway network layout and predefined routes from an XML file. The XML files in this case are produced as part of the RobustRails project[?] by the **Lyngby Railway Verification Tool-set** (LRVT) [VHP16], which contain a graphical tool that was implemented in another masters project at DTU[Fol15].

The model generating tool described in this chapter validates a given input model specification, rejects it if it contains invalid routes or if it violates constraints, and finally generates a full model with properties ready to be model checked if the model is valid.

The current implementation of the model generating tool is only able to generate models in the UMC model checking language. However, the tool has been implemented with other modeling languages in mind such that it is possible to reuse the core parts of the implementation in extending and adding support for other modeling languages.

The functionalities of the tool are

- Track Layout and Route Extraction which is the extraction of relevant data from XML files.
- Route Composition which is the ability to compose multiple routes into one.
- Route validation which is the validation of the user defined routes against a concrete network layout, and against each other to avoid obvious deadlocks.
- Enforcement of length constraints which is about constraining the produced models such that they are more performant during model checking and avoids obvious deadlocks.

- **Object Creation** which is the instantiation of the concrete model objects that together compose a final model.
- Model Composition which is the composition of the generated objects and properties, and the merging with a generic model description to form a valid executable model.

7.1.1 Track Layout and Route Extraction from XML files

The model generating tool can use specially formatted XML files generated by the graphical tool of LRVT. These XML files contains a description of a concrete track layout and a set of possible routes for the given track layout.

A snippet of the *network* definition is presented below, and the full version can be found in Appendix G.

```
<network id="mininetwork">
1
       <trackSection id="b10" length="100" type="linear">
2
            <neighbor ref="t10" side="up"/>
3
       </trackSection>
 4
       <trackSection id="t10" length="87" type="linear">
 5
            <neighbor ref="b10" side="down"/>
 6
            <neighbor ref="t11" side="up"/>
7
       </trackSection>
 8
9
       <trackSection id="t11" length="26" pointMachine="spskt11"
            type="point">
10
            <neighbor ref="t10" side="stem"/>
            <neighbor ref="t12" side="plus"/>
11
            <neighbor ref="t20" side="minus"/>
12
       </trackSection>
13
       <trackSection id="t12" length="3783" type="linear">
14
            <neighbor ref="t11" side="down"/>
15
            <neighbor ref="t13" side="up"/>
16
       </trackSection>
17
18
       <markerboard distance="50" id="mb10" mounted="up" track="b10"/>
19
        <markerboard distance="50" id="mb11" mounted="down"
20
            t r a c k = "t 1 0 " />
       <markerboard distance="50" id="mb13" mounted="up" track="t12"/>
21
22
        . . .
   </network>
23
```

The *network* definition contains a list of *trackSection* definitions, each specifying a track section element which can be either a *linear* or a *point*. Each track section also lists its immediate neighbors. This information is essentially what defines a network layout.

The *network* definition also contains a list of *markerboards*, where each marker

board contains a field *track* that refers to a *trackSection*. The model generator tool does not use the marker board definitions when extracting and generating a network layout. The marker boards are, however, referenced in the *route* definitions, which each refer to marker boards as the beginning and end of a given route. The *markerboard* definitions are therefore used by the tool to look up start and end *trackSections* for each route.

Following is a snippet of the *route* definitions in the *routetable* list definition in the XML files.

```
<routetable id="miniroutetable" network="mininetwork">
1
        <route id="r 1a" source="mb10" destination="mb13" dir="up">
\mathbf{2}
                                      val = 'plus' ref = 't11'/>
3
            <condition type='point'
            <condition type='point'
                                      val = minus' ref = t13'/>
4
            <condition type='signal' ref='mb11'/>
5
6
            <condition type='signal' ref='mb12'/>
            <condition type='signal' ref='mb20'/>
7
8
            <condition type='trackvacancy' ref='t10'/>
            <condition type='trackvacancy' ref='t11'/>
9
            <condition type='trackvacancy' ref='t12'/>
10
            <condition type='mutualblocking' ref='r_5b'/>
11
            <condition type='mutualblocking' ref='r 7 '/>
12
13
            . . .
       </route>
14
15
        . . .
   </routetable>
16
```

Each route defines a source and destination which are references to markerboards defined in the network definition. The model generating tool, uses these references to look up the trackSections for the start and end of the given route. A route also has an *id* field, and when specifying a model to be generated, the user will need to refer to these *id* fields.

Each route definition furthermore specifies a set of condition elements, which is divided by types into a set of trackvacancy elements, a set of point elements, a set of mutualblocking elements and a set of signal elements. The trackvacancy elements define the route sections between the source and destination of the route. It is assumed that the set of trackvacancy elements always is listed in the same order as the intended route in the network. The mutualblocking elements specify which other routes share track sections with the current route, the signal elements specify markerboards that must be closed when setting the route, and the point elements, only the elements of type trackvacancy and point are extracted and used by the model generating tool.

The model generating tool extracts the layout to be used later for validation of the user defined route compositions. Only the *routes* with route *ids* specified as input by the user, will be extracted. It is possible, though, for the user to specify a composition of multiple routes, by providing a list of *route ids*.

7.1.2 Route Validation

Generally speaking, when using the predefined routes specified in the XML file, the individual routes will be well formed since they were generated and verified by the LRVT which generated them.

In the model generating tool, it is, however, still possible for the user to pick two routes that conflicts. The user could for example choose two routes that start out at the same location in the track layout. Furthermore does the model generating tool allow the user to compose multiple routes into one, -so some validation must still be performed even for predefined routes.

Since it is also possible for the user to define a custom network layout and routes in a script, the model generating tool will by default perform validation on all routes specified, such as validating that a given route is a valid route in relation to the provided track layout.

The common validation for both the predefined routes from the XML file, and the custom routes specified in a script, are validations of all the routes to check if they are valid in the provided layout. A set of routes are essentially valid if there is no obvious deadlock or conflict between the routes.

The route validation checks the following set of properties:

• **Different beginning**. No two trains must have routes that start at the same track segment in the network.

If two trains were to start at exactly the same track segment, there would be a collision right from the beginning.

• **Different end**. No two trains must have routes that end at the same section in the network.

If two trains were to have the same final destination in a network, an obvious deadlock would occur since only one of the trains would be permitted to reserve and traverse its route.

• No exact opposite routes. No two trains must have routes such that the trains start and ends at exact opposite sections in the network. An obvious deadlock would occur and none of the trains would be permitted to reserve and traverse its route.

• No same routes. No two trains must have exactly the same routes. Either a collision would occur or an obvious deadlock would prevent any progress in the system.

A model obeying any of the first three conditions, will naturally also obey the last condition, which means that the model generating tool don't need to actively validate this condition when it has validated the other mentioned conditions.

The validation required for individual routes, which are either composed predefined routes or custom routes from a script, are

- Itinerary elements must be transitively wellformed in the layout. This is a validation that checks that all the neighboring track elements in the specified routes has a legal transitive relation in the track layout. Two neighboring route segments are invalid in a layout if there is no direct connection between them. The route segments must also obey the nature of points such that all routes go through points, from stem to fork or fork to stem, but never from fork to fork (as illustrated in figure 7.1).
- A train route must start and end at linear track segment types. Trains should never start or stop on a point track segment, but always start and end at linear track segments.

All of the above conditions are verified for each of the routes specified as input by the user as either a script or input values to the model generating program using XML files.

Following is an illustration of valid and invalid routes.



Figure 7.1: Illustrating examples of valid and invalid routes. The first is an *invalid* route that goes from point to point. The second is an *invalid* route that skips an element in the layout. The third is also an *invalid* route that goes from fork to fork through a point. The last two routes are examples of well formed routes.

7.1.3 Enforcement of length constraints

The generic UMC model essentially allows for any length to be defined for all the classes. As mentioned in the discussion in the previous chapter, the modeling freedom in defining lengths, can lead to various problems, where the first described problem is related to the performance of the model checking and the second described problem is a possible deadlock.

Both problems can be solved, by enforcing a set of constraints when generating models.

• All routes must start and end with a track segment of exactly the same length as the train.

This constraint must be enforced in order to prevent a train from causing a potential deadlock. If a train is allowed to be longer than its destination track segment, it might occupy more than just the final track segment, which might prevent other trains from progressing to their destination. If a train is allowed to be longer than the start track segment it might lead to a collision between two trains right from the beginning.

• No track segment length defined in a route must be longer than the train owning the route.

Constraining the track segment lengths such that they are exactly the same length or smaller than the train traversing them, improves performance of the model checking since it prevents the expansion of unnecessary movement states within the same track length. A train with a length smaller than the track segment that it traverses, will not add anything meaningful to the model compared to a train traveling over a track segment with exactly the same length as the train.

If a track segment is supposed to be modeled to be longer than the train, then it is good enough that the track in the model has exactly the same length as the train since this still will represent that the train is in transition over the track when the length of the train is solely on that track.

• The longest train determines the length of intersecting track segments between routes.

For any to trains with intersecting routes, the train with the longest length determines the length of the intersecting route segments.

If the trains are of equal length, then all their intersecting track segments must be of equal length.

If given two trains of different lengths with an intersecting track segment described in the route of the longest train, that is shorter than the length of the shortest train, then the intersecting track segment length in the route of the shortest train must be exactly the same length as the length specified in the route of the longest train.

If given two trains with different lengths with an intersecting track segment described in the route of the longest train to be of the same length as the longest train, then the length of the intersecting track segment in the route of the shortest train, must be exactly the length of the shortest train.

As already pointed out it is not efficient to traverse a track segment longer than the train that traverses it. This essentially justifies the last two constraints.

For the last constraint, the longest train must determine the length of the intersecting track segments for the shorter train, such that if the length of the intersecting segment is equal to the length of the longest train, then the length of the given track segment must be set to the exact value of the shortest train for its own route.

Observe that it is still possible to model tracks that are shorter than the lengths of the trains, this is such that very long trains covering multiple tracks can be modeled as well. Also note that only train lengths of two or higher are meaningful in this model, since a train of size one would be unable to simulate the overlapping transition between two tracks. A train of size one would essentially be reflecting a train jumping between tracks and not transitioning smoothly between them.

Following formula describes the length constraint for an intersecting track segment, which is represented as L1 in the route of the longest train T1 and as L1' in the route of the shortest train T2.

 $(T2.length \leq L1.length \leq T1.length \wedge L1'.length = T2.length) \lor$ $(T2.length > L1.length < T1.length \wedge L1'.length = L1.length)$

Note that the previously mentioned constraints must still hold true. For example if the the intersecting track segment is at the beginning or end of a route it must still obey to the constraint that the given track segment should be exactly as long as the train holding the route. Note also that are points constrained and defaulted to a length of one, which means that they are disregarded in the description of length constraints.

Three scenarios with intersecting routes between two trains Train1 and Train2 are illustrated below. In the scenarios Train2 has a length of two and Train1 has a length of four, and the relevant intersecting track section is L3 for the two first scenarios and L4 in the last. In the two first scenarios Train1 constraints Train2 s length representation of L3, and L4 in the last scenario. All the presented scenarios are examples of values that obeys the described constraint.



Figure 7.2: Three scenarios with intersecting routes where the length representations are obeying the constraints.

7.1.4 Creation of Object Instantiations and Modeling Language Specific Constructs

The key objective for the tool is to generate wellformed objects that together compose a concrete model.

The most defining element of the models, are the train routes which most of the object initializations depend upon. In the case of generating UMC models, the tool will generate three types of objects which are concrete instantiations of the generic class components described in the previous chapter. These are object instantiations of the *Train* class, the *Linear* class and the *Point* class. Furthermore will the tool generate the UMC specific *abstraction* definitions and *model checking properties*.

The generation of a UMC model is illustrated below, where it can be seen that *objects, abstractions* and *properties* are generated based on a railway layout and

a set of routes.



Figure 7.3: A model is generated from a specification of a railway network and a set of routes. The specification is turned into objects, abstractions and properties, using the generic model which the class definitions represents.

In this sub-section, concrete instantiations are illustrated with examples of object instantiations, *abstraction* definitions and *model checking property* definitions, for the UMC model described in the previous chapter. All the instantiation examples are based on the railway network model illustrated below. The model has two trains with routes consisting of the elements [L1, P1, L2, P2, L4] and [L4, P2, L3] where components prefixed L refer to linear track sections and components prefixed P are points. The points in the diagram have been illustrated with explicit *PLUS* and *MINUS* positionings in the form of plus and minus symbols.

A concrete example of a set of object instantiations, abstractions and properties can also be found in Appendix D, using the same example model as presented here, but with slightly different naming.



Figure 7.4: Example of a concrete model with two trains and two routes, which is used as running example in all of the following subsections.

7.1.4.1 Object Initializations

Point Objects The *point* objects are the simplest type of object instantiations for the UMC model.

For the given model in the diagram, the point object instantiations are simply as follows

The points don't need to be instantiated with any parameters because of the way the *Point* class is specified in the UMC model. As specified in the *Point* class, the point objects will be instantiated with a default positioning value of true (PLUS).

Linear Objects The *linear* objects are also quite simple, as all that is needed in the instantiation, is to instantiate the linears with information about the absence or presence of a train.

For the model in the diagram, the linear object instantiations would be as follows.

L1: Linear (train
$$=>$$
 train1);
L2: Linear;
L3: Linear;
L4: Linear (train $=>$ train2);
(7.2)

The *train* variables are only initialized for the linears which are at the beginning of a given train route. When no value is specified, the *train* variable simply defaults to *null*.

Train objects The *train* objects are the most involved objects as they contain information about track segment lengths which must be specified consistently across the trains, the initial *occupies* variables used for for simulating train movement, and finally the routes which must be valid between the trains.

The instantiation based on the running example model in figure 7.4 is as follows

train1: Train(
	$\mathrm{route_segments} => [\mathrm{L1}, \mathrm{P1}, \mathrm{L2}, \mathrm{P2}, \mathrm{L4}],$	
	$\mathrm{track_lengths} => [3,\!1,\!2,\!1,\!3],$	
	${ m train_length} => 3,$	
	occupies => [L1, L1, L1],	
	requested point positions => [null,True,null,True]);	
train2: Train(
	$\mathrm{route_segments} => [\mathrm{L4},\!\mathrm{P2},\!\mathrm{L3}],$	
	${ m track_lengths} => [3,\!1,\!3],$	
	${ m train_length} => 3,$	
	occupies => [L4, L4, L4],	
	$requested_point_positions => [null,False]);$	
		(7.3)

The array *route_segments* must be initialized with the ordered train route, such that the routes are valid between the trains in the same layout.

Likewise must the *track_lengths* array be initialized with the length value of the index-wise corresponding elements of the *route_segments* array, in a way such that the length of a given element obeys the length constraints between the route descriptions of the trains. As previously mentioned, points are always instantiated with a length of one.

The *occupies* array must be exactly same length as the train, and it must be filled with references to the first track segment of the given train route.

The requested_point_positions array, must be defined such that it refers indexwise to the route_segments array. The requested_point_positions array is simply filled with null values for the indexes which does not correspond to points on the route, and it only needs to define values up to the index of the last point element in the route array.

7.1.4.2 Generation of Language Specific Constructs

Specific for the UMC modeling language is that it has special constructs called *abstractions* which are used in the definition of the model checking properties. The concrete definitions of the abstractions are, like the the objects, dependent on the given model layout and routes.

Following are concrete examples of definitions based on the formally specified abstractions and properties that were formally described in the model checking section of the previous chapter.

The no collision property

The no-collision property is generic since it simply validates the abstraction *trains_at_diff_positions* globally over all paths. For the running model example, the property is simply defined as follows

AG (trains at diff positions)

The trains at diff positions abstraction

The trains_at_diff_positions abstraction is rather involved, and cannot be generalized so well in the language of UMC. In the tool, a cross product of the indexes of any two trains occupies arrays are generated, and based on this a set of conjunctions are composed, each specifying that two any two indexes of the occupies arrays must be different.

The instantiation based on the running example model is presented below.

State	train1.occupies[0]	/ =	train2.occupies[1] and
	train1.occupies[0]	/ =	train2.occupies[2] and
	train1.occupies[1]	/ =	train2.occupies[2] and
	train1.occupies[2]	/ =	train2.occupies[1] and
	train1.occupies[2]	/ =	train2.occupies[0] and
	train1.occupies[1]	/ =	train2.occupies[0] and
	train1.occupies[0]	/ =	train2.occupies[0] and
	train1.occupies[1]	/ =	train2.occupies[1] and
	train1.occupies[2]	/ =	$train2.occupies[2] \rightarrow trains_at_diff_positions$
			(7.4)

The no derailment property

As mentioned in the previous chapter, the *no derailment* property uses a set of abstractions defining absence of trains on points, and a set of abstractions defining positioning of points.

Using the running example, the absence of trains on points are declared as follows by the model generator tool.

State
$$p1.train = null \rightarrow no_train_on_p1$$

State $p2.train = null \rightarrow no_train_on_p2$ (7.5)

And the abstractions specifying points in positioning states, are declared as follows, using the running example model.

The *no derailment* property can now be specified, for the running model example, using above abstractions.

AG(

position_p1 implies no_train_on_p1 and (7.7) position_p2 implies no_train_on_p2)

The progress property

The progress property which specifies that trains eventually will arrive at their destinations, simply uses one abstraction which captures the the global state where a train has arrived in the system.

Using the running example model, an abstraction is simply defined for each of the trains as follows.

State
$$inState(train1.ARRIVED) \rightarrow train1_arrived$$

State $inState(train2.ARRIVED) \rightarrow train2_arrived$ (7.8)

The property can now be declared as follows, for the running example model.

EF AG (train2 arrived and train1 arrived)

As mentioned in the previous chapter, the above property only verifies that there exist states where the trains will reach their destinations. However, the claim is that the trains will arrive in all cases where the *points* on the routes functions correctly without malfunctions. And to verify this claim for the current model, a special property can be created as described in the previous chapter.

The property requires a set of abstractions, each capturing the situation where a point has entered a MALFUNCTION state.

The property for verifying the claim, can then be defined as follows

not $E[$	not $(p2_malfunction \text{ or } p1_malfunction)$ U			
	(final and not (train2_arrived and train1_arrived))]	(1.10)		

(For a more elaborate explanation of this property, refer to the formal specification of the given property in the previous chapter)

The no message loss property

The property for checking that all messages are handled in the system, is independent of the actual model, and therefore the abstraction *discarded_message*, and the property that verifies that for all state paths no message will ever be lost, -can both be used directly as they are defined in the previous chapter. Thus, for the running example model, the abstraction *discarded_message* is simply defined as

Action: lostevent -> discarded message

and the property itself is defined as

AG not (EX discarded message true)

7.2 Implementation

The model generating tool has been implemented in the programming language F#. F# was, first of all, chosen due to familiarity and experience, but also because F# provides a special set of tools for conveniently parsing data files such as XML files with minimal effort.[PGS16]

Other considered languages and frameworks were the Idris programming language, which is a functional language that provides dependent types as first class citizen as a core facility[BRA13], and RAISE (Rigorous Approach to Formal Software Engineering) RSL (RAISE Specification Language)[Hax14].

Using Idris was discarded due to lack of practical experience with the language, and using RSL was discarded due to the lack of out-of-the-box facilities for, for example, working with XML files.

Both an executable model generating program and simple scripting DSL (Domain Specific Language) library has been implemented, both using the same set of core functions for validation, constraint verification and internal model representation and composition.

The executable program can be given an XML file path as input together with a set of route definitions to generate a complete model, but has been simplified to only generate models where trains and linear segments all have a length of two and points a length of one. The scripting DSL gives full freedom in specifying lengths of trains and track segments, but still validates wrt. the constraints.

The source code used in the program and scripting DSL tools is divided into four main modules which are *Utils*, *InterlockingModel*, *UMC*, *XMLExtraction* and *MiniModelGenerator*.

Below an informal diagram is presented, showing the dependency relationship between all of the files containing the main modules, and where in the model generating process they are used.



Figure 7.5: Overview of the Tool components. Arrows points to where a given module is used.

The source code for all of the files can be found in Appendix E.

- The *Utils* module contains general types and functions which has no concrete relationship to the model generation.
- The *InterlockingModel* module defines generalized types and functions for defining a model, furthermore does it contain an higher order function *validateAndGenerateModel* which performs all validation and constraint verification on a model, and can be applied to a specific model generating function, such as for example, a function for generating a UMC model.
- The *UMC* module defines a set of functions for instantiating models in the UMC language, and defines a specific UMC model generating function which can be passed on to the higher order function *validateAndGenerateModel* defined in the *InterlockingModel* module.
- The *XMLExtraction* module defines functionality for reading XML files and constructing an internal F# data type representation of the model to be generated.
- The *MiniModelGenerator* module contains the entry point for the executeable program, and performs basic validation of the user inputs.

The scripting library tools are implemented in the *ScriptTools* module which exposes a set of simple types and functions that can be used as a small DSL directly from an F# script file.

Each of the mentioned modules are defined in its own file, and are divided into several sub modules that each contain functions related to the same aspect of the model generator.

A model can be generated either based on a specification in a script, or from the compiled *MiniModelGenerator* program which can be provided with a set of user input arguments including a file path to an XML file containing a network layout and predefined routes.

Descriptions on how to use the tool to generate models, can be found in Appendix A.

7.2.1 Modules

This subsection provides a high level description of each of the main modules involved in the model generation.

7.2.1.1 Utils module

This module contains common functionality such as functions for generating all possible paired combinations of values from a list or cross products from two lists, and types and functionality for error handling.

The module notably defines a type *Result*, a computation expression *resultFlow* and a computation expression *maybe*, -which all are used extensively throughout all of the other modules.

The type Result < T1, T2 > and the Computation Expression result-Flow

The Result type carries a generic success type ('T1) and a generic error type ('T2). This type is used throughout the whole program and libraries to handle error cases and to collect and propagate errors out to the user.

The Result type is defined as follows

```
1 type Result <'success,'error > = Ok of 'success
2 | Error of 'error
```

7.2 Implementation

The *Result* type is extended with a set of operators and functions for composability of values and functions using the Result type. The type is extended with functions for common list operations such as *reduce* and *fold*, and a special F#construct called a *Computation Expression*[PS14].

The type and its associated *Computation Expression* together form a Monadpattern[wikb]. The implemented monad pattern, used for the *Result* type, is more commonly known as the *Either Monad* pattern.¹

Monad patterns makes it syntactically convenient to compose value wrapping types and functions that returns types of the same value wrapping type.

To implement a Monad pattern, a function bind and a function return must be defined.

The *return* function is simply a function that takes a simple value of an arbitrary type as input and returns the same value wrapped in the type used for the monad pattern (eg. the Result type). The type used in a monad pattern is commonly referred to as a monadic type.

The *bind* function is a higher order function that takes two arguments as input, a value of arbitrary type wrapped in the monadic type, and a continuation function that takes a value of the same arbitrary type, as the first argument, -as input and returns a result which is another arbitrary type wrapped in the monadic type. The *bind* function essentially unwraps the first argument from the monadic type, and applies the result to the continuation function, after which the result of the continuation function is returned.

The abstract type signatures for the bind and return functions are sketched below

$$return: \quad a \to M \quad a$$
 bind: $M \quad a \to (a \to M \quad b) \to M \quad b$

where 'a and 'b are arbitrary types and M is the monadic type. The bind function is also commonly implemented as the binary operator $\gg =$, and such an operator is also defined for the Result type in the model generating tool implementation.

In order for a type to be classified as monadic and to be optimally composable, the bind and return functions must obey the three Monad Laws[wikb], which essentially describes how to compose the *bind* and *return* functions.

 $^{{}^{1}}F\#$ 4.1 will be released late 2016 and will implement a type *Result* with the exact same signature. Therefore the name *Result* has been chosen in this implementation, instead of the name Either.

The Computation Expression for the *Result* type is instantiated into a construct named *resultFlow*, and is used extensively throughout the implementation for error handling and propagation of error messages.

The maybe Computation Expression construct

F# defines a standard library type Option < T > for constructing optional types that can be either be *None* or a value of type 'T.

The Utils module implements a Computation Expression construct maybe to help composing values of type Option and functions returning the type Option. The defined Monad is often referred to as the Maybe Monad, thus the name maybe for the construct in this implementation.

7.2.1.2 InterlockingModel module

This module contains all the basic type definitions necessary for describing an interlocking system model. Furthermore does the module define sub-modules containing functions for verifying that a given model is sound with regards to the routes and with regards to the length constraints.

At last the module define an higher order function *validateAndGenerateModel* which takes a model generating function as input and generates a textual representation of a valid model.

The module contains the sub modules TypeDefinitions, RouteConstruction, RouteValidation, LengthConstraints and ModelGeneration. The TypeDefinitionsmodule contains all the basic types for representing a concrete railway model in F#. The module RouteConstruction contains functions for composing multiple routes together to form one route. The module RouteValidation contains functions for validating a set of routes against each other, and against a railway network layout. The module LengthConstraints contains functions for checking that the length constraints within and between between intersecting routes, are obeyed. The ModelGeneration contains functions that uses the functions from the other modules, to validate and compose valid models, most important, the sub module defines the validateAndGenerateModel function.

The core type definitions representing the internal representation of the concrete railway model components, are presented below.

```
1 type TrainId = TrainId of string
2 type TrainIds = TrainId list
3
4 type LinearId = LinearId of string
5
6 type PointId = PointId of string
7
8 type PointPosition = Plus | Minus
```

9

```
type RouteSegment =
10
11
         LinearRouteSegment of LinearId * length : int
          PointRouteSegment of PointId * required position :
12
             PointPosition
    type RouteSegments = RouteSegment list
13
14
    type RouteDirection = Up | Down
15
16
    type Route = Route of RouteSegments * RouteDirection
17
    type Routes = Route list
18
19
    type Train = { id : TrainId
20
                    route : Route
21
                    length : int }
22
   type Trains = Train list
23
24
    type Linear = { id : LinearId
25
                     train : Train option }
26
    type Linears = Linear list
27
28
    type Point = { id : PointId
29
                    position : PointPosition }
30
    type Points = Point list
31
32
33
    type LayoutSegment =
         LinearLayoutSegment of id : string
34
          PointStemLayoutSegment of id : string
35
        PointForkLayoutSegment of id : string * position :
36
             PointPosition
37
   {\bf type} \ {\tt RailwayNetworkLayout} = \ {\tt Map}\!\!< \ {\tt LayoutSegment} \,, \ {\tt LayoutSegment}\!>
38
39
    type ModelObjects = { trains
                                     : Map<TrainId, Train>
40
                            linears : Map<LinearId, Linear>
41
                            points : Map<PointId , Point> }
42
   type ValidatedModelObjects = Validated of ModelObjects
43
44
    type ModelGeneratorFunction = ValidatedModelObjects -> string
45
```

These types together describe the internal representation of a given model in the tool implementation, and the functions implemented in the *InterlockingModel* module all deal with one or more of these types.

Notably, is the type *ModelObjects* used to represent the objects that must be initialized in the modeling language to compose the concrete model. The simple wrapper type *ValidatedModelObjects* is defined to represent a model that has been validated.

The RailwayNetworkLayout type describes a railway network as a mapping from a LayoutSegment to a LayoutSegment. Consequently, the network layout is naturally only represented as connections from left to right, which also represents the Up direction. This means that when a route in the *Down* direction is to be

verified against the layout, it is reversed before the verification.

The last type definition ModelGeneratorFunction, is a signature description of a general function that can produce a concrete model in a string representation, based on a valid model. The *InterlockingModel* module itself implements such a function for outputting the 'raw' internal F# model representation as a string, but more importantly does the *UMC* module implement such a function as well for generating a textual representation of a full UMC model. The type is used in the signature of the function *validateAndGenerateModel* which is the only function in the module used from the other modules. The type signature and implementation of the function is presented below.

```
val validateAndGenerateModel : ModelGeneratorFunction \rightarrow
 1
\mathbf{2}
                                        RailwayNetworkLayout ->
                                       ModelObjects ->
3
                                        Result < string , string >
 \mathbf{4}
5
    let validateAndGenerateModel : modelGenFun = fun layout objects ->
6
7
        validateTrainRoutes layout
                                       objects
        >>= checkLengthContraints
8
        >>= updateTrainLocations
9
        >>= (modelGenFun >> Ok)
10
```

Note that signatures and functions normally aren't defined together like this in F#, but for the sake of presentation the evaluated type of the function is shown above the function in this code fragment.

As can be seen from the presented code, the function makes use of the bind operator described in the *Utils* module, for chaining together functions that produce *Result* types.

The function first makes sure the routes are validated by applying the validateTrainRoutes function, the result from that function is applied through the bind operator to the checkLengthContraints which verifies that the length constraints are obeyed. Next the result is applied through the bind operator to the updateTrainLocations function which updates the track elements in the model with regards to presence of trains. At last the result is applied through the bind operator to the modelGenFun function which for example can be a reference to the UMC model generating function. If at any of the bindings an error is returned, the error will simply be propagated out as an error result of the validateAndGenerateModel function.

The last thing to note about the *InterlockingModel* module, is that it defines a class interface *ModelCheckingPropertyDefinitions* which simply act as a template for the actual properties to be implemented. The interface definitions is presented below.

1 **type** ModelCheckingPropertyDefinitions =

2 abstract NoCollision : string
3 abstract AllTrainsArrived : string
4 abstract NoDerailment : string
5 abstract TrainsDetectedOnPoints : string
6 abstract AllMessagesHandled : string

7.2.1.3 UMC module

The UMC module imports the source files UMCLinearClass.fs, UMCPoint-Class.fs and UMCTrainClass.fs, which each simply contains a string representation of the three generic classes defined in UMC (The Linear class, the Point class and the Train class). At the end of the model generation, these string representations are simply concatenated and prepended to the generated objects and abstractions of the model. The motivation for containing the generic UMC class information this way instead of having them in separate files, is simply such that the type checker will yield an error if the files doesn't exists.

The UMC module basically contains functions for generating a full textual UMC model. The module contains the sub modules AbstractionDefinitions, ModelObjectInstantiations and Properties. The AbstractionDefinitions module defines functions for generating concrete UMC abstractions, the ModelObjectInstantiations module defines functions for generating the set of UMC object instantiations for a final model, and the Properties module define the functions for generating and composing UMC model properties.

The *UMC* module furthermore implements the *ModelCheckingPropertyDefinitions* interface (described in the *InterlockingModel* module) in a class that has a constructor which takes a set of validated model objects and instantiates each of the model properties.

At last the UMC module defines a function composeModel, which utilizes functions from the UMC module to implement a function of the type ModelGeneratorFunction, that generates and composes a full textual UMC model. Since the function has the type signature ModelGeneratorFunction, it can be used directly together with the validateAndGenerateModel function from the InterlockingModel module, to generate a valid full UMC model.

7.2.1.4 XMLExtraction module

This module defines functionality for extracting and composing an internal model representation, based on a given XML file. The module notably uses the special F# Type provider library for parsing and handling XML files. The module contains the sub modules BasicObjectExtraction, LayoutExtraction, RouteExtraction and ModelGenerationFromXML. The module BasicObjectExtraction, defines functions for extracting and creating the basic components required for creating an internal model. The LayoutExtraction module defines functions for extracting and constructing an internal railway network layout representation from an XML file. The module RouteExtraction defines functions for extracting a set of routes from an XML file and generating an internal model representation. The ModelGenerationFromXML module, finally defines a type ModelGenerationParameters and the function generateModelFromXML. The ModelGenerationParameters type is a record type holding a reference to a concrete model generating function with the type signature ModelGenerator-Function, a file path to an XML file and a field routes which is a list of lists of route ids to be extracted from the XML file. Each list of ids describes a composition of multiple routes.

```
1
2
3
4
```

```
type ModelGenerationParameters =
    { modelGeneratorFunction : ModelGeneratorFunction
        xml_file_path : string
        routes : string list list }
```

The generateModelFromXML function has following type signature, which returns a result that can be either a string representation of a final composed model, or an error message describing for example the violation of a constraint during the validation of a model.

 $val\ generateModelFromXML$: ModelGenerationParameters -> Result < string, string > range = range

The function uses the extraction functions described in the other sub modules to extract and compose an internal representation of the model, which it then proceeds to apply to the *validateAndGenerateModel* function from the *Interlock-ingModel* module to validate and generate a final concrete model instantiation in the modeling language of interest.

7.2.1.5 MiniModelGenerator module

The *MiniModelGenerator* module defines the entry point for the compiled model generator tool. The entry point is defined as a function *main* that takes an array of user provided arguments, parses them, generates a model and outputs the string representation of the given model instantiation in the console.

The module defines functionality for parsing user input such as lists of route ids, referring to the route ids of routes in an XML file, and a type *ModelOutput* with following type signature
```
1 type ModelOutput = UMC
2 | Raw // representing the raw F# objects
```

which describes the available textual model outputs, and are either a raw string representation of the internal model in F#, or a concrete UMC model which can be used directly as input to a UMC model checking tool.

7.2.1.6 ScriptingTools module

The scripting tools module describes a set of very simple types for specifying a concrete model, and exposes one function *generateUMCModel* which validates, composes and generates a concrete UMC model based on a simple type representation of the model.

The simple types for defining a model are listed below

```
type SimpleTrackSegment =
1
         LLinear of name : string
\mathbf{2}
         LPointFork of name : string * PointPosition
3
        LPointStem of name : string
4
5
6
   let (<+>) (el1 : SimpleTrackSegment)
7
              (el2 : SimpleTrackSegment) = el1, el2
8
9
   type SimpleLayout = (SimpleTrackSegment * SimpleTrackSegment) list
10
   type SimpleRouteElement =
11
        RLinear of name : string * length : int
12
        RPoint of name : string * position : PointPosition
13
   type SimpleRoute = SimpleRouteElement list
14
15
   type SimpleTrain =
16
17
        { id : string
        ; length : int
18
        ; route : SimpleRoute
19
20
         route
                direction : RouteDirection }
   type SimpleTrains = SimpleTrain list
21
22
   type Layout Type = CustomLayout of SimpleLayout
23
24
                     XMLLayout of path : string
25
26
   type SimpleModelArgs =
27
        { trains : SimpleTrain list
28
        ; layout : LayoutType
29
        ; show stats : bool
30
        ; output file : string option }
```

The types and operator basically forms a small DSL like language which the user can use to define a set of trains with routes and a network layout, and apply these to the *generateUMCModel* function to produce a full and valid textual UMC model.

A guide on how to compose a script can be found in Appendix A.

7.3 Extending the Model Generator to support other modeling languages

The code has been structured such that it can be used as a library for generating models. To implement support for more model checking languages, one could define a module similar to the *UMC* module, for generating the textual string representations in the given modeling language. The module must furthermore implement a function with the signature of the type *ModelGeneratorFunction*, which then can be used as input to the *validateAndGenerateModel* function from the *InterlockingModel* module, to produce validated concrete models in the target modeling language.

Chapter 8

Experiments

Logic takes care of itself; all we have to do is to look and see how it does it.

Ludwig Wittgenstein

During the project, many experiments has been performed with concrete models based on the presented generic UMC model.

This chapter describes a few of the experiments and presents the results from performing model checking on concrete models. Specifically, a set of experiments has been set up to investigate the scalability of the model with regards to the size of the railway network and number of trains. Investigating the model checking performance with regards to scalability, essentially serves to benchmark the performance of the generic model devised in this project.

8.1 Performing the experiments

The experiments performed in this project, refers to the generation of a concrete model instantiations with a set of train routes based on a specific type of network

layout, and at last the model checking of said model instantiation.

The three first types of model instantiations used in the following sections, has been generated using the scripting tools described in the previous chapter, and the concrete scripts used can be found in Appendix F.

The last set of experiments was performed with models generated from XML files by using the executable model generating tool.

The generated UMC models are loaded and model checked through an online service with a web-interface[Mazb]. The online service is hosted on a server with an Intel Xeon 2x2.66 GHz Quad-Core processor and 24 GB of Memory. The online service might be used simultaneously by other clients, and furthermore does the server host other applications, which all might impact the execution time of the model checking.

8.2 Experiments performed

This section describes to sets of different experiments performed to test the scalability of the model.

One set of experiments seeks to investigate the scalability of the model with regards to the length of train routes, and the other set of experiments seeks to investigate the scalability of the model with regards to number of active trains in the model.

8.2.1 Two trains and varying route lengths

The first set of experiments seek to investigate the performance of the model when it is instantiated with long train routes.

All the model instantiations contains two trains, each with a route as long as possible. The model instantiations are based on the layout below, which contains a set of reconnecting branch loops which can be perceived as stations.

For the given set of experiments, models from one to ten stations has been generated. Out of these ten models, it was possible to model check the first eight within reasonable time.



Figure 8.1: Drawing of the model type which is generated for the experiments. The generated layouts have a varying number of reconnecting loops, or stations.

The results from model checking the first eight models, are presented in the table below, where the model names refer to the number of stations in the given model.

	One	Two	Three	Four	Five	Six	Seven	Eight
Route lengths	[5;3]	[9;7]	[13;11]	[17; 15]	[21;19]	[25; 23]	[29;27]	[33;31]
Number of linears	4	7	10	13	16	19	22	25
Number of points	2	4	6	8	10	12	14	16
Number of route sub-segments	13	25	37	49	61	73	85	97
Number of shared points	1	3	5	7	9	11	13	15
Number of shared linears	1	2	3	4	5	6	7	8
Time for Trains correctly detected on points	0.3	5.7	48.4	242.1	1005.0	-	-	-
Time for No collisions	0.2	1.7	7.8	25.2	72.6	176.8	381.2	952.1
Time for No derailments	0.2	1.3	7.5	25.0	74.2	180.0	394.9	795.1
Time for Will arrive	0.2	0.9	6.0	14.1	67.7	140.2	273.3	567.3
Time for No message loss	0.1	0.9	4.8	14.9	42.3	96.7	212.4	408.6
Total time used checking properties	0.7	4.9	26.2	79.2	256.8	593.7	1261.9	2723.2
Number of states explored	736	6795	28768	84314	198868	406409	750228	1283696

Table 8.1: Resulting data from experiments performed with two trains and
varying number of stations from one station to eight stations. All
time values are given as seconds and the route lengths of the in-
volved trains are presented as a list.

All the listed properties evaluated to true in the model checking.

Following listing describes the variables presented in the table.

- *Route lengths* are presented as a list of values separated by ';', where each value refers to the length of a route. The length of a route describes how many track segments, consisting of points and linear segments, which the route covers.
- Number of linears is the total number of linear segments in the network.
- Number of points is the total number of points in the network.

- *Number of route sub-segments* is the sum of all of the sub-segments which both of the routes covers, where a sub-segment is either a point or a part of a linear segment.
- *Number of shared points* is the total number of points shared between all of the routes.
- *Number of shared linears* is the total number of linears shared between all of the routes.
- *Time for Trains correctly detected on points* presents the time used for verifying the property **Trains correctly detected on points** through model checking. As can be seen in the table, the property is significantly more time consuming to model check, and therefore it has been skipped for the last three models.
- *Time for No collisions* is the time used for model checking the property **No collision**.
- *Time for No derailments* is the time used for model checking the property **No derailments**.
- *Time for Will arrive* is the time used for model checking the property Will arrive.
- *Time for No message loss* is the time used for model checking the property No message loss.
- Total time used checking properties is the sum of the time used for model checking each property. However, to ease the comparison of the models, -the sum excludes the time used for checking the property **Trains correctly detected on points** since this property has only been checked for the first five models.
- *Number of states explored* is the total number of states explored by the model checker in its pursuit of verifying the properties.

All the described properties are described in chapter 6.

Following are two plots of the obtained data. First a plot of the number of states explored in relation to the number of stations, and next a plot illustrating the time spend on model checking the properties in relation to the number of stations.

From the plot below it can be observed that the number of states increases with an exponential growth as the number of stations increases and the routes gets longer.



Figure 8.2: Plot of the states explored for each number of stations

The following plot, clearly show that the two safety properties **No collision** and **No derailments** are guilty of the majority of time spend on model checking properties.



Figure 8.3: Stacked plot of the running times of each property for each number of stations

8.2.2 Varying number of trains

This set of experiments seeks to investigate how the model performs with regards to the number of active trains in the model, and specifically with regards to trains with intersecting routes.

The concrete models to be used, are based on the branching network layout presented in the drawing below.



Figure 8.4: Drawing of the model used as basis for creating experiments with multiple trains.

Even though the devised script for generating the models is able to create bigger networks with room for more trains, only the layout presented in the drawing above was used, since model checking couldn't even be performed within reasonable time for just four trains with intersecting routes.

A table of the data obtained from model checking concrete model scenarios with **two**, **three** and **four** trains, are presented below.

The model with four trains didn't succeed in being model checked within reasonable time, however was reported by the model checker that it had explored more than seven million states.

Also note that the shared points and shared linears here describes the total number of intersecting points and linears between any two routes.

	Two	Three	Four
Route lengths	[7;7]	[7;7;7]	[7;7;7;7]
Number of linears	9	9	9
Number of points	6	6	6
Number of route sub-segments	20	30	40
Number of shared points	4	8	16
Number of shared linears	1	3	6
Time for No collisions	0.9	78.6	-
Time for No derailments	0.7	79.8	-
Time for Will arrive	0.5	40.5	-
Time for No message loss	0.4	49.1	-
Total time used checking properties	2.5	248.0	-
Number of states explored	2750	234691	7000000 +

Table 8.2: Resulting data from experiments with varying number of trains.

All the listed properties evaluated to true in the model checking.

8.2.3 Experiments with particular layouts from XML files

Following experiments were performed with models generated by the executable model generating program with XML files containing layouts and routes.

	Mini	Twist	Threelines
Route lengths	[6;4]	[5;5;5]	[6;6;7]
Number of linears	6	8	13
Number of points	2	2	6
Number of route sub-segments	17	24	28
Number of shared points	1	3	5
Number of shared linears	1	2	2
Time for No collisions	0.4	8.4	91.9
Time for No derailments	0.3	8.1	96.3
Time for Will arrive	0.2	3.7	40.9
Time for No message loss	0.2	6.2	68.1
Total time used checking properties	1.1	26.4	297.2
Number of states explored	1473	34978	223294

 Table 8.3: Resulting data from experiments with models generated from XML files.

	Twist	Three trains	Threelines
Route lengths	[5;5;5]	[7;7;7]	[6;6;7]
Number of linears	8	9	13
Number of points	2	6	6
Number of route sub-segments	24	30	28
Number of shared points	3	8	5
Number of shared linears	2	3	2
Time for No collisions	8.4	78.6	91.9
Time for No derailments	8.1	79.8	96.3
Time for Will arrive	3.7	40.5	40.9
Time for No message loss	6.2	49.1	68.1
Total time used checking properties	26.4	248.0	297.2
Number of states explored	34978	234691	223294

 Table 8.4: Resulting data from experiments with models generated from XML files.

Here it is interesting to observe the dramatic difference between the two models Twist and Threelines which both involves three trains and three routes. Comparing the data from the Threelines model with the model using three trains from the experiment in the previous subsection, it seems that its the number of linears and points that make the difference. The Threelines model takes longer to model check and, has a total count of linears and points of 19, while the model with three trains from the previous subsection has a total count of linears and points of 15. The number of shared points and linears and the lengths of the routes are all smaller for the Threelines model. So it must be the number of points and linears that makes the difference here.

8.3 Discussion

As has been shown through the experiments, model checking concrete models with just two trains at the time is feasible for routes of limited lengths. The increase in states to explore is however exponential which displays an important limitation of the model with regards to length of routes. It is certainly feasible to model check routes with lengths shorter than the ones presented in the experiments, but if they get much longer the state space explosion will be too significant to perform any model checking.

The experiments performed with more than two trains displayed an even more drastic explosion in states to explore, and the model with four trains was impossible to model check within a reasonable time frame.

It is worth reflecting over the fact that one of the reasons why model checking becomes much harder as the number of trains with intersecting routes increases, is by large due to the reservation protocol. When model checking any model with more than one train and with intersecting routes, one of the trains will always be the first to succeed in reserving a route and the rest of the trains will keep attempting to reserve until they succeed as well. This results in a lot of fruitless attempts at reserving routes without success.

One way to improve the models performance, might be to abstract away the concept of route reservation rejection, such that trains will patiently wait for their routes to be reserved instead of reattempting reservations until success. The nodes representing the track segments and points, could for instance be equipped with a queue for reservations, in which it will queue up reservation requests while it is reserved, and as soon it is free it will pick up the first reservation request from the queue and complete that reservation. The downside of this model, though, is that it moves further away from the original engineering concept, and perhaps the abstract model would be too far from anything realistically possible.

Another way to solve the problem of model checking models with multiple trains, might simply be to use the model as it is, and model check each pair of two trains with intersection routes by themselves. This opens up for model checking the model in parallel, by assigning the verification of each pair of intersecting routes to its own process.

A challenge with this approach might be to verify progress and liveness properties for models with many trains. in order to confidently verify the whole model as sub-models in parallel, one would somehow have to prove that checking for liveness and progress for each pair would be the same as checking the whole model for liveness and progress.

Chapter 9

Future work

Even though a satisfying generic UMC model and a tool for generating concrete models, has been implemented, there is still possible work to be done. Notably the the generic UMC model can still be improved to better reflect a real life implementation, and the model generating tool can be extended with support for generating models in other modeling languages and be improved wrt. usability.

This chapter briefly elaborates over ideas for tool extensions, model improvements and usability enhancements for the tool.

9.1 Generic model enhancements

This section describes a few ideas for enhancement of the generic UMC model specification. Even though the ideas are described in the context of the generic UMC model conceived in this project, the ideas are more general as such and would also apply to a model specified in any other model checking language.

9.1.1 Repairment of faults

As mentioned in the discussion section of chapter 6, malfunctioning of a point will cause the point go into a MALFUNCTION state with no further transitions to take, and this essentially blocks trains from reserving and passing the given point. The fact that trains, in some cases, are prevented from reserving and traversing their route, makes checking the system for liveness impossible since liveness per definition requires the system to be deadlock free.

The current model could simply be enhanced such that points are able to transition back into a functioning state of availability again. This transition could represent that the point has been repaired.

9.1.2 Point Machines

In the discussion section of chapter 6, it is mentioned that the current model of the points is slightly detached from how a point would realistically operate in a life implementation.

The UMC model could simply be enhanced with a *Point machine class* and each *Point class* object would then have responsibility for one point machine, as described in the discussion of chapter 6. Modeling the points this way would also be more true to the nature of the two phase commit protocol, where changes ideally are to be enforced upon receiving the commit request -and not upon receiving the final agree response.

9.1.3 Modeling more types of faults

The model could be extended such that it models more types of faults and malfunctions. For instance, it could model failing track circuit sensors, such that all points and linear segments are able to randomly emit a false presence of a train, and letting reservation attempts fail as a consequence.

However, one should be careful about how the faults are modeled, since modeling of even a simple failure, leads to an increase of the size of the state space to be explored when model checking the properties.

9.2 Usability and performance improvements for the tool

9.2.1 Enhance the user experience with a route selection GUI

As the tool is implemented now, all user interaction either goes through the console or through user defined scripts. A user might greatly benefit from having a graphical user interface where he can define a fine grained route in a track layout diagram and define the lengths of the individual tracks.

9.2.2 Extend tool to support more modeling languages

Even though the UMC language does a great job at modeling especially distributed systems such as the one presented in this work, it could still be of interest to explore other types of modeling languages and approaches. Another modeling language might for example have better performance characteristics.

9.2.3 Model checking of huge railway networks

As briefly discussed in the experiments chapter, the current model might not be feasible if applied to large railway networks with many trains.

A way to solve this problem, could perhaps be to parallelize the model checking such that every pair of intersecting routes are model checked in their own process. And If any of the processes find any of the properties to be false, the given property has failed for the model as a whole.

It seems intuitive for the current model, that if it is verified for any pair of two trains with intersecting routes that no collision will happen, then there shouldn't be any collisions for any pairs of three trains in the system either. And the same could be said for verifying for derailment. This seems intuitive with the current model, since it require routes to be fully reserved from start to end. However, checking for liveness or progress properties might not be as trivial to check in parallel and would perhaps require other methods of verification.

Chapter 10

Conclusion

In this thesis an engineering concept of a distributed railway control system has been devised. The concept uses a two-phase commit protocol as a means for trains to reserve routes, and trains are required to fully reserve their assigned route before being permitted to traverse it.

The engineering concept has been distilled into an abstract model in the object oriented modeling language UMC. The abstract model describes three classes, each encapsulating the generic behavior of a communication node representing either a train, point or linear track segment. The model has been defined such that only the trains are aware of their routes and the connection layout in the railway network. The model has been defined such that all the physical length of all the involved elements can be described.

To ease the generation of objects from the generic classes, and to compose concrete models that obey a set of constraints, a tool has been developed in the programming language F#. The tool enables a user to generate concrete models that are valid and has the best possible characteristics with regards to performance under model checking. The user can use the tool as a library and small DSL to define models in a script, or specify a set of routes to be used from an XML file containing both routes and a railway network layout.

Using the developed model generating tool, a set of models has been gener-

ated and analyzed by model checking of safety and progress properties, and the running times and number of explored states has been recorded and compared.

For the analyzed models, the model checking has indeed revealed that all the specified safety and progress properties are valid. However, the recorded performance characteristics resulting from the model checking, also shows that the model suffers from state space explosion and doesn't scale particularly well for multiple trains and very long routes.

As discussed, the solution to this problem of scalability, could be to change the model itself with the risk of ending up with a model that doesn't reflect the engineering concept. However, as also mentioned, a better solution might be parallelize the model checking in a divide and conquer fashion such that all pairs of trains are verified by themselves in parallel.

A division of a concrete model into sub-models might be a feasible solution for verifying safety properties, however more research must be performed in this regard, especially with regards to verifying progress and liveness properties which might be the biggest challenge.

All in all, it has been shown in this project how an engineering concept can be turned into an abstract model specification, and verified through model checking. The UMC language has shown to be a great tool for describing distributed systems, by enabling the user to essentially describe a set of state machines and the communication between them.

Model checking, is a very useful tool for creating program specifications that can be verified. However, model checking by itself is merely a way to develop an validated abstract specification, and the software implementation itself must in many cases still be developed in traditional ways based on the specification. And so, model checking does not completely eliminate the need for rigorous testing, strong type systems and so on.

What model checking most importantly brings to the table, is a verified specification for the system to be implemented, thus a good way to implement safe systems might be to use a combination of all mentioned methods together.

Appendix A

User Guide for the Model Generating Tool

This appendix chapter serves to give a brief introduction on how to use the model generating tool developed as part of the project.

First a section that covers model generation through the compiled program is presented, and after that a section which covers how to compose a model through a script. At short guide on how to model check the generated models is presented.

A.1 Model generation through the model generator tool

Generating a model with the model generator tool, requires either Linux with the open source .Net platform Mono or a Windows platform with .Net. Furthermore does the tool require that the user has an XML file of the type generated from the LRVT tool set mentioned in chapter 7.

In the following examples it will be assumed that the user is using the Mono platform to execute the tool, and the examples will use the sample.xml file from

Appendix G.

To generate a model, the user must first decide upon a set of routes which the model should evolve around. Examining the layout and routes listed in Appendix G, we decide to make a route that goes from b10 to t14 and another route that goes from t14 to t20.

Examining the route lists and markerboard definitions in the XML file, we conclude that a route from b10 to t14 can be composed of the two routes with ids 'r_1a' and 'r_4_', and furthermore that the route from t14 to t20 is defined by the route with id 'r_5a'.

An UMC model with the chosen routes can now be generated by executing following command.

```
mono MiniModelGenerator.exe sample.xml umc [r_1a,r_4_] [r_5a]
```

If everything goes right, the UMC model will be written out in the console. To save it in a file, you can simply use the Linux pipeline operator '>' to pipe the resulting model into an output file.

A.2 Model generation using the scripting tools

There are multiple ways of generating a model from a script, and in fact the user has the full freedom of the F# core libraries at his disposal when creating scripts since the scripts are just normal F# scripts. This has indeed been exploited when generating multiple models for the experiments (see the experiments scripts in Appendix F).

However, the scripting tools also defines a very simple set of types that can be used like a simple DSL to specify a model, furthermore is it possible to load a layout from an XML file and use that in a script as well. These two approaches will be described here.

The scripts are executed using the F# interactive program which is bundled with all installations of F#, and is usually a program called *fsharpi*.

When creating a new script, it must have the file extension of '.fsx', and in the first lines of the script one must import the tools and types to be used.

A Prelude.fsx script has been created with the purpose of simplifying the process of creating new scripts. Loading the Prelude script will simply cause the required files to be loaded. (Note that the new script must be defined at the same location as the Prelude script). Next the namespaces *InterlockingModel* and *ScriptingTools* must be imported. Thus a basic starting script looks as follows.

```
    (* loading the prelude script *)
    #load "Prelude.fsx"
    (* importing required modules *)
    open InterlockingModel
    open ScriptingTools
```

The type like used in scripts to describe models, is presented below.

```
type SimpleTrackSegment = LLinear of name : string
1
\mathbf{2}
                             LPointFork of name : string *
                                  PointPosition
                               LPointStem of name : string
3
4
   let (+>) (el1 : SimpleTrackSegment) (el2 : SimpleTrackSegment) =
       el1, el2
5
   type SimpleLayout = (SimpleTrackSegment * SimpleTrackSegment) list
6
7
   type SimpleRouteElement =
8
        RLinear of name : string * length : int
9
         RPoint of name : string * position : PointPosition
   type SimpleRoute = SimpleRouteElement list
10
11
   type SimpleTrain =
12
       { id : string
13
        ; length : int
14
        ; route : SimpleRoute
15
        ; route direction : RouteDirection }
16
   type Simple \overline{T}rains = Simple Train list
17
18
   type Layout Type = CustomLayout of SimpleLayout
19
20
                     | XMLLayout of path : string
21
22
   type SimpleModelArgs =
23
       { trains : SimpleTrain list
        ; layout : LayoutType
24
        ; show_stats : bool
25
26
        ; output file : string option }
```

The script tools furthermore exposes two simple functions to be used by a user.

printRawLayout(path:string) $generateUMCModel(model_args:SimpleModelArgs):unit$

The *printRawLayout* permits the user to explore the layout in an XML file, by printing out a simple representation of the layout in the same format as layouts can be defined by the user. The function *generateUMCModel* takes record of

arguments as input, and based on the requirements specified in the record, the function will generate a model.

An example of using the printRawLayout in a file script.fsx is illustrated in the following listing (using the sample.xml file)

```
    #load "Prelude.fsx"
    open InterlockingModel
    open ScriptingTools
    let path = "sample.xml"
    printRawLayout path
```

Executing this file with the F# interactive *fsharpi* program.

fsharpiscript.fsx

Prints following output in the console.

```
LLinear "b10"
                            <+> LLinear "t10"
1
   LLinear "t10"
                            <+> LPointStem "t11"
2
   LLinear "t12"
                            <+> LPointFork ("t13", Plus)
3
   LLinear "t14"
                            <+> LLinear "b14"
4
   LLinear "t20"
                            <+> LPointFork ("t13", Minus)
5
   LPointStem "t11"
                            <+> LLinear "t10"
6
   LPointStem "t13"
                            <+> LLinear "t14"
7
   LPointFork ("t11", Plus) <+> LLinear "t12"
8
   LPointFork ("t11", Minus) <+> LLinear "t20"
9
   LPointFork ("t13", Plus) <+> LLinear "t12"
10
   LPointFork ("t13", Minus) <+> LLinear "t20"
11
```

Which illustrates the connections between linear segments (LLinear), point stems (LPointStem) and point forks (LPointFork). It is now trivial to look at the mappings and choose a route in the layout.

Based on the presented layout, a user could for example decide to define a route from "b10" to "t14", going through the elements "b10", "t10", "t11", "t12", "t13" and "t14". And another route from "b14" to "t20", going through "b14", "t14", "t13" and "t20". These routes must now each be defined for a train and the user must decide the lengths of the train and segments.

The user can define a train using the record type Simple Train.

```
1 { id = "1"
2 ; length = 3
3 ; route = [ RLinear(name = "b10", length = 3)
4                      ; RLinear(name = "t10", length = 3)
5                     ; RPoint(name = "t11", position = Plus)
6                      ; RLinear(name = "t12", length = 3)
7                    ; RPoint(name = "t13", position = Plus)
```

```
8  ; RLinear(name = "t14", length = 3) ]
9 ; route_direction = Up }
```

Here the user have chosen that the length of the modeled train should be a value of three and all its linear segments likewise, furthermore has the user decided that the route should go in the Up direction, since the route connects left to right in the described layout. Furthermore, has the user determined the required positionings of the points should both be *Plus*.

The user chooses to define the other train with a length of two and assigns it to the remaining route.

```
1 { id = "2"
2 ; length = 2
3 ; route = [ RLinear(name = "b14", length = 2)
4                            ; RLinear(name = "t14", length = 2)
5                            ; RPoint(name = "t13", position = Minus)
6                             ; RLinear(name = "t20", length = 2) ]
7 ; route_direction = Down }
```

The two train definitions can simply be represented together as a list, as follows.

```
let trains : SimpleTrains = [
 1
        \{ id = "1" ; length = 3 \}
\mathbf{2}
        ; route = [ RLinear(name = "b10", length = 3)
3
                       ; RLinear (name = "t10", length = 3)
 4
                       ; RPoint (name = "t11", position = Plus)
; RLinear (name = "t12", length = 3)
 5
 6
                       ; RPoint (name = "t13", position = Plus)
; RLinear(name = "t14", length = 3) ]
7
8
          route_d
id = "2"
                    direction = Up }
9
        :
10
        {
11
        ; length = 2
        ; route = [ RLinear(name = "b14", length = 2)
; RLinear(name = "t14", length = 2)
12
13
                       ; RPoint (name = "t13", position = Minus)
; RLinear (name = "t20", length = 2) ]
14
15
16
        ; route direction = Down } ]
```

At last to produce an UMC model, the user can apply the trains together with a set of arguments in a record to the function *generateUMCModel*, as follows.

```
1 generateUMCModel {
2 trains = trains
3 layout = XMLLayout path
4 show_stats = true
5 output file = Some "mymodel.txt" }
```

Here the input arguments to the functions specifies that the defined trains should be used, the layout should be extracted from an XML file previously specified by the path value. Furthermore does the inputs describe that a set of summary statistics must be shown together with the model that has been generated, and at last that the resulting model should be saved to the file "mymodel.txt". If a None type was given instead of a Some type with a filename, the script would simply print the model to the console instead of saving it to a file.

Composing all the described script fragments into one script, results in the following script.

```
#load "Prelude.fsx"
1
   open InterlockingModel
\mathbf{2}
   open ScriptingTools
3
   let path = "sample.xml"
4
    printRawLayout path
5
6
   let trains : SimpleTrains = [
        \{ id = "1" ; length = 3 \}
7
        ; route = [ RLinear(name = "b10", length = 3)
8
                   ; RLinear(name = "t10", length = 3)
9
                   ; RPoint (name = "t11", position = Plus)
; RLinear(name = "t12", length = 3)
10
11
                    ; RPoint (name = "t13", position = Plus)
12
                    ; RLinear(name = "t14", length = 3)
13
        ; route direction = Up }
14
        \{ id = "2" \}
15
16
        ; length = 2
        ; route = [ RLinear(name = "b14", length = 2)
17
                   ; RLinear(name = "t14", length = 2)
18
                    ; RPoint (name = "t13", position = Minus)
19
                    ; RLinear (name = "t20", length = 2)
20
        ; route direction = Down } ]
21
   generateUMCModel {
22
        trains = trains
23
        layout = XMLLayout path
24
        show stats = true
25
        output file = Some "mymodel.txt" }
26
```

And executing the script using the F# interactive program results in the following output.

```
LLinear "b10"
                                <+> LLinear "t10"
 1
   LLinear "t10"
                                <+> LPointStem "t11"
2
   LLinear "t12"
                                <+> LPointFork ("t13", Plus)
3
   LLinear "t14"
                                <+> LLinear "b14"
 4
   LLinear "t20"
                                <+> LPointFork ("t13", Minus)
5
   LPointStem "t11"
                                <+> LLinear "t10"
\mathbf{6}
                                <+> LLinear "t14"
   LPointStem "t13"
7
   LPointFork ("t11", Plus) <+> LLinear "t12"
8
   LPointFork ("t11", Minus) <+> LLinear "t20"
9
   LPointFork ("t13",Plus) <+> LLinear "t12"
LPointFork ("t13",Minus) <+> LLinear "t20"
10
11
   model written to file mymodel.txt
12
```

(Note that it is not required to print the layout again)

The script could also have been defined such that a custom layout is defined in the script. In that case, the script could instead look as follows.

```
#load "Prelude.fsx"
 1
   (* importing required modules *)
2
 3
   open InterlockingModel
 4
   open ScriptingTools
5
 6
   let network : SimpleLayout =
        [ LLinear "1"
                                   <+> LPointFork("1", Plus)
7
                                   <+> LPointFork ("1", Minus)
          LLinear "3"
8
          LPointStem "1"
                                   <+> LPointStem "2"
9
          LPointFork("2", Plus) <+> LLinear "2"
10
          LPointFork ("2", Minus) <+> LLinear "4"
11
12
   let trains : SimpleTrains =
13
        [ \{ id = "1" \}
14
15
          ; length = 2
          ; route = [ RLinear("1", 2)
16
                       RPoint("1", Plus)
17
                       RPoint ("2"
                                  , Plus)
18
                       RLinear ("2", 2)
19
20
          ; route direction = Up }
          \{ id = "2" \}
21
          ; length = 3
22
          ; route = [ RLinear("3", 3)
23
                       RPoint("1", Minus)
24
                       RPoint ("2", Minus)
25
                       RLinear("4", 3)]
26
27
          ; route direction = Up } ]
28
29
    generateUMCModel { trains = trains
                      ; layout = CustomLayout (network)
30
                      ; show stats = true
31
                      ; output file = Some "mymodel.txt" }
32
```

Notice that for this script the layout argument for the generateUMCModel function is of of type CustomLayout, and in the previous script the type XMLLayout was used.

The produced delta (-omitting the generic classes) of the model, is presented in following listing.

```
STATS:
1
2
  \{\text{num of trains} = 2;
    train lengths = [2; 3];
3
4
    route lengths = [4; 4];
    total route sub segments = 14;
5
6
    total linears = 4;
7
    total points = 2;
8
    shared points = 2;
```

```
9
     shared linears = 0;
10
11
    MODEL:
12
13
    ... omitted ....
14
15
    Objects
     train 1: Train(
16
    route segments \Rightarrow [linear 1, point 1, point 2, linear 2],
17
    \operatorname{track} lengths \Longrightarrow [2,1,1,2],
18
    train length \Rightarrow 2,
19
    occupies \Rightarrow [linear 1, linear 1],
20
    requested point positions => [null, True, True, null]);
21
22
    train 2: Train(
23
    route segments \Rightarrow [linear 3, point 1, point 2, linear 4],
^{24}
    track lengths => [3, 1, 1, 3],
25
    train length => 3,
26
    occupies => [linear_3, linear_3, linear_3],
27
    requested point positions => [null, False, False, null]);
^{28}
^{29}
    linear 1: Linear(train \Rightarrow train 1);
30
31
    linear 2: Linear(train \Rightarrow null);
32
33
    linear 3: Linear(train \Rightarrow train 2);
34
35
36
    linear 4: Linear(train => null);
37
38
    point 1: Point;
39
    point 2: Point;
40
    Abstractions {
41
    State: inState(train 1.ARRIVED) -> train 1 arrived
42
    State: inState(train_2.ARRIVED) -> train_2_arrived
43
    State: point 1 train = null -> no train on point 1
44
    State: point 2.train = null -> no train on point
                                                                 2
45
    State: inState(point_1.POSITIONING) -> positioning_point
State: inState(point_2.POSITIONING) -> positioning_point_
46
47
    State: point_1.current_position = True -> point_1_in_plus
48
    State: point_2.current_position = True -> point_2_in_plus
State: point_1.current_position = True -> point_1_in_minus
49
50
    State: point 2.current position = True -> point 2 in minus
51
    State: train 1.occupies [0] /= train 2.occupies [0] and
52
    train 1 occupies[0] /= train 2 occupies[1] and
53
    train 1. occupies [0] /= train 2. occupies [2] and
54
    train 1 \cdot \text{occupies} \begin{bmatrix} 1 \end{bmatrix} = \text{train} 2 \cdot \text{occupies} \begin{bmatrix} 0 \end{bmatrix} and
55
    train 1.occupies [1] /= train 2.occupies [1] and
56
    train 1. occupies [1] /= train 2. occupies [2] ->
57
         trains_at_diff_positions
    State: train 1.occupies[0] /= point 1 and
58
    train 1.occupies [1] /= point 1 -> train 1 not on point 1
59
    State: train 1.occupies [0] /= point 2 and
60
    train 1. occupies [1] /= point 2 -> train 1 not on point 2
61
62
    State: train 2.occupies [0] /= point 1 and
```

```
train 2.occupies[1] /= point 1 and
63
  train 2.occupies [2] /= point 1 -> train 2 not on point 1
64
65 State: train 2. occupies [0] /= point 2 and
66 train 2 occupies [1] \neq point 2 and
   train 2.occupies [2] /= point 2 -> train 2_not_on_point 2
67
   Action: lostevent -> discarded message
68
69
   }
70
71
   --- safety property:
   -- no incident
72
   --- no trains occupy the same location node at the same time
73
   AG (trains at diff positions);
74
75
   --- safety property:
76
   --- no trains are located at any 'point' while it is changing its
77
       position
   AG (positioning point 1 implies no train on point 1 and
78
   positioning point 2 implies no train on point 2);
79
80
   -- property to verify that all trains are correctly detected at
81
        points
   AG ((not (train 1 not on point 1 and train 2 not on point 1)
82
        implies not no_train_on_point_1) and
   (not (train 1 not on point 2 and train 2 not on point 2) implies
83
       not no train on point 2));
84
   -- progress property that specifies that
85
   -- all trains has arrived at their destinations
86
   EF AG (train 1 arrived and train 2 arrived);
87
88
   --- no signal is ever lost in the system
89
   AG not (EX {discarded message} true);
90
```

As can be seen in the above listing, the stats are presented at the beginning followed by the generic model which has been omitted for the presented code, and thereafter comes the object instantiations, abstraction definitions and at last the properties for the generated model.

A.3 Model checking the generated models with the UMC web tool

The produced model from a script or from the tool program, can now be model checked with the UMC model checking tool.

This tool is exposed as a service at the site http://fmt.isti.cnr.it/umc/V4. 2/umc.html. When entering the site, choose 'Model Definition' from the menu at the left, and after that choose 'Edit a new Model' from the new menu point. An online editor is now displayed in the browser with an existing model skeleton. Delete the skeleton before proceeding. After deleting the skeleton open the generated model file and copy everything after the **MODEL**: except for the properties at the end of the file. Insert the model into the online editor and click the 'Load Current Model' button.

When the model is done loading, a new menu is presented and options for exploring the model are shown. To model check the generated properties of the generated model, simply copy the properties from the file containing the model, and click the 'Modelcheck L2TS ..' button. A small box opens at the bottom of the screen. Paste in the properties into the box and click the 'Check the Formula' button on the right side of the screen. Now all the properties will be model checked for the given model, and if they are all evaluated to be true, then the model has been verified with regards to the given properties. In the event that one or more properties evaluates to false, then the model has failed the verification. In this case it is possible to get a trace to the failing states by clicking the 'Explain the Result' button at the right side of the screen.

Appendix B

UMC BNF

This Appendix chapter presents the BNF grammar for the UMC modeling language.

The BNF is extracted from the UMC User Guide and presented here for completeness.[Maza]

{item} denotes 0 or more occurrences of the item
[item] denotes 0 or 1 occurrence of the item
"item" denotes a terminal character sequence
"item | item " denotes indicates alternative items

```
1
\mathbf{2}
   Model ::= { Class } { Object }
3
    Class ::= "class" ClassName "is"
4
                  [ "Signals"
5
                  Signal, {"," Signal} ]
6
                   "Operations" Operation, {"," Operation} ]
7
                  [ "Vars" Attribute {"," Attribute}]
[ "State" "top" "=" Composite
8
9
                  {"State" Statepath "=" State } ]
10
                  [ "Transitions" {Transition} ]
11
                  "end;" [ClassName]
12
13
   Signal ::= SignalName ["(" ParamName [":" TypeName]
14
                         {"," ParamName [":" TypeName] }
")" ]
15
16
```

```
Operation ::= OpName ["(" Name [":" TypeName]
18
                          {"," Name [":" TypeName] }
19
                           ")" ] [ ":" TypeName]
20
21
    Attribute ::= AttrName [":" TypeName] [":=" StaticExpr ] ";"
22
23
   State ::= Composite | Parallel
^{24}
25
    Composite ::= StateName { "," StateName}
26
27
                     ["Defers" Defer {"," Defer } ]
28
29
    Parallel ::= Name { "/" Name}
                     ["Defers" Defer {"," Defer }]
30
31
   StateName ::= Name | "final" | "initial"
32
33
    Defer ::= EventName ["(" ParamName {"," ParamName } ")"]
34
35
    Transition ::= Statepaths "-(" Trigger[Guard] ["/" Actions] ")->"
36
        Statepaths
37
   Statepaths ::= Statepath | "(" Statepath {"," Statepath} ")"
38
39
   Statepath ::= ["top."] Name { "." Name}
40
41
   Trigger ::= "-" | EventName ["(" ParamName {"," ParamName } ")"]
42
43
   Guard ::= "[" BoolBoolExpr "]"
44
45
    Actions::= [ Stm \{"; " Stm\} ]
46
47
   Object ::= "Object" ObjName ":" ClassName [ Initializations ]
48
49
    Initializations ::= "(" AttrName "=>" StaticExpr
50
                          { "," AttrName "=>" StaticExpr } ")"
51
52
   - - action statements
53
54
   Stm ::= Assignment
55
            SignalSending
56
            OperationCall
57
            FunctionCall
58
            ConditionalStm
59
60
            LoopStm
            VarDecl
61
            ReturnStm
62
            ExitStm
63
64
   Assignment ::= TargetExpr ":=" Expr
65
66
   SignalSending ::= ObjExpr "." SignalName ["(" Expr {"," Expr} ")"]
67
68
    OperationCall ::= ObjExpr "." OpName ["(" Expr {"," Expr} ")"]
69
70
```

17

```
71
    FunctionCall ::= TargetVar ":=" ObjExpr "." OpName ["(" Expr {","
        Expr } ")"]
72
    ConditionalStm ::= "if" BoolBoolExpr [ "then" ] "{" Actions "}" [
73
        "else {" Actions "}" ]
74
    LoopStm ::= "for" LoopIndex "in" IntExpr ".." IntExpr "{" Actions
75
        "}"
76
    VarDecl ::= VarName ":" TypeName
77
78
    ReturnStm ::= "return" ["(" Expr \{ ", " Expr \} ")"]
79
80
    ExitStm ::= "exit"
81
82
    TargetExpr ::= AttrName [ Selection ] | VarName [Selection]
83
84
    Selection ::= "[" IntExpr "]"
85
86
    - - names and expressions
87
88
    Expr ::= "("Expr")" | BoolBoolExpr | IntExpr | ObjExpr | VectorExpr
89
90
    BoolBoolExpr ::= BoolExpr {"and" BoolExpr}
91
                     BoolExpr {"or" BoolExpr}
92
                      "not" BoolExpr
93
                     BoolExpr
94
95
    BoolExpr ::= "true" | "false"
96
                 AttrName [Selection] | VarName [Selection]
97
                 Expr "=" Expr
-98
                Expr "/=" Expr
-99
                IntExpr relop IntExpr
100
101
    ObjExpr ::= "null" | AttrName [Selection]| VarName [Selection]
102
               | ObjName | "self" | "this"
103
104
    IntExpr ::= Number | AttrName [Selection] | VarName [Selection]
105
               | (Intexpr intop IntExpr ")" | VectorExpr ".head"
106
107
    VectorExpr ::= "[]" | AttrName | VarName | VectorExpr "+"
108
         VectorExpr
                  VectorExpr ".tail"
109
110
    StaticExpr ::= Number | ObjName | "null" | "self" | "this"
111
112
    relop ::= ">" | ">=" | "<" | "<="
113
114
    intop ::= "+" | "-" | "*" | "/" | "mod"
115
116
    TypeName ::= "int" | "bool" | "obj" | ClassName
117
                  "int [] " | "bool [] " | "obj [] " | ClassName" [] "
118
```

Appendix C

Generic UMC Model

This chapter contains the source code for the three generic classes that together defines the modeled concept.

```
1
   Class Train is
2 Signals: ok, no;
3
4
   Vars:
  requested point positions : bool [];
5
  train length : int = 2; - how many track segments does the train occupy
6
7 route segments : obj[];
8 route index : int := 0; -- current location on the route
   occupies : obj []; - - the tc and pt objects which the train currently occupies
9
   front advancement count : int; -- a variable for keeping track of the trains front
10
         advancement over a track
    track lengths : int []; -- same number of elements as route segments
11
12
13
   State Top = READY, WAIT OK, MOVEMENT, ARRIVED
14
    Transitions:
15
   - - send out initial reservation request to the first node on route
16
   READY -> WAIT OK {
17
18
      - /
      route segments [0] req(self, 0, route segments,
19
           requested point positions);
   }
20
21
22
   - - when the train reservation is rejected we just keep cycling between
         WAIT OK and READY
```

```
23
   WAIT OK \rightarrow READY { no }
^{24}
25
    - - train receives acknowledgment that the route has been reserved successfully
   -- the front advancement count variable is initialized to reflect the
26
        trains front location on the track
   WAIT OK -> MOVEMENT { ok / front advancement count := train length
27
        -1;
28
   MOVEMENT \rightarrow MOVEMENT {
29
30
31
    [not (route index = route segments.length -1 and
      track lengths [route index] -1 = front advancement count)] / -- at
32
           end \ of \ track
      at end of track: bool := track lengths[route index] - 1 =
33
          front advancement count; -- determine if we have reached the end of the
          current \ track
      if at end of track = true then \{ -- the train has reached the end of its
34
          current track
        front advancement count := 0;
35
        if route_index < route_segments.length -1 then { -- the
36
             route index is not the last
37
           - - train enters next track
           route index := route index + 1;
38
           route segments [route index] sensorOn (self); - the next track
39
               detects the train
40
        };
      } else {
41
        front advancement count := front advancement count + 1;
42
43
      };
      - - update the occupies array
44
      rear: obj := occupies.head;
45
      next_rear: obj := occupies.tail.head;
46
      occupies := occupies.tail + [route segments[route index]];
47
      if rear != next rear then { - determine if the rear of the train has left a track
48
        rear.sensorOff(self); -- the past track detects that the train does not occupy it
49
             anymore
      };
50
    }
51
52
   MOVEMENT -> ARRIVED {
53
54
    [route index = route segments.length -1 and -at last track segment of
55
        route
      track lengths [route index] -1 = front advancement count] - at end
56
          of track
    }
57
   end Train
58
59
60
    Class Linear is
61
    Signals:
62
    req(sender: obj, route index: int, route elements: obj[],
63
        requested point positions: bool[]);
    ack(sender: obj);
64
    nack(sender: obj);
65
```

```
commit(sender: obj);
66
     agree(sender: obj);
67
68
    disagree(sender: obj);
69
70
    Operations:
    sensorOn(sender: obj);
71
72
    sensorOff(sender: obj);
73
74
    Vars:
    next: obj;
75
    prev: obj;
76
    train: obj := null;
77
78
    State Top = NON RESERVED, WAIT ACK, WAIT COMMIT, WAIT AGREE,
79
         RESERVED, TRAIN IN TRANSITION
80
81
     Transitions
    - - first node receive request
82
    NON RESERVED -> WAIT ACK {
83
       req(sender, route index, route elements,
84
           requested point positions)
       [route index = 0 and sender = train and route_elements.length >
85
           0] /
86
       prev := null;
       next := route elements [1];
87
       next.req(self, 1, route elements, requested point positions);
88
    }
89
90
91
    - - intermediate node receive request
    NON RESERVED -> WAIT ACK {
92
       req(sender, route_index, route_elements,
93
           requested point positions)
       [train = null and (route_index > 0 and route_index+1 < 
94
           route elements.length) / /
       prev := route_elements[route_index - 1];
95
       next := route_elements[route_index + 1];
next.req(self, route_index + 1, route_elements,
96
97
           requested point positions);
     }
98
99
100
    - - initial reservation request for last node
    - - starts ack phase
101
    NON RESERVED -> WAIT COMMIT {
102
       req(sender, route index, route elements,
103
           requested point positions)
       [train = null and route_elements.length = route_index+1] /
104
       prev := route elements [route index -1];
105
       next := null;
106
107
       prev.ack(self);
     }
108
109
110
    - - intermediate node receive ack
    WAIT ACK -> WAIT COMMIT {
111
112
       ack (sender)
       [prev /= null] /
113
```

```
prev.ack(self);
114
     }
115
116
    - - first node receive ack
117
118
    - - and starts commit phase
    WAIT ACK -> WAIT AGREE {
119
120
       ack (sender)
121
       [prev = null] /
122
       next.commit(self);
     }
123
124
    - - intermediate node receives commit
125
    WAIT COMMIT -> WAIT AGREE {
126
       commit (sender)
127
       [next /= null]
128
       next.commit(self);
129
     }
130
131
    - - last node receive commit
132
    - - and starts agree phase
133
    WAIT COMMIT -> RESERVED {
134
135
       commit (sender)
       [next = null] /
136
       prev.agree(self);
137
     }
138
139
140
    - - intermediate node receive agree
     WAIT AGREE -> RESERVED {
141
       agree(sender)
142
143
       [prev /= null]
       prev.agree(self);
144
145
     }
146
    - - first node receive agree
147
    - - and sends ok to the train
148
     WAIT AGREE -> TRAIN IN TRANSITION {
149
       agree(sender)
150
       [prev = null and train /= null] /
151
       train.ok;
152
     }
153
154
    - - train moves onto current node
155
     RESERVED -> TRAIN IN TRANSITION {
156
       sensorOn(sender) /
157
158
       train := sender;
     }
159
160
     - - sequential release
161
162
    - - reset train
     TRAIN_IN_TRANSITION \rightarrow NON_RESERVED {
163
       sensorOff(sender) /
164
       train := null;
165
     }
166
167
168
    - - nack received
```
```
169
     - - forwards and goes into non-reserved
     WAIT ACK -> NON RESERVED {
170
171
       nack(sender) /
        if prev = null then { -- is first node on itinerary
172
173
          train.no
        } else { -- is not first node
174
175
          prev.nack(self)
176
        };
177
     }
178
     - - disagree received
179
180
     - - forwards and goes into non-reserved
     WAIT COMMIT -> NON RESERVED {
181
182
        disagree(sender)
        if next /= null then { -- not last node on itinerary
183
          next.disagree(self)
184
185
        };
186
     }
187
188
     - - disagree received
     - - forwards and goes into non-reserved
189
     WAIT AGREE -> NON RESERVED {
190
        disagree(sender) /
191
        if prev /= null then { -- not first node on itinerary
192
193
          prev.disagree(self)
        } else { -- is first node
194
          train.no
195
        };
196
     }
197
198
     - - disagree received
199
     - - forwards (if there is someone to forward to) and goes into non-reserved
200
     RESERVED -> NON RESERVED {
201
        disagree(sender)
202
        if next /= null then { -- not last node on itinerary
203
204
          next.disagree(self)
205
        };
     }
206
207
208
     - - reservation request received
209
     - - however a train is already on the track, so a nack is returned to sender
    NON RESERVED -> NON RESERVED {
210
        req(sender, route index, route elements,
211
       requested point positions)
[train /= null and sender /= train] /
212
213
        sender.nack(self);
214
     }
215
216
     - - reservation request received
     - - however, the node is already in wait-ack, so it returns a nack to sender
217
     WAIT ACK -> WAIT ACK {
218
        req(sender, route index, route elements,
219
            requested point positions) /
220
        sender.nack(self);
     }
221
```

```
223
     - - reservation request received
224
    - - however, the node is already in wait-commit, so it returns a nack to sender
    WAIT COMMIT -> WAIT COMMIT {
225
       req(sender, route index, route elements,
226
            requested point positions) /
227
       sender.nack(self);
228
     }
229
    - - reservation request received
230
    - - however, the node is already in wait-agree, so it returns a nack to sender
231
    WAIT AGREE -> WAIT AGREE {
232
       req(sender, route_index, route_elements,
233
            requested point positions) /
234
       sender.nack(self);
     }
235
236
237
    - - reservation request received
    - - however, the node is already reserved, so it returns a nack to sender
238
    RESERVED -> RESERVED {
239
       req(sender, route index, route elements,
240
            requested point positions) /
       sender.nack(self);
241
     }
242
243
244
    - - reservation request received
245
    - - however, a train is in transition on the node, so it returns a nack to sender
     TRAIN IN TRANSITION -> TRAIN IN TRANSITION {
246
       req(sender, route index, route elements,
247
            requested point positions) /
       sender.nack(self);
248
     }
249
     end Linear
250
251
252
     - - points are always intermediate nodes
253
254
     - - so we don't need to check if they are first or last in the guards
     Class Point is
255
     Signals:
256
     req(sender: obj, route_index: int, route_elements: obj[],
257
          requested point positions: bool[]);
     ack(sender: obj);
258
     nack(sender: obj);
259
260
     commit (sender: obj);
261
     agree(sender: obj);
     disagree(sender: obj);
262
263
     Operations:
264
265
     sensorOn(sender: obj);
     sensorOff(sender: obj);
266
267
     Vars:
268
     next: obj;
269
270
     prev: obj;
     requested position: bool;
271
```

222

```
272
     current position: bool := True;
     train: obj := null;
273
274
     State Top = NON RESERVED, WAIT ACK, WAIT COMMIT, WAIT AGREE,
275
         POSITIONING, RESERVED, TRAIN IN TRANSITION, MALFUNCTION
276
277
     Transitions:
278
    - - initial reservation request
279
    NON RESERVED -> WAIT ACK {
       req (sender, route index, route elements,
280
            requested point positions) /
       prev := route elements [route index -1];
281
282
       next := route_elements[route_index + 1];
       requested position := requested point positions[route index];
283
       next.req(self, route index + 1, route elements,
284
            requested point positions);
285
     }
286
     - - receiving and forwarding ack
287
    WAIT ACK -> WAIT COMMIT {
288
       ack(sender) /
289
290
       prev.ack(self);
     }
291
292
293
    - - receiving and forwarding commit
    WAIT COMMIT -> WAIT AGREE {
294
295
       commit(sender) /
296
       next.commit(self);
     }
297
298
     - - if the point is positioned as required for the given route reservation
299
300
    - - receiving and forwarding agree
     WAIT AGREE -> RESERVED {
301
302
       agree (sender)
       [current_position = requested position]/
303
       prev.agree(self);
304
     }
305
306
     - - if the point is not positioned as required for the given route
307
    - - goes into positioning state
308
     WAIT AGREE -> POSITIONING {
309
       agree (sender)
310
       [current position /= requested position] /
311
312
313
     }
314
315
     - - successfully performing positioning
     POSITIONING -> RESERVED {
316
317
       - /
       current_position := not current_position;
318
319
       prev.agree(self);
     }
320
321
322
     - - simulating sudden malfunction of positioning system
    - - and sending disagrees to neighbor nodes
323
```

```
324
     POSITIONING -> MALFUNCTION {
325
       - /
326
       prev.disagree(self);
       next.disagree(self);
327
     }
328
329
330
    - - train moves onto current node
    RESERVED -> TRAIN IN TRANSITION {
331
       sensorOn(sender) /
332
333
       train := sender;
334
     }
335
336
    - - sequential release
    - - reset all train
337
    TRAIN IN TRANSITION \rightarrow NON_RESERVED {
338
       sensorOff(sender) /
339
       - - [sender = train]
340
       train := null;
341
     }
342
343
    - - nack received and forwarded
344
    WAIT ACK -> NON RESERVED {
345
       nack(sender) /
346
       prev.nack(self);
347
     }
348
349
    - - disagree received and forwarded
350
351
    WAIT COMMIT -> NON RESERVED {
        disagree (sender)
352
353
       next.disagree(self);
     }
354
355
    - - disagree received and forwarded
356
    WAIT AGREE -> NON RESERVED {
357
        disagree(sender) /
358
        prev.disagree(self);
359
     }
360
361
     - - disagree received and forwarded
362
     POSITIONING -> NON RESERVED {
363
        disagree (sender)
364
365
       next.disagree(self);
     }
366
367
368
     - - disagree received and forwarded
     RESERVED -> NON RESERVED {
369
        disagree(sender) /
370
       next.disagree(self);
371
     }
372
373
     - - reservation request received
374
    - - however, the node is already in wait-ack, so it returns a nack to sender
375
    WAIT ACK -> WAIT ACK {
376
        req(sender, route index, route elements,
377
            requested point positions) /
```

```
378
       sender.nack(self);
     }
379
380
     - - reservation request received
381
382
    - - however, the node is malfunctioning
    MALFUNCTION -> MALFUNCTION {
383
384
       req(sender, route index, route elements,
            requested point positions) /
385
       sender.nack(self);
     }
386
387
388
    - - reservation request received
    - - however, the node is already in wait-commit state and returns nack to the sender
389
    WAIT\_COMMIT -> WAIT\_COMMIT 
390
       req(sender, route index, route elements, requested position) /
391
       sender.nack(self);
392
     }
393
394
     - - reservation request received
395
396
    - - however, the node is already in wait-agree state and returns nack to the sender
    WAIT AGREE -> WAIT AGREE {
397
       req(sender, route index, route elements, requested position) /
398
399
       sender.nack(self);
     }
400
401
402
    - - reservation request received
     - - however, the node is already in positioning state and returns nack to the sender
403
     POSITIONING -> POSITIONING {
404
       req(sender, route index, route elements, requested position) /
405
406
       sender.nack(self);
     }
407
408
     - - reservation request received
409
    - - however, the node is already reserved and returns nack to the sender
410
     RESERVED -> RESERVED {
411
       req(sender, route index, route elements, requested position) /
412
       sender.nack(self);
413
     }
414
415
     - - reservation request received
416
     - - however, the node is occupied by a train and returns nack to the sender
417
     TRAIN IN TRANSITION -> TRAIN IN TRANSITION {
418
       req(sender, route index, route elements, requested position) /
419
       sender.nack(self);
420
```

```
421
       }
```

```
end Point
422
```

Appendix D

UMC model delta

Example of the appended delta part of a concrete UMC model generated by the tool.

In the generated model, the presented code would be appended to the code from the previous appendix chapter, thus the code presented here can be seen as a delta of a generated model.

```
Objects
1
      train 0: Train(
2
3
         route segments =>
             [linear b10, linear t10, point t11, linear t12, point t13, linear t14],
         t \operatorname{rack} lengths => [2, 2, 1, 2, 1, 2],
\mathbf{4}
         train \ length \implies 2,
\mathbf{5}
6
         occupies \Rightarrow [linear b10, linear b10],
         requested point positions => [null, null, True, null, True, null]);
\overline{7}
8
      train_1: Train(
9
         route\_segments \Rightarrow [linear b14, linear t14, point t13, linear t20],
10
        11
12
         occupies \Rightarrow [linear b14, linear b14],
13
         requested point positions => [null, null, False, null]);
14
15
16
      linear b10: Linear (train => train 0);
17
      linear b14: Linear (train => train 1);
18
19
      linear t10: Linear (train \Rightarrow null);
20
```

```
22
      linear t12: Linear (train \Rightarrow null);
23
      linear t14: Linear(train => null);
24
25
      linear t20: Linear(train => null);
26
27
28
      point t11: Point;
29
      point t13: Point;
30
31
    Abstractions {
32
33
      State: inState(train 0.ARRIVED) -> train 0 arrived
      State: inState(train_1 ARRIVED) -> train_1 arrived
34
35
      State: point t11.train = null -> no_train_on_point_t11
36
      State: point t13.train = null \rightarrow no train on point t13
37
38
      State: inState(point t11.POSITIONING) \rightarrow positioning point t11
39
      State: inState(point t13.POSITIONING) -> positioning point t13
40
41
      State: point t11.current position = True -> point t11 in plus
42
      State: point t13.current position = True -> point t13 in plus
43
      State: point t11.current position = False -> point t11 in minus
44
      State: point t13.current position = False -> point t13 in minus
45
46
      State: inState(point t11.MALFUNCTION) -> point_t11_malfunction
47
      State: inState(point t13.MALFUNCTION) -> point t13 malfunction
48
49
50
      State: train 0.occupies[0] /= train 1.occupies[0] and
        train 0.occupies[0] /= train 1.occupies[1] and
51
        train 0 occupies [1] /= train 1 occupies [0] and
52
        train 0. occupies [1] /= train 1. occupies [1] \rightarrow
53
            trains at diff positions
54
      State: train 0.occupies[0] /= point t11 and
55
        train 0.\text{occupies}[1] /= point t11 -> train 0 not on point t11
56
57
      State: train 0.occupies[0] /= point t13 and
58
        train 0.\text{occupies}[1] /= point t13 -> train 0 not on point t13
59
60
      State: train 1.occupies[0] /= point t11 and
61
        train 1.occupies[1] /= point t11 -> train 1 not on point t11
62
63
64
      State: train 1.occupies[0] /= point t13 and
        train 1.occupies [1] /= point t13 -> train 1 not on point t13
65
66
      Action: lostevent -> discarded message
67
   }
68
69
   - - safety property:
70
71
   - - no incident
   - - no trains occupy the same location node at the same time
72
   AG (trains_at_diff_positions);
73
74
```

21

```
75
   - - safety property:
   - - no trains are located at any 'point' while it is changing its position
76
    AG (positioning_point_t11 implies no_train_on point t11 and
77
         positioning point t13 implies no train on point t13);
78
79
80
    - - property to verify that all trains are correctly detected at points
   AG ((not (train_0_not_on_point_t11 and train_1_not_on_point_t11)
81
         implies not no train on point t11) and (not
         (train_0_not_on_point_t13 and train_1_not on point t13)
         implies not no train on point t13));
82
83
    - - progress property that specifies that
   - - all trains has arrived at their destinations
84
   EF AG (train 0 arrived and train 1 arrived);
85
86
    - - property that specifies that
87
88
   - - there does not exist a final state where at least one train has not arrived
    - - and in all states leading to this final state, no points have malfunctioned
89
    not E[not (point t11 malfunction or point t13 malfunction) U
90
         (final and not (train 0 arrived and train 1 arrived))];
91
   - - no signal is ever lost in the system
92
   AG not (EX {discarded message} true);
93
```

Appendix E

Tool Source Code

This chapter lists the source code for the implemented model generator tool and related files. All the code has been developed on a linux platform using emacs as editor and executed with Mono, however F# is primarily a .Net language, and therefore it should be possible to run the code on a windows platform with the latest Visual Studio installation. (even though this hasn't been tested)

The code also defines a small set of unit tests defined using the testing library XUnit[mad] and a few property based tests using the FsCheck[maa] library. The tests are listed last in this chapter in its own section.

E.1 Compiler version and third party packages

As mentioned, the tool has been developed on a linux platform using the open source .Net platform Mono and an fsharp compiler targeted at Mono. The tool has been developed using the following versions.

- Mono JIT compiler version 4.6.1
- F# 4.0 (Open Source Edition)

The tool utilizes a set of third party libraries which have been installed through the package .Net manager Nuget[mac]. Most notably, the package FSharp.Data[mab] has been used as it contains the F# type provider library for parsing XML files.

Following is a listing of the packages and version numbers used for this project.

- FsCheck (2.6.2)
- FsCheck.Xunit (2.6.2)
- FSharp.Data (2.3.2)
- xunit (2.1.0)
- FSharp.Core (4.0.0.1)

E.2 Auxiliary dependency files

E.2.1 Project files and compile order

F# source code files must be compiled in a certain order, this order is usually defined in a project file with the suffix 'fsproj', however these files also contains a lot of noise and irrelevant information. Here a snippet of the so called Item-Groups are listed. This information essentially contains the compile order of the source code files where the files must be compiled in the listed order.

The source code project is represented in the following listing.

```
<ItemGroup>
1
     <Compile Include="Utils.fs" />
2
     <Compile Include="InterlockingModel.fs" />
3
     <Compile Include="UMCTrainClass.fs" />
4
     <Compile Include="UMCLinearClass.fs" />
5
     <Compile Include="UMCPointClass.fs" />
6
     <Compile Include="UMC.fs" />
7
     <Compile Include="XMLExtraction.fs" />
8
9
     <Compile Include="ScriptTools.fs" />
     <Compile Include="MiniModelGenerator.fs" />
10
     <None Include="App.config" />
11
   </ItemGroup>
12
```

The test project is represented by following listing.

```
1 <ItemGroup>

2 <Compile Include="Tests.Utils.fs" />

3 <Compile Include="Tests.InterlockingModel.fs" />

4 </ItemGroup>
```

E.2.2 Sample XML file used to bootstrap the typeprovider library

See Appendix G

E.3 Source code

E.3.1 Utils.fs

```
module Utils
1
 2
 3
    open System
 4
 5
    /// Generate all unique products with values from a given list
 6
    /// where no product contains a pair of identical values
 \overline{7}
    let rec uniqueProducts (xs : 'a list) : ('a * 'a) seq = seq {
        match xs with
8
 9
        x :: x s ->
             for y in xs do
10
11
                 yield x,y
             yield! uniqueProducts xs
12
         | -> () \}
13
14
    /// Generate all cross products of two sequences
15
16
    let crossProductOfLists xs ys = seq {
        for x in xs do
17
             for y in ys do
18
19
                 yield x,y }
20
    /// Generate 'n choose k' combinations of values from list xs
21
    /// where n is length of xs and each combination is of length k
22
    let combinations (k : int) (xs : 'a list) : ('a list) seq =
23
         let rec loop (k : int) (xs : 'a list) : ('a list) seq = seq {
24
             match xs with
25
               [] -> ()
26
               xs when k = 1 \rightarrow for x in xs do yield [x]
27
28
             \mathbf{x} :: \mathbf{x} \mathbf{s} \rightarrow
                 let k' = k - 1
29
30
                 for ys in loop k' xs do
31
                      yield x :: ys
                 yield! loop k xs }
32
```

```
33
        loop k xs
        |> Seq.filter (List.length >> (=)k)
34
35
    // In F# 4.1 the Result type will be in the core library with
36
        exactly the same definition
    type Result <'success,'error> = Ok of 'success
37
38
                                    Error of 'error
39
        with
        static member map (f : 'a -> 'b) (x : Result <'a, 'error>) :
40
            Result < b, error > =
            match x with
41
             | Ok x \rightarrow Ok (f x)
42
43
             Error err -> Error err
        /// Binding value in result to parameter of a continuation
44
            function
        static member bind (x : Result <'a, 'error>) (continueationFun
45
            : 'a \rightarrow Result <'b, 'error>)
46
            : Result <'b, 'error> =
            match x with
47
             Error err -> Error err
48
             Ok x -> continueationFun x
49
50
51
   // Computation-Expression definition for the Result type.
52
    // The defined Result type has same functionality as
53
    // the more commonly known Either monad defined in Haskell and
54
        other languages.
    // The reason why it's called Result in this code, is because
55
    // (soon to-be-released) F# 4.1 will have a Result type defined in
56
        its core library.
    type ResultBuilder() =
57
        member this.Bind (x, f) = Result<_,_>.bind x f
58
        member this Return (x : 'a) : Result <'a, 'error > = Ok x
59
60
    let resultFlow = new ResultBuilder()
61
    let private traverseResults (f : 'a -> Result <'b, 'error>) (xs :
62
         'a list)
        : Result <'b list , 'error > =
63
        let folderFun (head : 'a) (tail : Result < 'b list , 'error >) :
64
            Result <'b list , 'error> =
             resultFlow { let! (h : 'b) = f head
65
                           let! (t : 'b' list) = tail
66
67
                           return h :: t }
        let initial val = Ok []
68
        // folding from right to left in order to maintain original
69
            order of the input list (xs)
        List.foldBack folderFun xs initial val
70
71
72
    let private sequenceResults (xs : Result <'a, 'error > list) :
        \operatorname{Result} <'a list , 'error> =
        traverseResults id xs
73
74
    let private reduceResults (f : 'a -> 'a -> Result <'a, 'error >) (xs
75
        : Result <'a, 'error > seq)
        : \operatorname{Result} < a, \operatorname{reror} > =
76
```

```
77
          let reducerFun = fun x y -> resultFlow {
               let ! x' = x
78
               let ! y' = y
79
               let! combined = f x' y'
 80
81
               return combined }
          xs |> Seq.reduce reducerFun
82
83
84
     let private foldResults
          (f : 'a -> 'b -> Result <'b, 'error>) (initial :
 85
               Result <'b, 'error >) (xs : 'a list)
          : \operatorname{Result} < b, \operatorname{rror} > =
 86
          let folderFun (state : Result <'b, 'error >) (x : 'a) :
 87
               \operatorname{Result} < b, \operatorname{rror} > =
               \operatorname{Result} <\_, \_>.bind state (f x)
 88
          Seq.fold folderFun initial xs
 89
90
     // Extending the Result type with a set of functions for handling
91
          Result types
     type Result with
92
          /// Applies a function ('a -> Result) on all elements in a list
93
          /// and lifts the list of results to a Result containing a list
94
          static member traverse f xs = traverseResults f xs
95
96
          /// Lifts a list of Results to a Result with a list
97
          static member sequence xs = traverseResults id xs
98
-99
          /// Reduces a list of Result < a, .. > to a Result < a, .. >
100
101
          /// using a function a \rightarrow a \rightarrow Result < a,.. >
          static member reduce f xs = reduceResults f xs
102
103
          /// Fold over a list of 'a with an initial value of 'b
104
          /// and a function 'a -> 'b -> Result <'b,..>
105
          static member fold f initial xs = foldResults f initial xs
106
107
          /// A bind operator for conveniently chaining together
108
          /// functions that produce Result types from non-Result types
109
          static member (>>=) (a: Result <'a, 'error>, f : 'a ->
110
               \label{eq:result} \begin{split} \operatorname{Result} < `b\,, \quad `error>) \ : \ \operatorname{Result} < `b\,, \quad `error> = \end{split}
               \operatorname{Result} <\_,\_>. \ bind \ a \ f
111
112
113
     // computation expression definition for the Option type (called
114
          Maybe in other languages)
115
     type MaybeBuilder() =
          member this. Bind (m : 'a \text{ option}, f : 'a \rightarrow 'b \text{ option}) : 'b
116
               option =
117
               Option.bind f m
          member this. Return (x : 'a) : 'a \text{ option} = \text{Some } x
118
119
     let maybe = new MaybeBuilder()
```

E.3.2 InterlockingModel.fs

```
1 namespace InterlockingModel
```

```
open Utils
3
4
5
   [<AutoOpen>]
   module TypeDefinitions =
6
7
       type TrainId = TrainId of string
       type TrainIds = TrainId list
8
9
10
       type LinearId = LinearId of string
11
       type PointId = PointId of string
12
13
       type PointPosition = Plus | Minus
14
15
       type RouteSegment = LinearRouteSegment of LinearId * length :
16
            int
                           PointRouteSegment of PointId *
17
                               required position : PointPosition
18
       type RouteSegments = RouteSegment list
19
       type RouteDirection = Up | Down
20
21
22
       type Route = Route of RouteSegments * RouteDirection
23
       type Routes = Route list
24
        type Train = { id : TrainId
25
                        route : Route
26
                       length : int }
27
       type Trains = Train list
28
29
       type Linear = { id : LinearId
30
                        train : Train option }
31
       type Linears = Linear list
32
33
34
       type Point = { id : PointId
35
                        position : PointPosition }
       type Points = Point list
36
37
        /// Elements for composing a railway network layout
38
        type LayoutSegment = LinearLayoutSegment of id : string
39
                            PointStemLayoutSegment of id : string
40
                            PointForkLayoutSegment of id : string *
41
                                position : PointPosition
42
       type RailwayNetworkLayout = Map<LayoutSegment, LayoutSegment>
43
44
        /// A collection of objects to be instantiated in the end model
45
        type ModelObjects = { trains : Map<TrainId , Train>
46
                               linears : Map<LinearId , Linear>
47
                               points : Map<PointId , Point> }
48
        type ValidatedModelObjects = Validated of ModelObjects
49
        type ModelGeneratorFunction = ValidatedModelObjects -> string
50
51
52
        (* Extending the types with field access functions *)
53
54
       type TrainId with
```

```
55
              static member value : TrainId \rightarrow string = fun (TrainId v)
                 -> v
56
         type LinearId with
57
             static member value : LinearId -> string = fun (LinearId
58
                  v) -> v
59
         type PointId with
60
61
             static member value : PointId \rightarrow string = fun (PointId v)
                 -> v
62
         type RouteSegment with
63
64
             static member length : RouteSegment -> int = function
                  LinearRouteSegment( , len) -> len
65
                  // All points has been simplified to have a length of
66
                      one
                  | PointRouteSegment -> 1
67
68
         type Route with
69
              static member segments : Route \rightarrow RouteSegments =
70
                  fun (Route (segments,_)) -> segments
71
              static member direction : Route -> RouteDirection =
72
                  fun (Route ( , dir)) -> dir
73
74
         type ModelObjects with
75
             member this.trainList : Trains =
76
                  this.trains |> Map.toList |> List.map snd
77
78
             member this.pointList : Points =
                  this.points |> Map.toList |> List.map snd
79
80
              {\bf member this.linearList : Linears = } 
                  this.linears |> Map.toList |> List.map snd
81
82
         (* Creating static access functions for record fields,
83
             with the functions having the same name as its field *)
84
85
         [<CompilationRepresentation(CompilationRepresentationFlags.ModuleSuffix)>]
86
87
         module Train =
             let id : Train \rightarrow TrainId = fun t \rightarrow t.id
88
             let route : Train \rightarrow Route = fun t \rightarrow t.route
89
             let length : Train \rightarrow int = fun t \rightarrow t.length
90
91
         [<CompilationRepresentation(CompilationRepresentationFlags.ModuleSuffix)>]
92
         module Linear =
93
             let id : Linear -> LinearId = fun tc -> tc.id
94
95
             let train : Linear -> Train option = fun tc -> tc.train
96
97
         [<CompilationRepresentation(CompilationRepresentationFlags.ModuleSuffix)>]
         module Point =
98
99
             let id : Point \rightarrow PointId = fun p \rightarrow p.id
             let position : Point \rightarrow PointPosition = fun p \rightarrow p.position
100
101
         [<CompilationRepresentation(CompilationRepresentationFlags.ModuleSuffix)>]
102
         module Layout Element =
103
             let id : LayoutSegment -> string = function
104
105
                  | LinearLayoutSegment id -> id
```

```
106
                   | PointStemLayoutSegment id -> id
107
                   | PointForkLayoutSegment (id, ) -> id
108
         /// Helper type used in the validation process.
109
110
         /// The type is used where routes or route segment lengths
              need validation
         /// and can represent a simple success or an error case with a
111
              description
112
         type SuccessResult = Result < unit, string >
          /// Infix operator for combining simple unit results
113
         let (&&&) (a : SuccessResult) (b : SuccessResult) :
114
              SuccessResult =
115
              match a with
              | Ok () \rightarrow b
116
              Error -> a
117
118
     /// Functions for constructing routes
119
     [<AutoOpen>]
120
     module RouteConstruction =
121
          /// Stitch two route fragments together to one route
122
         let stitchRoutePair (route1 : Route) (route2 : Route) :
123
              \operatorname{Result} < \operatorname{Route}, \operatorname{string} > =
              let stitch : RouteSegments -> RouteSegments ->
124
                   RouteDirection \rightarrow Route =
                   fun route1 elements route2 elements direction ->
125
                   let stitched = List.concat [route1_elements; List.tail
126
                       route2 elements]
127
                   Route (stitched, direction)
128
              let must have same direction : Route -> Route -> string =
129
                   sprintf """
130
                   routel and route2 must have same direction
131
                   route1: %A
132
                   route2 : %A
133
                   0.0.0
134
              let (|Diff_directions|_|) (r1 : Route, r2 : Route) =
let (Route(_, dir1)) = r1
135
136
                   let (Route(\_, dir2)) = r2
137
                   if dir1 \Leftrightarrow dir2
138
                   then Some(must_have_same_direction r1 r2)
139
140
                   else None
141
              let r1 must end where r2 starts : Route -> Route -> string
142
                   sprintf "route1 must end where route2 starts\nroute1:
143
                       A \setminus nroute2 : A''
              let (|NoCommonStichPoint|_|) (r1 : Route, r2 : Route) =
144
                   let (Route(r1 elements, -)) = r1
145
                   let (Route (r2 elements,
146
                                               )) = r^2
                  match r1_elements, r2_elements with
147
                   | r1 elements, (r2 first::)
148
                    when r1_elements <> []
&& List.last r1_elements = r2_first -> None
149
150
151
                   \rightarrow Some (r1 must end where r2 starts r1 r2)
152
```

```
153
            match route1, route2 with
             | Diff directions (error msg) -> Error error msg
154
155
              NoCommonStichPoint(error_msg) -> Error error_msg
             Route (route1 elements, dir), Route (route2 elements, ) ->
156
                   Ok (stitch route1_elements route2_elements dir)
157
158
159
         let stitchRoutes (routes : Routes) : Result<Route, string> =
160
             routes
161
             > Seq.map Ok
162
             > Result<_,_>.reduce stitchRoutePair
163
    /// Functions for checking if routes are valid together in a layout
164
165
    module RouteValidation =
         /// Checks that a route is has a linear as start and end
166
167
         let private routeHasLinearStartAndEnd (route : Route) :
             SuccessResult =
             let route segments = Route.segments route
168
            match Seq.head route_segments, Seq.last route_segments with
169
             | LinearRouteSegment _, LinearRouteSegment _ -> Ok ()
170
             -> route segments
171
                    > sprintf "route is must have a linear as start
172
                        and end\n%A"
                    > Error
173
174
         /// Checks that a given route is legal in a given layout
175
         let private routeIsValidInLayout (layout :
176
             RailwayNetworkLayout) (route : Route)
177
                                           : SuccessResult =
             // helper function for looking up an element in the layout
178
179
             let tryFind = fun from element ->
                 Map.tryFind from element layout
1.80
181
             // helper function that evaluates if two segments are
182
                 connected
             let areConnected : LayoutSegment -> LayoutSegment -> bool =
183
                 fun from element to element ->
184
                 match tryFind from_element with
185
                 Some(to element') when to element' = to element \rightarrow
186
                     true
                 ______ false
187
188
             let linearToLinear : string -> string -> bool = fun
189
                 from id to id \rightarrow
                 let from linear, to linear = LinearLayoutSegment
190
                     from id, LinearLayoutSegment to id
                 areConnected from linear to linear
191
192
             let linearToPoint : string -> string -> PointPosition ->
193
                 bool =
                 fun from_id to_id pos ->
194
                 let from linear = LinearLayoutSegment from id
195
                 let to stem = PointStemLayoutSegment to id
196
                 let to fork = PointForkLayoutSegment (to_id, pos)
197
                 areConnected from linear to stem || areConnected
198
                     from linear to fork
```

199		
200	let	pointToLinear : string \rightarrow PointPosition \rightarrow string \rightarrow
		bool =
201		fun from_id pos to_id ->
202		let from_stem = PointStemLayoutSegment from_id
203		<pre>let from_fork = PointForkLayoutSegment(from_id, pos)</pre>
204		let to_linear = LinearLayoutSegment to_id
205		// Since the Route-elements doesn't specify stem or fork
206		<pre>// -we have to try both to see if they exists in the layout</pre>
207		areConnected from_stem to_linear areConnected from fork to linear
208		
209	let	pointToPoint : string -> PointPosition -> string -> PointPosition -> bool =
210		<pre>fun from_id from_pos to_id to_pos -></pre>
211		<pre>let from_stem = PointStemLayoutSegment from_id</pre>
212		<pre>let from_fork = PointForkLayoutSegment(from_id,</pre>
213		let to stem = PointStemLayoutSegment to id
214		let to fork = PointForkLayoutSegment(to id, to pos)
215		areConnected from stem to stem
216		areConnected from stem to fork
217		areConnected from fork to stem
218		areConnected from fork to fork
219		
220	111	checks that a connection between two given elements
	111	exist in the current layout
221	///	basically we look up in the layout map to see if there exist a mapping from
999	111	a route element to the other given route element
222	let	connectionExistInLayout · (RouteSegment *
220	100	RouteSegment) -> bool =
224		LinearDouteSegment(LinearId from id)
220		LinearRouteSegment (LinearId from_id, _)
220		linearTeLinear from id to id
221		Linear PouteSegment (Linear Id from id)
220		Deint RouteSegment (Deint Id to id peg)
229		lineerTeDeint from id to id nee
230		Deint Deute Comment (Deint Le from id nea)
231		LincorDouteSegment (LincorLd to id)
232		neint Telineen from id not to id
233		point i obinear i rom id pos to id
234		PointRouteSegment (PointId from_id, from_pos),
230		romittoutesegment (romita to_la, to_pos) ->
230		point for orner from in from pos to in to pos
237	1.04	uarifu Cogmont Dain . Dout of cogmont [] . Success Docult
298	let	fun segment pair ->
239		<pre>let segment1, segment2 = segment_pair.[0], segment pair.[1]</pre>
240		match connectionExistInLayout(segment1, segment2) with
241		$ $ true \rightarrow Ok ()
242		false ->

243		sprintf "no connection between tracks [%A -> %A]" segment1 segment2
244		> Error
245		
246		match Route.direction route with
247		Up -> Route.segments route
248		Down -> List.rev (Route.segments route)
249		> Seq.windowed 2
250		> Seq.map verifySegmentPair
251		> Seq.reduce (&&&)
252		
253	///	verifying that two given routes can be used together in a model without obvious deadlock
254	let	<pre>private noObviousConflict (Route (route1_segments, _)) (Route (route2_segments, _))</pre>
255		: SuccessResult =
256		<pre>let diffStart : RouteSegments -> RouteSegments -> SuccessResult =</pre>
257		fun r1 segments r2 segments $->$
258		<pre>let diff_start = Seq.head r1_segments <> Seq.head r2 segments</pre>
259		if diff start then Ok ()
260		else Error "The given routes start at the same place"
261		
262		let diffEnd : RouteSegments -> RouteSegments ->
		SuccessResult =
263		fun r1 segments r2 segments \rightarrow
264		<pre>let diff_end = Seq.last r1_segments <> Seq.last r2_segments</pre>
265		if diff end then Ok ()
266		else Error "The given routes have the same destination"
267		0
268		let validStartAndEnd : RouteSegments -> RouteSegments ->
260		SuccessResult = f_{uv} r1 segments $->$
209		let route1 start - Seg head r1 segments
270		let route? start - Seq head r? segments
271		let routel end $-$ Seq last r1 segments
272		let route? end $=$ Seq. last r? segments
275		let diff start end -
274		not (route1_start = route2_end && route2_start = route1_end)
976		if diff start and then Ok ()
270		also Error "The given routed start and and in event
277		opposite locations"
278		
279		diffStart route1_segments route2_segments
280		xxxx diffEnd route1_segments route2_segments
281		www.validStartAndEnd route1_segments route2_segments
282		
283	let	verify Koutes (layout: Railway Network Layout) (routes :
		Koutes) : SuccessKesult =
284		let individual_routes_valid : SuccessResult seq =
285		routes
286		> seq.map (run route ->

```
287
                              routeHasLinearStartAndEnd route
                              &&& routeIsValidInLayout layout route)
288
289
             let routes are valid together : SuccessResult seq =
290
                 uniqueProducts routes
291
                 |> Seq.map (fun (r1, r2) \rightarrow noObviousConflict r1 r2)
292
293
294
             [ individual routes valid
295
             ; routes are valid together ]
             > Seq.concat
296
297
             |> Seq.reduce (&&&)
298
299
    /// Validation functions for verifying that the route segments
    /// obey the constraints defined by the lengths of the trains
300
    module LengthConstraints =
301
         type Intersection =
302
             { train1 : Train
303
               train2 : Train
304
               train1 track length : int
305
               train2 track length : int
306
               track id : LinearId }
307
308
         /// Checks that a route segment is shorter or equal to the
30.9
             train that holds the route
         let private routeSegmentIsShorterOrEqual (train : Train) :
310
             RouteSegment \rightarrow SuccessResult =
             function
311
             LinearRouteSegment (segment id, length)
312
                 when length > train.length ->
313
314
                      let err msg =
                          sprintf "%A in the route of train %A must be
315
                              equal to or smaller than %i"
                      err msg segment id train.id train.length
316
                      > Error
317
             | _ -> Ok ()
318
319
         /// Verify that lengths of intersecting track segments
320
         /// are obeying the following rule:
321
322
         /// if t2.length <= t1.track length
323
         /// then t2.track length == t2.length
324
             else t2.track length == t1.track length
325
326
         /// where tl.length >= t2.length
327
328
         let private shortestConstrainedByLongest (intersection :
             Intersection) : SuccessResult =
             // dividing the trains of the intersection into longest
329
                 and shortest trains
330
             // together with the length of the intersecting track
                 representation in their route.
             // train1 is the longest train and train2 is the shortest
331
                 train
             let [ t1, t1 track length
332
                  ; t2, t2 track length ] =
333
```

```
334
                    [ intersection.train1,
                        intersection.train1 track length
335
                    ; intersection.train2,
                        intersection.train2_track_length |
                   > List.sortByDescending (fst >> Train.length)
336
337
338
             let track id = intersection.track id
339
340
             // When the shortest train is shorter than the length of
             // the track representation in the longest train,
341
             // then the shortest trains track representation must be
342
             // exactly the length of the shortest train.
343
344
             // Eg. if the shortest train length is 2 and the longest
345
                 train length is 4
             // and the longest train track representation is 3,
346
             // then the shortest train track representation must be
347
                 equal to 2
             if t2.length <= t1 track length then
348
                 if t_2 track length = t_2.length then Ok ()
349
350
                 else
                      let err msg = sprintf """
351
                          the intersecting track %A, between train %A
352
                              and train %A
                          must have a length of %i in the route of train
353
                              %A
                          .....
354
355
                      Error(err msg track id t1.id t2.id t2.length t2.id)
             else// shortest train.length > longest train track length
356
357
                 // for example the length of shortest train is
                                                                    2
                 // and the length of the longest train track
358
                      representation is 1,
                 // then the length of the shortest trains track
359
                      representation
                  // must also be 1
360
                 if t2 track length = t1_track_length then Ok ()
361
362
                 else
                      let \operatorname{err}_m \operatorname{sg} = \operatorname{sprintf} """
363
                          intersecting track %A between train %A and
364
                               train %A
                          must have a length of %i in the route of train
365
                              %A
                          ......
366
                      Error(err msg track id t1.id t2.id t1.length t2.id)
367
368
         // Collect all intersections between two train routes
369
370
         let private getIntersections (t1 : Train, t2 : Train) :
             Intersection seq =
371
             let getLinearSegment : RouteSegment -> (LinearId * int)
                 option =
                 function
372
                   LinearRouteSegment(id, length) -> Some(id, length)
373
                   -> None
374
375
             let getLinearSegments : Route -> (LinearId * int) seq =
376
```

```
377
                  fun (Route(segments, )) ->
                  segments |> Seq.choose getLinearSegment
378
379
             let t1 linear lengths : Map<LinearId, int> =
380
381
                  getLinearSegments t1 route |> Map.ofSeq
382
383
             getLinearSegments t2.route
384
             > Seq.choose (
385
                  fun (track id, t2 track len) ->
                 Map.tryFind track id t1 linear lengths
386
387
                  > Option.map (fun t1 track len ->
                                 \{ train \overline{1} = t1 \}
388
389
                                   t\,r\,a\,i\,n\,2\ =\ t\,2
                                   train1 track length = t1 track len
390
                                   train2 track length = t2 track len
391
                                   track id = track id \}))
392
393
         let checkLengthContraints (trains : Trains) : SuccessResult =
394
             let all individual routes are valid : SuccessResult seq =
395
                  trains
396
                  |> Seq.collect (fun train ->
397
                                   let (Route(route segments, )) =
398
                                       train.route
399
                                   route segments
400
                                   > Seq.map
                                       (routeSegmentIsShorterOrEqual
                                       train))
401
             let all route intersections are valid : SuccessResult seq =
                  uniqueProducts trains
402
403
                  > Seq.collect getIntersections
                  > Seq.map shortestConstrainedByLongest
404
405
             [ all individual routes are valid
406
             ; all route intersections are valid ]
407
             > Seq.concat
408
             |> Seq.reduce (&&&)
409
410
    [<AutoOpen>]
411
    module ModelGeneration =
412
         /// Interface describing the properties to be generated for
413
             the model
         type ModelCheckingPropertyDefinitions =
414
             abstract NoCollision : string
415
             abstract AllTrainsArrived : string
416
             abstract NoDerailment : string
417
             abstract\ TrainsDetectedOnPoints\ :\ string
418
             abstract AllMessagesHandled : string
419
             abstract NoMalfunctionsWhenTrainHasNotArrived : string
420
421
         /// Validates that all trains have a route and that all the
422
             routes are valid in the layout
         let private validateTrainRoutes (layout :
423
             RailwayNetworkLayout) (objects : ModelObjects)
424
                                                Result < Validated ModelObjects,
```

```
\operatorname{string} > =
             /\,/\,/ gets a route if the train have one
425
426
             let getRoute : Train -> Result < Route, string > = fun train
                 ->
                 match train.route with
427
                 // there exist a route with at least one element
428
429
                  | Route(head::tail, direction) as route -> Ok (route)
                 _ -> Error (sprintf "no route for train %A" train.id)
430
431
             let routes valid : SuccessResult =
432
                 objects.trainList
433
434
                 > Result< , >.traverse getRoute
435
                 >>= (RouteValidation.verifyRoutes layout)
436
437
             match routes valid with
             | Ok () -> Ok(Validated objects)
438
             | Error msg -> Error msg
439
440
         let checkLengthContraints (valid objects :
441
             Validated ModelObjects)
                                     : Result < Validated ModelO bjects,
442
                                         \operatorname{string} > =
             let (Validated objects) = valid objects
443
             let length constraints ok =
444
445
                 objects.trainList
446
                 > LengthConstraints.checkLengthContraints
             match length constraints ok with
447
             Ok ()
                        -> Ok(Validated objects)
448
             Error msg -> Error msg
449
450
         // Updates all the linears, which are first on a route, to
451
             reflect presence of a train
         let updateTrainLocations (Validated objects) :
452
             Result < Validated ModelObjects, string > =
             let updateTrainLocation (train : Train) (objects :
453
                 ModelObjects) = resultFlow {
                 let! linear id =
454
                     match train.route with
455
                      Route(LinearRouteSegment(linear id,)::,) ->
456
                          Ok linear_id
                       _ -> Error (sprintf """
457
                                     possibly malformed route for train %A
458
                                    perhaps validation is missing?
459
                                    """ train)
460
461
                 let! linear =
                     match Map.tryFind linear id objects.linears with
462
                       Some linear -> Ok linear
463
                      | None -> Error (sprintf "linear %A doesnt exist"
464
                          linear id)
                 let updated_linear = { linear with train = Some train }
465
                 let updated linears = objects linears |> Map.add
466
                     linear_id updated_linear
                 return { objects with linears = updated linears } }
467
468
             objects.trainList
             |> Result<_,_>.fold updateTrainLocation (Ok objects)
469
```

```
| > Result < , > map Validated
470
471
472
         let generateRawModel : ModelGeneratorFunction = fun (Validated
             objects) ->
             sprintf "%A" objects
473
474
475
         /// Validates the routes,
         /// updates the train locations in the network based on their
476
             first route segment,
         /// and generates the final model instantiation using the
477
             generateModel function
         let validateAndGenerateModel (modelGenFun :
478
             ModelGeneratorFunction)
             : RailwayNetworkLayout -> ModelObjects -> Result<string ,
479
                  \operatorname{string} > =
             fun layout objects ->
480
             validateTrainRoutes layout objects
481
482
             >>= checkLengthContraints
             >>= updateTrainLocations
483
             >>= (modelGenFun >> Ok)
484
```

E.3.3 UMCTrainClass.fs

```
module UMCTrain
1
2
   let class definition = """
3
4
   Class Train is
5
6
      Signals:
7
       ok, no;
8
9
      Vars:
10
        requested point positions : bool[];
11
        train length : int = 2; --- how many track segments does the
            train occupy
        route segments : obj[];
12
        route index : int := 0; --- current location on the route
13
14
        occupies : obj[]; — the tc and pt objects which the train
            currently occupies
        front advancement count : int; --- a variable for keeping track
15
            of the trains front advancement over a track
        track lengths : int []; --- same number of elements as
16
            route segments
17
      State Top = READY, WAIT OK, MOVEMENT, ARRIVED
18
19
      Transitions:
20
21
          - send out initial reservation request to the first node on
            route
22
        READY -> WAIT OK {
23
                     _ /
^{24}
                     route segments [0].req(self, 0, route segments,
                         requested point positions);
25
            }
```

26	
27	— when the train reservation is rejected we just keep cycling between WAIT OK and READY
28	WAIT OK \rightarrow READY { no }
29	
30	— train receives ackknowledgement that the route has been reserved succesfully
31	— the front_advancement_count variable is initialized to reflect the trains front location on the track
32	WAIT_OK -> MOVEMENT { ok / front_advancement_count := train length - 1; }
33	
34	MOVEMENT \rightarrow MOVEMENT {
35	
36	[not (route index = route segments.]ength -1 and
37	track lengths [route index] - 1 =
	front advancement count)] / at end of track
38	at end of track: bool := track lengths[route index] - 1 =
	front advancement count; — determine if we have
	reached the end of the current track
39	if at end of track = true then $\{$ the train has
	reached the end of its current track
40	front advancement count $:= 0$:
41	if route index < route segments, length -1 then
	{ the route index is not the last
42	train enters next track
43	route index := route index $+ 1$;
44	route segments [route index].sensorOn(self);
	the next track detects the train
45	};
46	} else {
47	front advancement count := front advancement count + 1;
48	_ };
49	
50	rear: obj := occupies.head;
51	next rear: obj := occupies.tail.head;
52	occupies := occupies.tail + [route segments[route index]];
53	if rear != next_rear then { determine if the rear of the train has left a track
54	rear.sensorOff(self); the past track detects that the train does not occupy it anymore
55	};
56	
57	
58	MOVEMENT -> ABRIVED {
59	
60	[route index = route segments, length -1 and $$ at
00	last track segment of route
61	track lengths [route index] - 1 =
	front advancement count] — at end of track
62	} = = '
63	
64	end Train
65	

E.3.4 UMCLinearClass.fs

```
module UMCLinear
1
2
   let class definition = """
3
   Class Linear is
4
5
      Signals:
6
            req(sender: obj, route index: int, route elements: obj[],
7
8
                     requested point positions: bool[]);
9
            ack(sender: obj);
10
            nack(sender: obj);
11
            commit(sender: obj);
            agree(sender: obj);
12
13
            disagree(sender: obj);
14
15
      Operations:
        sensorOn(sender: obj);
16
        sensorOff(sender: obj);
17
18
      Vars:
19
20
        next: obj;
        prev: obj;
21
22
        train: obj := null;
23
      State Top = NON RESERVED, WAIT ACK, WAIT COMMIT, WAIT AGREE,
^{24}
          RESERVED, TRAIN IN TRANSITION
25
      Transitions
26
27
            --- first node receive request
28
       NON RESERVED -> WAIT ACK {
29
                     req(sender, route_index, route_elements,
30
                         requested point positions)
                     [route index = 0 and sender = train and
31
                         route elements.length > 0 /
32
                     prev := null;
33
                     next := route elements [1];
34
                     next.req(self, 1, route elements,
                         requested point positions);
35
            }
36
            --- intermediate node receive request
37
38
       NON RESERVED -> WAIT ACK {
                     req (sender, route index, route elements,
39
                         requested point positions)
40
                     [train = null and (route index > 0 and
                         route index+1 < route elements.length)] /
41
                     prev := route elements [route index -1];
42
                     next := route elements [route index + 1];
43
                     next.req(self, route index + 1, route elements,
                         requested point positions);
44
            }
45
46
            -- initial reservation request for last node
```

```
47
             --- starts ack phase
        NON RESERVED -> WAIT COMMIT {
48
                      req(sender, route_index, route_elements,
49
                      requested point positions)
[train = null and route_elements.length =
50
                          route index + 1 /
51
                      prev := route elements [route index -1];
                      n ext := n u ll;
52
53
                      prev.ack(self);
             }
54
55
            --- intermediate node receive ack
56
57
        WAIT ACK -> WAIT COMMIT {
                      ack(sender)
58
                      [prev /= null] /
59
                      prev.ack(self);
60
             }
61
62
            --- first node receive ack
63
            --- and starts commit phase
64
        WAIT ACK -> WAIT AGREE {
65
                      ack (sender)
66
                      [prev = null] /
67
68
                      next.commit(self);
             }
69
70
71
             -- intermediate node receives commit
        WAIT COMMIT -> WAIT AGREE {
72
                      commit (sender)
73
74
                      [next /= null] /
                      next.commit(self);
75
             }
76
77
            --- last node receive commit
78
            --- and starts agree phase
79
        WAIT COMMIT -> RESERVED {
80
                      commit (sender)
81
                      [next = null] /
82
                      prev.agree(self);
83
             }
84
85
            -- intermediate node receive agree
86
        WAIT AGREE -> RESERVED {
87
88
                      agree (sender)
89
                      [prev /= null]
                      prev.agree(self);
90
             }
91
92
93
            --- first node receive agree
            --- and sends ok to the train
94
        WAIT AGREE -> TRAIN IN TRANSITION {
95
96
                      agree (sender)
                      [prev = null and train /= null] /
97
98
                      train.ok;
             }
-99
```

```
100
101
             -- train moves onto current node
         RESERVED -> TRAIN IN TRANSITION {
102
                      sensorOn(sender) /
103
104
                      train := sender;
             }
105
106
107
             --- sequential release
108
             --- reset train
         TRAIN IN TRANSITION -> NON RESERVED {
109
                      sensorOff(sender) /
110
                      train := null;
111
112
             }
113
             --- nack received
114
             -- forwards and goes into non-reserved
115
         WAIT ACK -> NON RESERVED {
116
117
                      nack(sender) /
                          prev = null then \{ --- is first node on
                      i f
118
                           itinerary
119
                               train.no
                      } else { --- is not first node
120
                               prev.nack(self)
121
122
                      };
             }
123
124
             --- disagree received
125
             -- forwards and goes into non-reserved
126
         WAIT COMMIT -> NON RESERVED {
127
128
                      disagree(sender) /
                      if next /= null then { -- not last node on
129
                           itinerary
                               next.disagree(self)
130
                      };
131
             }
132
133
             --- disagree received
134
             -- forwards and goes into non-reserved
135
         WAIT AGREE -> NON RESERVED {
136
137
                      disagree(sender) /
                      if prev /= null then { -- not first node on
138
                           itinerary
                               prev.disagree(self)
139
                      } else { --- is first node
140
                               train.no
141
                      };
142
143
             }
144
145
             --- disagree received
             -- forwards (if there is someone to forward to) and goes
146
                  into non-reserved
         RESERVED -> NON RESERVED {
147
                      disagree(sender) /
148
                      if next /= null then { -- not last node on
149
                           itinerary
```

```
150
                               next.disagree(self)
                      };
151
152
             }
153
154
             --- reservation request received
             -- however a train is already on the track, so a nack is
155
                  returned to sender
         NON RESERVED -> NON RESERVED {
156
157
                      req(sender, route index, route elements,
                           requested point positions)
158
                      [train /= null and sender /= train] /
                      sender.nack(self);
159
160
             }
161
162
             -- reservation request received
             -- however, the node is already in wait-ack, so it returns
163
                 a nack to sender
         WAIT ACK -> WAIT ACK {
164
                      req(sender, route index, route elements,
165
                           requested point positions) /
166
                      sender.nack(self);
             }
167
168
169
             -- reservation request received
             -- however, the node is already in wait-commit, so it
170
                  returns a nack to sender
         WAIT_COMMIT -> WAIT COMMIT {
171
172
                      req(sender, route index, route elements,
                          requested point positions) /
                      sender.nack(self);
173
174
             }
175
             -- reservation request received
176
             -- however, the node is already in wait-agree, so it
177
                  returns a nack to sender
         WAIT AGREE -> WAIT AGREE {
178
179
                      req(sender, route index, route elements,
                           requested point positions) /
180
                      sender.nack(self);
             }
181
182
183
             -- reservation request received
             -- however, the node is already reserved, so it returns a
184
                  nack to sender
         \operatorname{RESERVED} \ -> \ \operatorname{RESERVED} \ \{
185
                      req(sender, route index, route elements,
186
                           requested point positions) /
                      sender.nack(self);
187
188
             }
189
             --- reservation request received
190
             -- however, a train is in transition on the node, so it
191
                  returns a nack to sender
         \label{eq:train_transition} TRAIN_IN\_TRANSITION ~ \{
192
```

E.3.5 UMCPointClass.fs

```
module UMCPoint
1
2
   let class_definition = """
3
\mathbf{4}
   --- points are always intermediate nodes
   --- so we don't need to check if they are first or last in the
5
        guards
   Class Point is
\mathbf{6}
7
8
      Signals:
        req(sender: obj, route index: int, route elements: obj[],
9
            requested point positions: bool[]);
10
        ack(sender: obj);
11
        nack(sender: obj);
12
        commit(sender: obj);
13
        agree(sender: obj);
        disagree(sender: obj);
14
15
16
      Operations:
        sensorOn(sender: obj);
17
        sensorOff(sender: obj);
18
19
      Vars:
20
^{21}
        next: obj;
22
        prev: obj;
        requested position: bool;
23
        current position: bool := True;
24
        train: obj := null;
25
26
      State Top = NON RESERVED, WAIT ACK, WAIT COMMIT, WAIT AGREE,
27
                                POSITIONING, RESERVED,
28
                                    TRAIN IN TRANSITION, MALFUNCTION
29
30
     Transitions:
31
            --- initial reservation request
32
        NON RESERVED -> WAIT ACK {
33
                     req (sender, route index, route elements,
34
                          requested point positions) /
                     prev := route elements [route index - 1];
35
36
                     next := route elements [route index + 1];
                     requested position :=
37
                          requested _ point _ positions [ route _ index ] ;
38
                     next.req(self, route index + 1, route elements,
                          requested point positions);
```

```
39
             }
40
41
            --- receiving and forwarding ack
        WAIT ACK -> WAIT COMMIT {
42
43
                     ack(sender) /
                      prev.ack(self);
44
45
             }
46
47
            -- receiving and forwarding commit
        WAIT COMMIT -> WAIT AGREE {
48
                     commit(sender) /
49
                      next.commit(self);
50
51
             }
52
            -- if the point is positioned as required for the given
53
                 route reservation
            -- receiving and forwarding agree
54
        WAIT AGREE -> RESERVED {
55
                      agree (sender)
56
                      [current_position = requested_position]/
57
                      prev.agree(self);
58
             }
59
60
            -- if the point is not positioned as required for the
61
                 given route
            --- goes into positioning state
62
        WAIT AGREE -> POSITIONING {
63
64
                      agree (sender)
                      [current position /= requested position] /
65
66
             }
67
68
            -- successfully performing positioning
69
        POSITIONING -> RESERVED {
70
71
                     - /
                      current position := not current position;
72
73
                      prev.agree(self);
74
            }
75
            -- simulating sudden malfunction of positioning system
76
            --- and sending disagrees to neighbor nodes
77
        {\rm POSITIONING} \ {\rm {->}} \ {\rm MALFUNCTION} \ \ {\rm {}}
78
                     - /
79
80
                      prev.disagree(self);
81
                      next.disagree(self);
             }
82
83
            -- train moves onto current node
84
        RESERVED -> TRAIN IN TRANSITION {
85
                      sensorOn(sender) /
86
                      train := sender;
87
             }
88
89
            --- sequential release
90
            -- reset all train
91
```

```
92
         TRAIN IN TRANSITION -> NON RESERVED {
                      sensorOff(sender) /
93
94
                      -- [sender = train] /
95
                      train := null;
96
             }
97
98
             -- nack received and forwarded
         WAIT ACK -> NON RESERVED {
99
100
                      nack(sender) /
101
                      prev.nack(self);
102
             }
103
104
             -- disagree received and forwarded
         WAIT COMMIT -> NON RESERVED {
105
                      disagree(sender) /
106
                      next.disagree(self);
107
             }
108
109
             --- disagree received and forwarded
110
         WAIT AGREE -> NON RESERVED {
111
                      disagree(sender) /
112
                      prev.disagree(self);
113
             }
114
115
             -- disagree received and forwarded
116
         POSITIONING -> NON RESERVED {
117
118
                      disagree(sender) /
119
                      next.disagree(self);
             }
120
121
             -- disagree received and forwarded
122
         RESERVED -> NON RESERVED {
123
                      disagree(sender) /
124
                      next.disagree(self);
125
             }
126
127
             --- reservation request received
128
             -- however, the node is already in wait-ack, so it returns
129
                 a nack to sender
        WAIT ACK -> WAIT ACK {
130
                      req(sender, route_index, route_elements,
131
                          requested point positions) /
                      sender.nack(self);
132
             }
133
134
             --- reservation request received
135
             -- however, the node is malfunctioning
136
        MALFUNCTION -> MALFUNCTION {
137
                      req(sender, route index, route elements,
138
                          requested point positions) /
139
                      sender.nack(self);
             }
140
141
142
             --- reservation request received
```

```
143
             -- however, the node is already in wait-commit state and
                 returns nack to the sender
        WAIT COMMIT -> WAIT COMMIT {
144
145
                     req(sender, route index, route elements,
                          requested position) /
146
                     sender.nack(self);
147
             }
148
149
             --- reservation request received
150
             -- however, the node is already in wait-agree state and
                 returns nack to the sender
151
        WAIT AGREE -> WAIT AGREE {
152
                     req(sender, route_index, route_elements,
                          requested position) /
153
                     sender.nack(self);
             }
154
155
156
             -- reservation request received
             -- however, the node is already in positioning state and
157
                 returns nack to the sender
        POSITIONING -> POSITIONING {
158
                     req(sender, route index, route elements,
159
                          requested position) /
160
                     sender.nack(self);
             }
161
162
163
             -- reservation request received
164
             -- however, the node is already reserved and returns nack
                 to the sender
165
        RESERVED -> RESERVED {
                     req(sender, route index, route elements,
166
                          requested position) /
167
                     sender.nack(self);
             }
168
169
             --- reservation request received
170
             -- however, the node is occupied by a train and returns
171
                 nack to the sender
        TRAIN IN TRANSITION -> TRAIN IN TRANSITION {
172
                     req(sender, route_index, route_elements,
173
                          requested position) /
174
                     sender.nack(self);
175
             }
176
177
    end Point
    178
```

E.3.6 UMC.fs

```
    namespace UMC
    open InterlockingModel
    open UMCTrain
    open UMCPoint
```

```
open UMCLinear
6
   open System
7
8
   open Utils
q
10
   [<AutoOpen>]
   module UMCDefinitions =
11
12
        /// the UMC classes defining the behavior of the model
        let train class = UMCTrain.class_definition
13
        let point class = UMCPoint class definition
14
        let linear class = UMCLinear.class_definition
15
16
        /// Model specific string representations
17
18
        /// used as object identifiers in the UMC model
        type TrainId with
19
            static member modelRepresentation train id =
20
                 TrainId.value train id |> sprintf "train %s"
21
        type LinearId with
22
23
            static member modelRepresentation linear id =
                 LinearId.value linear id |> sprintf "linear %s"
24
        type PointId with
25
            static member modelRepresentation point id =
26
                 PointId.value point id |> sprintf "point %s"
27
        type PointPosition with
28
            static member modelRepresentation : PointPosition ->
29
                string = function
                 | Plus -> "True"
30
                 | Minus -> "False"
31
        type RouteSegment with
32
            static member modelRepresentation : RouteSegment -> string
33
                = function
                 | LinearRouteSegment(lin id, ) ->
34
                     LinearId.modelRepresentation lin id
                 | PointRouteSegment (point id, ) ->
35
                     PointId.modelRepresentation point_id
36
    /// Functions for generation of UMC abstractions
37
   [<AutoOpen>]
38
   module AbstractionDefinitions =
39
        type AbstractionType = Action | State
40
        type Abstraction <'a> =
41
            \{ name : 'a \rightarrow string \}
42
              abstraction\_type : AbstractionType
43
              predicate : 'a \rightarrow string }
44
45
46
        let getAbstractionName : 'a \rightarrow Abstraction<'a> \rightarrow string = fun
            args abstraction ->
47
            abstraction.name args
48
49
        let abstraction Definition (abstraction : Abstraction <'a>)
            (args : 'a) : string =
            let predicate = abstraction.predicate args
50
            let name = abstraction.name args
51
            match abstraction.abstraction type with
52
            | Action -> sprintf "Action: \overline{\%}s -> \%s" predicate name
53
            State -> sprintf "State: %s -> %s" predicate name
54
```
```
55
         let with Point ModelRep : Point -> (string -> string) -> string =
56
57
             fun {id=id} stringGenerator ->
             PointId.modelRepresentation id
58
59
             > stringGenerator
60
61
         let withTrainModelRep : Train -> (string -> string) -> string =
62
             fun {id=id} stringGenerator ->
63
             TrainId. modelRepresentation id
             > stringGenerator
64
65
         let pointIn : PointPosition -> Abstraction <Point> = fun
66
             position ->
             let name = fun point \rightarrow
67
                 match position with
68
                  | Plus -> withPointModelRep point (sprintf
69
                      "%s in plus")
70
                   Minus -> withPointModelRep point (sprintf
                      "%s in minus")
             let predicate = fun point ->
71
                 match position with
72
                  | Plus -> withPointModelRep point (sprintf
73
                      "%s.current position = True")
                   Minus \rightarrow with \overline{P} oint Model Rep point (sprintf
74
                      "%s.current position = False")
75
             { name = name
             ; abstraction type = State
76
77
             ; predicate = predicate }
78
79
         let pointInPlus : Abstraction <Point> = pointIn Plus
         let pointInMinus : Abstraction < Point > = pointIn Minus
80
81
         \label{eq:let_noTrainDetectedOnPoint} \ : \ Abstraction {<} Point > =
82
             let name = fun point \rightarrow
83
                 withPointModelRep point (sprintf "no train on %s")
84
             let predicate = fun point ->
85
                 withPointModelRep point (sprintf "%s.train = null")
86
             { name = name
87
             ; abstraction type = State
88
             ; predicate = predicate }
89
90
         let all_pairs_of_trains_at_diff_positions :
91
             Abstraction < Trains >
             let name = fun _-> "trains_at_diff_positions"
let predicate = fun trains ->
92
93
                  let trainPairAtDiffPositions : (Train * Train) ->
94
                      string =
                      fun (train1, train2) \rightarrow
95
96
                      let train1 id = TrainId.modelRepresentation
                           train1.id
                      let train2_id = TrainId.modelRepresentation
97
                           train2.id
98
                      let trainPartsAtDiffPositions : (int * int) ->
99
                           string = fun (id1, id2) \rightarrow
```

```
100
                           sprintf "%s.occupies[%d] /= %s.occupies[%d]"
101
                                   train1 id
102
                                   id1
103
                                   train2 id
104
                                   id2
105
106
                      crossProductOfLists [0..train1.length-1]
                           [0..train2.length-1]
107
                      > Seq.map trainPartsAtDiffPositions
                      | > String concat " and n"
108
109
                  uniqueProducts trains
110
                  > Seq.map trainPairAtDiffPositions
111
                  | > String concat " and \backslash n"
112
             { name = name
113
             ; abstraction type = State
114
             ; predicate = predicate }
115
116
         let positioning : Abstraction < Point > =
117
             let name = fun point ->
118
                  (sprintf "positioning_%s")
119
                  > withPointModelRep point
120
             let predicate = fun point ->
121
                  (sprintf "inState(%s.POSITIONING)")
122
123
                  > withPointModelRep point
             { name = name
124
125
             ; abstraction_type = State
126
               predicate = predicate }
             ;
127
128
         let trainArrived : Abstraction < Train > =
             let name = fun train ->
129
                  withTrainModelRep train (sprintf "%s arrived")
130
             let predicate = fun train ->
131
                  withTrainModelRep train (sprintf "inState(%s.ARRIVED)")
132
             { name = name
133
             ; abstraction_type = State
134
             ; predicate = predicate }
135
136
         let trainNotOnPoint : Abstraction <Train * Point> =
137
             let name : Train * Point -> string = fun (train, point) ->
138
                  let train model rep = TrainId modelRepresentation
139
                      train.id
                  let point model rep = PointId.modelRepresentation
140
                      point.id
                  sprintf "%s_not_on_%s" train_model_rep point_model_rep
141
             let predicate : Train \overline{*} Point \rightarrow string = fun (train,
142
                  point) ->
                  let point model rep = PointId.modelRepresentation
143
                      point.id
                  let train model rep = TrainId.modelRepresentation
144
                      train.id
                  let trainPartNotOnPoint : int -> string = fun index ->
145
                      sprintf "%s.occupies[%d] /= %s"
146
                               train model rep
147
                               index
148
```

149		point_model_rep
150		$\begin{bmatrix} 0 & \dots & \text{train} & \text{length} & - & 1 \end{bmatrix}$
151		> Seq.map trainPartNotOnPoint
152		$ >$ String.concat " and \n"
153		{ name = name
154		; abstraction_type = State
155		; predicate = predicate }
156		
157	\mathbf{let}	discarded msg : Abstraction $<$ unit $> =$
158		{ name = fun> "discarded_message"
159		; abstraction_type = Action
160		; predicate = fun> "lostevent" }
161		
162	let	pointMalfunction : Abstraction < Point > =
163		<pre>let pointModelRep = fun p -> PointId.modelRepresentation p.id</pre>
164		{ name = fun p -> sprintf "%s_malfunction" (pointModelRep p)
165		: $abstraction type = State$
166		; predicate = fun p -> sprintf "inState(%s.MALFUNCTION)"
		(point ModelRep p) }
167		
168	let	all_abstraction_declarations (validated_objects : ValidatedModelObjects) : string =
169		let (Validated objects) = validated objects
170		let trains : Trains = objects.train \overline{L} ist
171		let points : Points = objects.pointList
172		1 5 1
173		let no trains detected on points =
174		points > List.map (abstractionDefinition
		noTrainDetectedOnPoint)
175		let points positioning =
176		points > List.map (abstractionDefinition positioning)
177		let points in plus =
178		points > List.map (abstractionDefinition pointInPlus)
179		let points in minus =
180		points > List.map (abstractionDefinition pointInMinus)
181		let trains_arrived =
182		trains > List.map (abstractionDefinition trainArrived)
183		<pre>let trains_at_diff_positions =</pre>
184		(all_pairs_of_trains_at_diff_positions, trains)
185		> abstractionDefinition
186		<pre>let trains_not_on_points =</pre>
187		crossProductOfLists trains points
188		> List.ofSeq
189		> List.map (abstractionDefinition trainNotOnPoint)
190		let discarded_message =
191		abstractionDefinition discarded_msg ()
192		<pre>let points_malfunction =</pre>
193		points > List.map (abstractionDefinition pointMalfunction)
194		
195		[trains_arrived
196		; no_trains_detected_on_points
197		; points_positioning

```
198
             ; points in plus
             ; points in minus
199
             ; points malfunction
200
             ; [ trains at diff positions ]
201
202
             ; trains_not_on_points
             ; [ discarded message ] ]
203
204
             > List.concat
             > String.concat "\n"
205
206
    //// Extension functions for generating object instantiations in
207
        UMC
    [<AutoOpen>]
208
209
    module ModelObjectInstantiations =
        type Linear with
210
             static member modelObjectInstantiation : Linear -> string
211
                 = fun linear ->
                 let train id =
212
                     match linear train with
213
                      Some train -> TrainId.modelRepresentation
214
                          train.id
                                   -> "null"
215
                      None
                 let linear id = LinearId.modelRepresentation linear.id
216
                 sprintf "%s: Linear(train => %s);" linear id train id
217
218
        type Point with
219
             static member modelObjectInstantiation : Point -> string =
220
                 fun point ->
221
                 let model point id = PointId.modelRepresentation
                     point.id
                 sprintf "%s: Point;" model point id
222
223
224
        type Train with
             static member modelObjectInstantiation : Train *
225
                 ModelObjects \rightarrow string =
                 fun (train, objects) ->
226
                 let train id : string = TrainId modelRepresentation
227
                     train.id
228
                 let pointPosition : RouteSegment -> string = function
229
                      | PointRouteSegment (_, pos) ->
230
                          PointPosition.modelRepresentation pos
                      231
232
233
                 let route segments : RouteSegments = Route.segments
                     train.route
234
                 let route element ids : string =
235
                     route segments
236
237
                     > Seq.map RouteSegment.modelRepresentation
                     > String.concat ","
238
239
                 let track lengths : string =
240
                     route segments
241
242
                     |> Seq.map (RouteSegment.length >> string)
                     > String.concat ","
243
```

244	
245	lot requested point positions , string -
240	ret requested point positions : string -
240	route_segments
247	> Seq map pointPosition
248	> String.concat ","
249	
250	let occupies : string option =
251	Seq.tryHead route segments
252	> function
253	Some(LinearRouteSegment(linear_id,_)) -> Some linear_id
254	> None
255	> Option.map (LinearId.modelRepresentation
256	>> Seq.replicate train.length
257	>> String.concat ",")
258	
259	match occupies with
260	Some occupies \rightarrow
261	sprintf "%s: Train (" train id
262	sprintf "route segments \Rightarrow [%s]."
202	route element ids
263	\sim sprintf "track langths \rightarrow [%s] " track langths
200	, sprint "train length \rightarrow [705], since length
204	, sprinte train_iegen > /0, train.iegen
200	; sprint occupies $\rightarrow [705]$, occupies
200	; sprint requested point positions -> [/05]);
0.05	le duested point positions]
267	> String concat \(n'')
268	None -> sprinti
269	%s: 1 rain (
270	route segments \Rightarrow [],
271	$track_lengths \Rightarrow []$
272	$train_length => \%i$,
273	occupies => [],
274	requested point positions \Rightarrow []);
275	
276	train_id train.length
277	
278	let $modelObjectInstantiation$ (Validated objects) : string =
279	let trains : string seq =
280	Map.toSeq objects.trains
281	> Seq.map (fun (, train) $->$
	Train modelObjectInstantiation (train, objects))
282	let linears : string seq =
283	Map.toSeq_objects linears \geq Seq.map (snd \geq
	Linear, modelObjectInstantiation)
284	let points · string seg =
204	Man to Sea objects points IN Sea man (and N)
200	Reprint modelObjectingtantian)
200	[troing, lineared, points]
200 907	[viains, fillears; points]
287	> Seq.concat
288	> String.concat \n\n
289	
290	[< AutoOpen >]
291	module properties =
292	/// Class containing generated properties

```
293
         /// (implements the ModelCheckingPropertyDefinitions interface)
294
         type ModelCheckingProperties(validated objects :
             ValidatedModelObjects) =
             let (Validated objects) = validated objects
295
296
             let trains = objects.trainList
             let points = objects.pointList
297
298
299
             interface ModelCheckingPropertyDefinitions with
300
                 member this.NoMalfunctionsWhenTrainHasNotArrived :
                      string =
301
                      let p malfunctions : string =
302
                          points
303
                          > Seq.map (fun p -> getAbstractionName p
                              pointMalfunction)
                          |> String.concat " or "
304
                      let t arrivals : string =
305
                          trains
306
307
                          > Seq.map getAbstractionName
                          |> Seq.map ((|>) train Arrived)
308
                          > String concat " and "
309
                      sprintf "not E[not (%s) U (final and not (%s))];"
310
                              p malfunctions t arrivals
311
312
313
                 member this.NoCollision : string =
                      all pairs of trains at diff positions
314
                      > getAbstractionName trains
315
                      |> sprintf "AG (%s);"
316
317
                 member this.AllTrainsArrived : string =
318
319
                      trains
                      > Seq.map getAbstractionName
320
321
                      |> Seq.map ((|>) train Arrived)
                      > String concat " and "
322
                      > sprintf "EF AG (%s);"
323
324
                 member this NoDerailment : string =
325
                      let positioningImpliesNoTrain = fun
326
                          abstractionName \rightarrow
                          let point is positioning = abstractionName
327
                              positioning
                          let no train detected =
328
                              abstractionName noTrainDetectedOnPoint
329
                          [ point_is_positioning; " implies ";
330
                              no train detected
                          |> String.concat ""
331
332
                      points
333
                      |> Seq.map (getAbstractionName >>
                          positioningImpliesNoTrain)
                      > String.concat " and \n"
334
                      | > sprintf "AG (%s);"
335
336
                 member this.TrainsDetectedOnPoints : string =
337
                      let trainsAtPointImpliesTrainsDetected = fun
338
                          (train1, train2, point) \rightarrow
339
                          let train1 not on point =
```

340	trainNotOnPoint > getAbstractionName
	(train1, point)
341	<pre>let train2_not_on_point =</pre>
342	trainNotOnPoint > getAbstractionName
	$(t \operatorname{rain2}, \operatorname{point})$
343	let no_train_on_point =
344	noTrainDetectedOnPoint >
	getAbstractionName point
345	<pre>["(not ("; train1_not_on_point; " and ";</pre>
346	; "implies not "; no train on point; ")"]
347	> String.concat ""
348	points
349	> Seq.collect (fun point ->
350	uniqueProducts trains
351	> Seq.map (fun (t1,t2) $->$ t1,t2, point))
352	> Seq.map trainsAtPointImpliesTrainsDetected
353	$>$ String concat " and \n"
354	> sprintf "AG (%s);"
355	
356	member this.AllMessagesHandled : string =
357	getAbstractionName () discarded msg
358	> sprintf "AG not (EX {%s} true);"
359	
360	/// Collects all the model properties into one string
361	let collectModelProperties (properties :
	ModelCheckingPropertyDefinitions) =
362	let trains at diff positions =
363	properties. NoCollision
364	> sprintf """
365	safety property:
366	— no incident
367	no trains occupy the same location node at the
	same time
368	%s
369	и и и
370	<pre>let no_derailment =</pre>
371	properties . NoDerailment
372	> sprintf """
373	— safety property:
374	— no trains are located at any 'point' while it is changing its position
375	%s
376	H H H
377	<pre>let all_trains_arrived =</pre>
378	properties . AllTrainsArrived
379	> sprintf """
380	progress property that specifies that
381	all trains has arrived at their destinations
382	%s
383	н н н
384	<pre>let no_malfunction_when_train_has_not_arrived =</pre>
385	properties . NoMalfunctionsWhenTrainHasNotArrived
386	> sprintf """

```
387
                      -- property that specifies that
                      -- there does not exist a final state where at
388
                           least one train has not arrived
                       --- and in all states leading to this final state,
389
                          no points have malfunctioned
                      \%s
390
                      .....
391
392
              let trains_detected_on_points =
393
                  properties. TrainsDetectedOnPoints
                  | > sprintf """
394
395
                      -- property to verify that all trains are
                           correctly detected at points
396
                      \%s
                      .....
397
              let all_messages_handled =
398
                  properties. AllMessagesHandled
399
                  |> sprintf """
400
401
                      -- no signal is ever lost in the system
                      \%s
402
                      0.0.0
403
404
             [ trains at diff positions
405
             ; no derailment
406
             ; trains detected on points
407
             ; all trains arrived
408
             ; no malfunction when train has not arrived
409
               all messages handled
410
             > String.concat "\n"
411
412
    /// Functions for composing a UMC model
413
    module UMCModelConstruction =
414
         let private objects section objects =
415
              modelO\,bjectInstantiation \ objects
416
             | > sprintf "Objects \ n \%s"
417
418
         let private abstractions section objects =
419
             objects
420
             > AbstractionDefinitions.all abstraction declarations
421
             | > sprintf "Abstractions {\n%s\n}"
422
423
         {\tt let \ private \ properties\_section \ objects = }
424
             ModelCheckingProperties(objects)
425
             > collect Model Properties
426
427
428
         let composeModel : ModelGeneratorFunction = fun objects ->
             [ train class
429
             ; linear_class
430
             ; point class
431
432
             ; objects section objects
             ; abstractions_section objects
433
              ; properties section objects ]
434
             |> String.concat "\n"
435
```

E.3.7 XMLExtraction.fs

```
namespace XMLExtraction
1
2
   open FSharp.Data
3
   open Utils
4
\mathbf{5}
   open InterlockingModel
6
    /// Required types and extensions of existing types
7
   [<AutoOpen>]
8
9
   module TypeDefinitions =
10
        |<Literal>|
        let sample_xml file = "sample.xml"
11
        // Loading the type provider with a sample file
12
13
        type RailwayXML = XmlProvider<sample xml file>
14
15
        (* Modules and functions for more convenient access of
           values extracted by the type provider *)
16
17
       module XMLRoute =
18
            let Id (route : RailwayXML.Route) : string = route.Id
19
20
       module TrackSection =
21
            let Id (track section : RailwayXML. TrackSection) : string
22
                = track section.Id
            let Type (track_section : RailwayXML.TrackSection) :
23
                string = track section.Type
24
        module Neighbor =
25
            let Id (neighbor : RailwayXML.Neighbor) : string =
26
                neighbor.Ref
27
            let Side (neighbor : RailwayXML.Neighbor) : string =
                neighbor.Side
28
        module MarkerBoard =
29
30
            let Id (markerboard : RailwayXML.Markerboard) : string =
                markerboard.Id
31
            let Track (markerboard : RailwayXML.Markerboard) : string
                = markerboard.Track
32
33
        module Condition =
34
            let Type (condition : RailwayXML.Condition) : string =
                condition . Type
35
            let Ref (condition : RailwayXML.Condition) : string =
                condition.Ref
36
37
        type PointPosition with
            static member from String : string -> Point Position =
38
                function
39
                  "plus"
                          -> Plus
                  "minus" -> Minus
40
41
42
        type RouteDirection with
43
            static member from String : string -> RouteDirection =
                function
```

```
44
                    "up" \longrightarrow Up
                    "down" -> Down
45
46
        type LayoutSegment with
47
             static member from String (id : string) : string * string
48
                 -> LayoutSegment =
49
                  function
                    "linear", _____ -> LinearLayoutSegment id
"point", "stem" -> PointStemLayoutSegment id
"point", "plus" -> PointForkLayoutSegment (id, Plus)
50
51
52
                    "point", "minus" -> PointForkLayoutSegment (id,
53
                      Minus)
54
    [<AutoOpen>]
55
    module BasicObjectExtraction =
56
        type ModelObjectsExtractionParameters =
57
             { xml_file_path : string
58
59
                train_ids : TrainIds
                train length : int
60
                routes : Routes }
61
         /// Extracts all trains, points and linears from xml file
62
         let extractBasicModelObjectsFromXML :
63
             ModelObjectsExtractionParameters \rightarrow ModelObjects =
64
             fun parameters ->
             let xml = RailwayXML.Load parameters.xml file path
65
             let linears : (LinearId * Linear) seq =
66
67
                  xml. Interlocking. Network. TrackSections
68
                  > Seq.choose
                      (fun track section ->
69
70
                       match track_section Type with
                        | "linear" ->
71
72
                            Some(LinearId track section.Id,
                                  \{ id = LinearId track section.Id \}
73
74
                                     train = None \})
75
                            \rightarrow None)
             let points : (PointId * Point) seq =
76
77
                  xml. Interlocking. Network. TrackSections
                  > Seq.choose
78
                      (fun track section ->
79
                       match track_section.Type with
80
                        | "point" ->
81
                            Some(PointId track section.Id,
82
                                    { id = PointId track section.Id
83
                                      position = Plus)
84
             | = -> \text{ None } )
| = -> \text{ None } )
85
86
                  List.zip parameters.train ids parameters.routes
87
                  |> List.map (fun (id, route) ->
88
89
                                 id, { id = id; route = route; length =
                                      parameters.train length })
90
             let basic objects : ModelObjects =
                  { trains = trains |> Map.ofList
91
                    points = points |> Map.ofSeq
92
                    linears = linears |> Map ofSeq \}
93
94
             basic objects
```

```
95
    [<AutoOpen>]
96
97
    module LayoutExtraction =
         /// Retrieves all connection pairs from a given xml file.
98
         /// Assumes that the layout defined in the xml file is
99
             well-formed
100
         let createLayoutFromXML (path : string) :
             Result < Railway Network Layout, string > =
101
             let xml = RailwayXML.Load path
102
             let elements = xml. Interlocking. Network. TrackSections
103
             /// getting the adjacent neighbor type
             /// if its a linear then its straightforward
104
105
             /// if its a point then we have to figure out if its the
                 stem or one of the forks
             let getNeighborType : string -> string ->
106
                 Result < LayoutSegment, string > =
                 fun from id to id -> resultFlow {
107
108
                 let! element =
                      elements
109
                      |> Seq.tryFind (TrackSection.Id >> (=)to id)
110
                      > function
111
                           | None -> Error (sprintf "no tracksection with
112
                               id %s" to id)
                          Some element \rightarrow Ok element
113
114
                 let! from neighbor =
                      element. Neighbors
115
116
                      |> Seq.tryFind (Neighbor.Id >> (=)from id)
117
                      > function
                            Some neighbor -> Ok neighbor
118
                            None -> sprintf "could not find %s in
119
                               neighbors of %s" to id from id
120
                                     > Error
                  return LayoutSegment.fromString to id (element.Type,
121
                      from neighbor.Side) }
122
             /// All connection pairs going from linear to other
123
             let linears : Result <LayoutSegment * LayoutSegment ,</pre>
124
                 \operatorname{string} > \operatorname{seq} =
                 let isLinearWithUpNeighbor : RailwayXML.TrackSection
125
                      \rightarrow bool =
126
                      fun element ->
                      let element is linear = element.Type = "linear"
127
                      let element has up neighbor =
128
                          element.Neighbors |> Seq.exists (Neighbor.Side
129
                              >> (=)"up")
                      (element is linear && element has up neighbor)
130
131
                 let getFromIdAndToId : RailwayXML.TrackSection ->
132
                      string * string =
                      fun element ->
133
                      let from id = element.Id
134
                      let neighbor = element.Neighbors |> Seq.find
135
                          (Neighbor.Side >> (=)"up")
                      let to id = n eighbor Ref
136
                      from_id, to_id
137
```

```
139
                  let getLayoutElementPair
140
                       : string * string -> Result < Layout Segment *
                           LayoutSegment, string > =
141
                      fun (from id, to id) \rightarrow
                      let from element = LinearLayoutSegment from id
142
143
                      let to element = getNeighborType from id to id
                       Result<_,_>.map (fun to_el -> from_element, to_el)
144
                           to element
145
                  elements
146
                  > Seq.filter isLinearWithUpNeighbor
147
                  |> Seq.map (getFromIdAndToId >> getLayoutElementPair)
148
149
150
              let getLayoutElementPair
                  : string -> RailwayXML.Neighbor ->
151
                      Result < LayoutSegment * LayoutSegment, string > =
152
                  fun from id neighbor ->
                  let neighbor id = neighbor.Ref
153
                  let from_element =
154
                      LayoutSegment.fromString from id ("point",
155
                           neighbor.Side)
                  getNeighborType from id neighbor id
156
                  |> Result<_,_>.map (fun to_element -> from element,
157
                      to element)
158
              /// All connection pairs going from point to other
159
              let points : Result < LayoutSegment * LayoutSegment, string >
160
                  seq = seq {
161
                  for element in elements |> Seq.filter
                       (TrackSection.Type >> (=)"point") do
162
                      let from id = element.Id
                      for neighbor in element. Neighbors do
163
                           yield getLayoutElementPair from id neighbor }
164
165
              linears; points
             > Seq.concat
166
             > List.ofSeq
167
             | > \operatorname{Result} <\_, \_> . \operatorname{sequence}
168
             | > \text{Result} < , > \text{map Map. of List}
169
170
    [<AutoOpen>]
171
    module RouteExtraction =
172
         let extractRouteFragmentFromXML (path : string) (linear length
173
              : int) (route id : string)
174
                                             : Result <Route, string > =
                                                 resultFlow {
175
              let xml = RailwayXML.Load path
176
177
              let route = xml. Interlocking. Routetable. Routes
                           |> Seq.tryFind (XMLRoute.Id >> (=)route id)
178
179
              let ! (route : RailwayXML.Route) =
180
                  xml. Interlocking. Routetable. Routes
181
                  >> Seq.tryFind (XMLRoute.Id >> (=)route id)
182
                  > function
183
```

138

```
184
                        Some route \rightarrow Ok route
                        None -> Error (sprintf "no route with id %s"
185
                          route id)
186
             let markerboard src id : string = route.Source
187
188
189
             let! (linear src id : string) =
                 xml. Interlocking. Network. Markerboards
190
191
                 > Seq.tryFind (MarkerBoard.Id >>
                      (=) markerboard src id)
192
                 > function
                      Some markerboard -> Ok markerboard. Track
193
194
                      None -> Error (sprintf "no markerboard for id
                          %s" markerboard src id)
195
             let points : (string * PointPosition) seq =
196
                 route. Conditions
197
198
                 |> Seq.filter (Condition.Type >> (=)"point")
                 |> Seq.map (fun condition ->
199
                              let pos = Option.get condition.Val
200
                              let \quad id = condition.Ref
201
202
                              let point pos = PointPosition.fromString
                                   pos
                              (id, point pos) )
203
204
             // if the id exists as a point id then the id is a point
205
             let tryGetPoint : string -> (string * PointPosition)
206
                  option =
                 fun id -> points |> Seq.tryFind (fst >> (=)id)
207
208
             let vacancies : RouteSegments =
209
                 let routeElement : RailwayXML.Condition ->
210
                      RouteSegment =
211
                      fun condition ->
                      let id = condition.Ref
212
213
                      match tryGetPoint id with
                      Some (id, pos) -> PointRouteSegment(PointId id,
214
                          pos)
215
                      None
                                       -> LinearRouteSegment (LinearId id,
                          linear length)
                 route.Conditions
216
                 |> Seq.filter (Condition.Type >> (=)"trackvacancy")
217
218
                 > Seq.map routeElement
219
                 > List.ofSeq
220
             let! (direction : RouteDirection) =
221
222
                 xml. Interlocking. Network. Markerboards
                  > Seq.tryFind (MarkerBoard.Id >>
223
                      (=) markerboard src id)
224
                 > function
                      | None -> Error (sprintf "no markerboard with id
225
                          %s" markerboard src id)
                      | Some markerboard \rightarrow
226
                          markerboard. Mounted
227
228
                          > RouteDirection.fromString
```

```
229
                           |> Ok
230
              let first element = LinearRouteSegment(LinearId
231
                  linear src id, linear length)
232
              let route elements = first element :: vacancies
233
234
              return Route (route elements, direction) }
235
236
         let extractRouteFragmentsFromXML (path : string) (train len :
              int) (route ids : string list)
237
                                               : Result < Route, string > =
              \label{eq:let_extract} \texttt{let} \ \texttt{extractRouteFragment} \ : \ \texttt{string} \ -\!\!\!> \ \texttt{Result}\!<\!\!\texttt{Route}\,, \ \texttt{string}\!>
238
                  = fun route id ->
                  extractRouteFragmentFromXML path train len route id
239
240
              route ids
              > Seq.map extractRouteFragment
241
              |> Result<_,_>.reduce stitchRoutePair
242
243
     [<AutoOpen>]
244
     module ModelGenerationFromXML =
245
         type ModelGenerationParameters =
246
              { modelGeneratorFunction : ModelGeneratorFunction
247
                xml file path : string
248
                routes : string list list }
249
         let generateModelFromXML : ModelGenerationParameters ->
250
              Result < string, string > =
251
              fun parameters -> resultFlow {
252
              let default train length = 2
              let extractRouteFragments : string list ->
253
                   Result < Route, string > =
                   extractRouteFragmentsFromXML parameters.xml file path
254
                       default train length
              let! (routes : Route list) =
255
256
                   parameters.routes
                   | > Result <_ , _>.traverse extractRouteFragments
257
258
              let! (layout : RailwayNetworkLayout) = createLayoutFromXML
259
                   parameters.xml file path
              let validateAndGenerate = validateAndGenerateModel
260
                   parameters.modelGeneratorFunction
261
262
              let train ids = [0 \dots Seq.length routes - 1]
                                |> List map (sprintf "%i" >> TrainId)
263
264
265
              let! model =
                      xml file path = parameters.xml file path
266
267
                      train ids = train ids
                      train length = default_train_length
268
269
                      routes = routes }
                   > extractBasicModelObjectsFromXML
270
                   > validateAndGenerate layout
271
272
              return model }
273
```

E.3.8 ScriptTools.fs

```
namespace ScriptingTools
1
2
   open InterlockingModel
3
   open XMLExtraction.LayoutExtraction
4
   open UMC
5
   open Utils
6
7
   open System.IO
8
9
   [<AutoOpen>]
10
   module SimpleTypes =
       type SimpleTrackSegment = LLinear of name : string
11
                                  | LPointFork of name : string *
12
                                      PointPosition
                                  LPointStem of name : string
13
14
        let (<+>) (el1 : SimpleTrackSegment) (el2 :
            SimpleTrackSegment) = el1, el2
        type SimpleLayout = (SimpleTrackSegment * SimpleTrackSegment)
15
            list
16
        type SimpleRouteElement =
17
            RLinear of name : string * length : int
18
            RPoint of name : string * position : PointPosition
19
        type SimpleRoute = SimpleRouteElement list
20
21
        type SimpleTrain =
22
23
            { id : string
24
            ; length : int
            ; route : SimpleRoute
25
            ; route direction : RouteDirection }
26
        type SimpleTrains = SimpleTrain list
27
28
29
        type LayoutType = CustomLayout of SimpleLayout
30
                         XMLLayout of path : string
31
32
        type SimpleModelArgs =
33
            { trains : SimpleTrain list
34
            ; layout : LayoutType
35
            ; show stats : bool
36
            ; output file : string option }
37
        type Stats =
38
39
            { num of trains : int
40
            ; train lengths : int list
            ; route lengths : int list
41
42
            ; total route sub segments : int
            ; total linears : int
43
44
            ; total points : int
45
            ; shared points : int
46
            ; shared linears : int }
47
48
        type SimpleRouteElement with
49
            static member Length (element : SimpleRouteElement) =
50
                match element with
```

51		RLinear(_,len) -> len
52		-> 1
53		
54	/// Fun	ctions for converting script model representation to
55	/// to a	a validated internal representation
56	[<autoo< td=""><td>pen >l</td></autoo<>	pen >l
57	module	Script Tools =
58 58	let	private toLavoutSegment · SimpleTrackSegment ->
00	100	Lavout Segment -
59		function
60 60		I Point Fork (n Plus) > Point Fork I avout Sogmont (n Plus)
00		LP of $nt F of K(n, F f us) -> F of nt F of K Layout Segment (n, F f us)$
01 60		LP of the form of
62 60		L Pointstein n -> PointsteinLayoutsegment n
63		LLinear n -> LinearLayoutSegment n
64		
65	type	e SimpleRouteElement with
66		static member toRouteSegment : SimpleRouteElement ->
		RouteSegment =
67		function
68		RLinear(n,len) -> LinearRouteSegment (LinearId n,
		len)
69		RPoint(n, Plus) -> PointRouteSegment (PointId n,
		Plus)
70		RPoint(n, Minus) -> PointRouteSegment (PointId n,
		Minus)
71		
72	let	private getRailwayLayoutFromCustom (custom layout :
		SimpleLayout) : RailwayNetworkLayout =
73		custom layout
74		> List.map (fun (ell, el2) -> toLayoutSegment ell,
		toLavoutSegment el2)
75		> Map. of List
76		1, t
77	let	private getRoute (train : SimpleTrain) : Route =
 78		let route elements -
79		train route
80		∖ List man SimpleRouteElement toRouteSegment
80 81		Route (route elements train route direction)
01		foure (foure_crements, train.foure_diffection)
04 09	lot	private setTrains (trains , SimpleTrain list) , Trains -
00 04	Iet	p_{11} p_{12} p
04 07		$\begin{bmatrix} \text{id} & \text{Train} \\ \text{id} & \text{Train} \\ \end{bmatrix} = \begin{bmatrix} \text{id} & \text{Irain} \\ \text{id} & \text{Irain} \\ \end{bmatrix}$
00		tu = frainfu t.fu; fengti = t.fengti; foute =
		getRoute t }
86		trains > List.map toTrain
87		
88	111	Extract linears from layout
89	let	private getLinears (layout : RailwayNetworkLayout) :
		Linears =
90		Map toList layout
91		> List.unzip
92		> List.append
93		> List.choose
94		(function
95		<pre>LinearLayoutSegment n -> Some({id = LinearId n;</pre>
		train = None

```
_ -> None)
96
                   |> Set.ofList
97
98
             > Set.toList
99
100
         /// Extract points from layout
         let private getPoints (layout : RailwayNetworkLayout) : Points
101
102
             Map.toList layout
103
             > List.unzip
             ||> List.append
104
105
             > List.choose
                  (function
106
                   | PointForkLayoutSegment(n, _)
| PointStemLayoutSegment n -> Some({id = PointId n;
107
108
                       position = Plus})
                     \rightarrow None)
109
                   | _
             |> Set of List
110
111
             > Set.toList
112
         let private getObjects (trains : SimpleTrains) (layout :
113
             RailwayNetworkLayout)
                                  : ModelObjects =
114
             let train ids = trains |> List.map (fun t -> TrainId t.id)
115
             let trains map : Map<TrainId, Train> =
116
117
                  List.zip train ids (getTrains trains)
                  > Map. of List
118
119
             let linears = getLinears layout
120
             let linear ids = linears |> List.map Linear.id
121
122
             let linears map : Map<LinearId,Linear> =
                  List.zip linear ids linears
123
124
                  > Map. of List
125
             let points = getPoints layout
126
             let point ids = points |> List.map Point.id
127
             let points map : Map<PointId,Point> =
128
                  List.zip point ids points
129
                  > Map. of List
130
             { trains = trains map
131
                linears = linears map
132
                points = points map }
133
134
         /// Pretty print the raw layout from an XML file
135
136
         let printRawLayout (path : string) =
137
              let layoutSegmentToSimple segment =
                  match segment with
138
139
                  | LinearLayoutSegment id -> LLinear id
                  | PointForkLayoutSegment(id, pos) -> LPointFork(id,
140
                      pos)
                  | PointStemLayoutSegment id -> LPointStem id
141
                  | > sprintf "%A"
142
143
             let layout = resultFlow {
144
145
                  let! layout = createLayoutFromXML path
                  let output layout =
146
```

```
147
                       layout
                       > Map.toList
148
                       |> List .map (fun (x,y) ->
149
                                      let x simple = layoutSegmentToSimple x
150
                                      let y_simple = layoutSegmentToSimple y
151
                                      \operatorname{sprintf} "%s <+> %s"
152
                                          (x_simple.PadRight 24) y_simple)
                  return output_layout |> String.concat "\n" }
153
154
              match layout with
              | Ok layout_string -> printfn "%s" layout string
155
              | Error msg -> printfn "ERROR: %s" msg
156
157
         let private generateStats (trains : SimpleTrains) (layout :
158
              RailwayNetworkLayout) : Stats =
              let num of trains = trains |> List.length
159
              let train lengths = trains |> List.map (fun {length=len}
160
                  \rightarrow len)
161
              let route_lengths = trains |> List.map (fun {route=r} ->
                  List.length r)
              let total route sub segments =
162
                  trains
163
                  |> Seq.map
164
                       (fun \{route=r\} \rightarrow
165
                        Seq.map (SimpleRouteElement.Length) r |> Seq.sum)
166
                  |> Seq.sum
167
              let total linears = getLinears layout |> List length
168
              let total points = getPoints layout |> List.length
169
170
              let getPointNames = function RPoint(n, ) \rightarrow Some n \mid ->
171
                  None
                                    > Seq.choose
172
              let shared points =
173
                  uniqueProducts trains
174
                  |> Seq.map (fun ({route=r1}, {route=r2}) >
175
                                let r1_points = r1 |> getPointNames |>
176
                                    \operatorname{Set} . of \operatorname{Seq}
                                let r2_points = r2 | > getPointNames | >
177
                                    \operatorname{Set} . of \operatorname{Seq}
                                Set.intersect r1 points r2 points)
178
                  > Seq.map Set.count
179
                  > Seq.sum
180
              let getLinearNames = function RLinear(n, ) -> Some n
181
                  -> None
182
                                      |> Seq.choose
              let shared linears =
183
                  unique Products trains
184
185
                  |> Seq.map (fun ({route=r1}}, {route=r2}) >
                                let r1 linears = r1 | getLinearNames | >
186
                                    Set.ofSeq
                                let r2 linears = r2 | getLinearNames | >
187
                                    Set.ofSeq
                                Set.intersect r1 linears r2 linears)
188
                  > Seq.map Set.count
189
                  > Seq.sum
190
              { num of trains = num of trains
191
```

192		; train lengths = train lengths
193		; route lengths = route lengths
194		; total route sub segments = total route sub segments
195		; total linears = total linears
196		total points = total points
197		; shared points = shared points
198		; shared linears = shared linears }
199		
200		
201	let	generateUMCModel (model_args : SimpleModelArgs) : unit =
202		let validateAndGenerate =
203		${ m UMCModelConstruction}$. composeModel
204		> validateAndGenerateModel
205		let output = resultFlow {
206		let! layout =
207		match model args.layout with
208		CustomLayout custom layout ->
209		Ok(getRailwayLayoutFromCustom custom layout)
210		XMLLayout path -> createLayoutFromXML path
211		let trains = model args trains
212		let objects = $getObjects$ trains layout
213		<pre>let! model = validateAndGenerate layout objects</pre>
214		let stats = generateStats trains layout
215		let output =
216		if model args.show stats then
217		$sprintf$ "STATS: $n A \in n $ and $sprintf$ "STATS: $n A \in n $
218		else sprintf "MODEL:\n%s" model
219		return output }
220		match output, model args.output file with
221		Ok output, None -> printfn "%s" output
222		Ok output, Some file path ->
223		File.WriteAllText(file_path, output)
224		printfn "model written to file %s" file_path
225		$ $ Error msg,> printfn "ERROR:\n%s" msg

E.3.9 MiniModelGenerator.fs

```
module MiniModelGenerator
1
\mathbf{2}
   open System. Text. RegularExpressions
3
4
   open InterlockingModel
   open UMC
5
   open XMLExtraction
6
7
   open Utils
8
   open System
9
   open System.IO
10
   type ModelOutput = UMC
11
                      | Raw // representing the raw F# objects
12
13
14
   type ModelOutput with
        static member from String (s : string) : Result < ModelOutput,
15
             \operatorname{string} > =
            match s. ToLower() with
16
```

```
17
               "umc" -> Ok UMC
               "raw" -> Ok Raw
18
               _ -> Error "wrong model type"
19
20
21
    let parseItin arg =
        match Regex ("[^ \langle | \rangle] + "). Match arg with
22
        | m when m. Success && m. Value <> "" ->
23
^{24}
             let parsed =
                 m. Value. Split ','
25
                 |> Array.filter ((<>)"")
26
27
                 > List.ofArray
             if \ {\rm Seq} \ length \ parsed \ > \ 0
28
29
             then Ok parsed
             else Error "error in itinerary argument no routes provided"
30
        -> Error "error in itinerary argument"
31
32
    let parseInt arg = 
33
34
        match Int32. TryParse arg with
         | true, x -> Ok x
35
         -> Error (sprintf "not an integer: %A" arg)
36
37
    let getPath curr dir path arg =
38
        if \ File. Exists \ path\_arg
39
        then Ok path arg
40
        else
41
             let full path = sprintf "%s/%s" curr_dir path_arg
42
             if File Exists full path
43
             then Ok full path
44
             else Error (sprintf "no file with path %s" path arg)
45
46
    [<EntryPoint>]
47
    let main argv =
48
        let curr dir = Directory.GetCurrentDirectory()
49
        if Array length argv < 4 then
50
             [ "Following arguments must be provided (in same order):"
51
               "1. file-path of xml file"
52
               "2. model type (umc|raw)"
53
               "3. itinerary for train 1 in the form [r 1, r 2,...]"
54
               "4. itinerary for train 2 in the form [r 3, r 4,...]"
55
               "5. ... "]
56
             > String.concat "\n"
57
            | > printfn "%s"
58
        else
59
60
          let model = resultFlow {
               let! path = getPath curr_dir argv.[0]
61
               let ! model_output_type = ModelOutput.fromString argv.[1]
62
               let! routes =
63
                    [2 \dots \text{Array.length} argv - 1]
64
65
                   |> Result<_,_>.traverse
    (fun arg_id -> resultFlow {
66
                         let! route = parseItin argv. [arg id]
67
                         return route })
68
69
               let parameters =
                    { modelGeneratorFunction = generateRawModel
70
71
                      xml file path = path
```

72	routes = routes }
73	let! model =
74	match model output type with
75	Raw -> generateModelFromXML parameters
76	$UMC \rightarrow$
77	{ parameters with modelGeneratorFunction =
	UMCModelConstruction.composeModel }
78	> generateModelFromXML
79	return model }
80	match model with
81	Ok model -> printfn "%s" model
82	Error err —> printfn "ERROR: \n%s" err
83	0 // return an integer exit code

E.3.10 Prelude.fsx

```
1
   (*
\mathbf{2}
       Loading the required files and assemblies for the scripts
3
   *)
4
\mathbf{5}
   // required assembly for parsing xml files
6
   #r "../../ packages/FSharp.Data/lib/net40/FSharp.Data.dll"
7
8
   (* loading required files *)
9
10
   #load "Utils.fs"
   #load "Interlocking Model.fs"
11
   #load "UMCTrainClass.fs"
12
   #load "UMCLinearClass.fs"
13
   #load "UMCPointClass.fs"
14
   #load "UMC.fs"
15
   #load "XMLExtraction.fs"
16
   #load "ScriptTools.fs"
17
18
   open ScriptingTools
19
```

E.3.11 Script.fsx

A sample script for defining a model using the DSL scripting tools library.

```
1
   (*
\mathbf{2}
      Example script for generating a UMC model with a custom layout
   *)
3
4
   #load "Prelude.fsx"
5
6
   (* importing required modules *)
7
   open InterlockingModel
8
9
   open ScriptingTools
10
   (* Define the trains and routes to be used in the model *)
11
```

```
let trains : SimpleTrains =
12
         [ \{ id = "1" \}
13
14
              length = 3
              route = [ RLinear(name = "1", length = 3)
15
                        ; RPoint (name = "1", position = Plus)
16
                        ; RLinear (name = "2", length = 2)
17
                        ; RPoint (name = "2", position = Plus)
; RLinear (name = "4", length = 3) ]
18
19
20
              route direction = Up }
            \{ id = \overline{"2"} \}
21
22
              length = 3
              route = [ RLinear(name = "4", length = 3)
23
                        ; RPoint (name = "2", position = Minus)
; RLinear (name = "3", length = 3) ]
24
25
              route direction = Down } ]
26
27
    (* Define the network layout in a 'left-to-right' fashion,
28
        using '+>' to indicate connection between elements *)
29
    let network layout : SimpleLayout =
30
         [ LLinear "1"
                                       <+> LPointStem "1"
31
         ; LPointFork("1", Plus) <+> LLinear "2"
; LPointFork("1", Minus) <+> LLinear "3"
32
33
         ; LLinear "2"
                                       <+> LPointFork("2", Plus)
34
         ; LLinear "3"
                                       <+> LPointFork("2", Minus)
35
         ; LPointStem "2"
                                       <+> LLinear "4" ]
36
37
    (* Generate model based on the definitions above *)
38
39
    generateUMCModel { trains = trains
                         ; layout = CustomLayout (network_layout)
40
41
                         ; show stats = true
                         ; output file = Some "mymodel.txt" }
42
```

E.4 Tests

This section defines a few unit tests and property based tests that all evaluates to true for the current source code.

E.4.1 Tests.Utils.fs

Testing selected functions from the Utils module.

```
    namespace Tests.Utils
    open Utils
    module crossProductOfLists =
    open Xunit
    open FsUnit.Xunit
```

```
7
        open FsCheck.Xunit
8
9
        [< Fact >]
        let ''simple test1'' () =
10
             let result = crossProductOfLists [1;2] ["a";"b"] |>
11
                 Set.ofSeq
             let expected = Set.ofList [1, "a"; 1, "b"; 2, "a"; 2, "b"]
12
13
             result |> should equal expected
14
        [< Property >]
15
16
        let ''length of cross product list is n**2, where n is the
             length of one of the input lists "
17
             (xs : int list) =
             let result =
18
                 crossProductOfLists xs xs
19
                 > List.ofSeq
20
                 > List.length
21
22
             let expected = float (List.length xs) **2.0 |> int
             result = expected
23
24
25
   module uniqueProducts =
26
        open FsCheck
27
        open FsCheck. Xunit
28
29
        let sets bigger than two : Arbitrary<NonEmptySet<int>> =
30
             Arb. Default.NonEmptySet<int>()
31
32
             | Arb.filter (fun x -> Set.count x.Get >= 2)
             > Arb.filter (fun x -> Set.count x.Get <= 12)
33
34
        let n choose k n k =
35
             let rec factorial n =
36
                 match n with
37
                  n when n = 0 \rightarrow 1
38
                  n when n = 1 \rightarrow 1
39
                  n \rightarrow factorial(n - 1) * n
40
             (factorial n) / ((factorial k)*(factorial (n - k)))
41
42
        [< Property >]
43
        let "product elements are unique in each product "() =
44
             Prop.forAll sets bigger than two (fun xs ->
45
                 List ofSeq xs.Get
46
                 > uniqueProducts
47
                 |> Seq.map (fun (e1, e2) -> e1 <> e2)
48
49
                 | > Seq.reduce (&&))
50
51
        //[<Property (Verbose = true) >]
        [< Property >]
52
        let ''n choose k products produced''() =
53
             \label{eq:prop.forAll_sets_bigger_than_two (fun xs ->
54
                 let input = xs.Get
55
                 let n = Set.count input
56
                 let k = 2
57
                 let expected = n choose k n k
58
                 let result =
59
```

```
60
                        List.ofSeq input
61
                        > uniqueProducts
                        > Seq.length
62
                   expected = result)
63
64
65
    module Result =
66
67
         open Xunit
         open FsUnit.Xunit
68
69
70
         [< Fact >]
          let ''simple success test of flow'' () =
71
              let result : Result <int , string > = resultFlow {
72
                   let! x = Ok 42
73
                   let! y = Ok 3
74
                   return x + y }
75
              let expected : Result < int , string > = Ok 45
76
              result \mid > should equal expected
77
78
         [< Fact >]
79
          let ''simple fail test of flow '' () =
80
              let result = resultFlow {
81
                   let ! x = Ok 42
82
                   let! y = Error "wrong"
83
                   return x + y }
84
              let expected : Result <int , string > = Error "wrong"
85
              result |> should equal expected
86
87
         [< Fact >]
88
89
          let "simple success test of sequence" () =
              let input = [Ok 1; Ok 2; Ok 3]
90
91
              let expected = Ok [1;2;3]
              let result = Result<_, > sequence input
result |> should equal expected
92
93
94
         [< Fact >]
95
          let ''simple fail test of sequence'' () =
96
              let input = [Ok 1; Error "wrong"; Ok 3]
97
              let expected : Result <int list , string > = Error "wrong"
98
              let result = Result<_, >.sequence input
result |> should equal expected
99
100
101
         [< Fact >]
102
          let ''simple success test of traverse'' () =
103
104
              let input = [1 .. 5]
              let expected : Result < int list , string > = Ok [1 \quad 5]
105
              let result =
106
                   input
107
108
                   | > Result < , > .traverse
                        (function
109
                         | n when n = 0 \rightarrow Error "wrong"
110
                         | n \rightarrow Ok n \rangle
111
              result |> should equal expected
112
113
114
         [< Fact >]
```

```
115
          let "simple fail test of traverse" () =
               let input = [0 \dots 5]
116
               let expected : Result < int list , string > = Error "wrong"
117
               let result =
118
119
                    input
                    | > \ {\rm Result} <\_\,, \_>\, . \, t \, r \, a \, v \, e \, r \, s \, e
120
121
                         (function
122
                           | n when n = 0 \rightarrow Error "wrong"
123
                           | n \rightarrow Ok n \rangle
               result |> should equal expected
124
125
     module maybe =
126
127
          open Xunit
          open FsUnit. Xunit
128
129
130
          [< Fact >]
          let ''simple success test of maybe flow '' () =
131
               let result : int option = maybe {
132
                    let! x = Some 42
133
                   let! y = Some 3
134
                   return x + y }
135
               let expected : int option = Some 45
136
               result \ | > \ should \ equal \ expected
137
138
139
          [< Fact >]
          let ''simple fail test of maybe flow '' () =
140
               let result : int option = maybe {
141
142
                    let! x = Some 42
                    let! y = None
143
144
                    return x + y 
               let expected : int option = None
145
146
               result |> should equal expected
```

E.4.2 Tests.InterlockingModel.fs

Testing selected functions from the InterlockingModel module.

```
namespace Tests.InterlockingModel
1
\mathbf{2}
   open Utils
   open InterlockingModel
3
4
   module RouteConstruction =
5
       open FsCheck
6
        open FsCheck.Xunit
7
8
9
        /// Generate integers bigger than zero
10
        let int bigger than zero =
            Arb.generate<NonNegativeInt>
11
            |> Gen.where (fun i -> i.Get > 0)
12
13
14
        /// Generator of random routes
```

```
15
        let routeGen : Gen<Route> =
16
            let route s =
17
                let direction = Arb.generate<RouteDirection>
                let linear segment id (l : NonNegativeInt) =
18
                     LinearRouteSegment(LinearId id, l.Get)
19
                let point segment id p =
20
21
                     PointRouteSegment(PointId id, p)
22
                let segment id =
                     [Gen.map (linear_segment id) int_bigger_than_zero
23
^{24}
                     ; Gen.map (point segment id)
                         Arb.generate<PointPosition> ]
                     > Gen.oneof
25
26
                let segments =
27
                     [for id in [1..s] |> Seq.map string -> segment id]
                     |> Gen.sequence
28
                Gen map2 (fun s d -> Route(s,d)) segments direction
29
            Gen.sized route
30
31
        let validRouteArb : Arbitrary <Route> =
            Arb.fromGen routeGen
32
            > Arb.filter
33
                (fun (Route(segments,_)) ->
34
                 let first is linear =
35
                     match Seq.head segments with
36
37
                       LinearRouteSegment -> true
                        —> false
38
                 let last is linear =
39
                     match Seq.last segments with
40
                      | LinearRouteSegment _ -> true
41
                        | _-> fals
first_is_linear
42
43
                 && last is linear)
44
45
        [< Property >]
46
        let ''route split in half and stitched with stitchRoutePair
47
            yields same route '' () =
            Prop for All valid Route Arb
48
                (fun route ->
49
                 let (Route(all segments, dir)) = route
50
                 let half = (List.length all segments) / 2
51
                 let segments1 = List.take half all segments
52
                 let segments 2 = \text{List.skip} (\text{half}-1) all segments
53
                 let route1 = Route(segments1, dir)
54
                 let route2 = Route(segments2, dir)
55
                 let result = stitchRoutePair route1 route2
56
                 match result with
57
                  | Ok result route -> result route = route
58
                  Error msg -> raise (System.ArgumentException(msg)))
59
60
        // gen route from layout and verifyRoutes
61
        // gen length constrained routes and checkLengthConstraints
62
```

Appendix F

Experiment Scripts

This chapter contains the scripts used to generate the models used as experiments in the Experiments chapter.

F.1 SimpleTwoTrains.fsx

Generates 10 models with an increasing number of stations, where the first model have one station and the last have ten stations.

```
1
   #load "Prelude.fsx"
\mathbf{2}
   open InterlockingModel
3
   open ScriptingTools
4
5
6
   let basic layout (names : string list) =
        let [\overline{1}1; p_2; 13; 14; p_5; 16] = names
7
        [ LLinear 11
                                  <+> LPointStem p2
8
        ; LPointFork(p2, Plus) <+> LLinear 13
9
        ; LPointFork(p2, Minus) <+> LLinear 14
10
        ; LLinear 13
11
                                 <+> LPointFork(p5, Plus)
        ; LLinear 14
                                 <+> LPointFork (p5, Minus)
12
        ; LPointStem p5
13
                                <+> LLinear 16
14
   let generateLayout (N : int) : SimpleLayout =
15
```

```
16
        let layouts = seq {
             for n in [0..N-1] do
17
18
                 let start = n * 5 + 1
                 let end' = start + 5
19
20
                 let layout = [start .. end']
                              > List.map string
21
22
                              |> basic layout
23
                 yield layout }
24
        List.ofSeq layouts
25
        > List.concat
26
    let generateRoute layout map (segment : SimpleTrackSegment) (pos :
27
        PointPosition) =
28
        let rec loop segment = seq {
            yield segment
29
            let next segment = layout map |> Map.tryFind segment
30
            match next segment with
31
            | Some segment ' \rightarrow
32
                 match segment' with
33
                   LPointStem n -> yield! loop (LPointFork(n, pos))
34
                  LPointFork(n, ) \rightarrow yield! loop (LPointStem n)
35
                  -> yield! loop segment'
36
             | None -> () }
37
38
        loop segment
39
    let generateTrains (t1 length : int) (t2 length : int) (layout :
40
        SimpleLayout) : SimpleTrains =
        let layout map = Map. of List layout
41
        let route\overline{1} =
42
43
            generateRoute layout map (LLinear "1") Plus
            > List.ofSeq
44
            > List.map (function
45
                            LLinear n \rightarrow RLinear(n, t1 length)
46
                           | LPointStem n | LPointFork(n, ) \rightarrow RPoint(n, )
47
                               Plus))
        let route2 =
48
            generateRoute layout map (LLinear "4") Minus
49
            > List.ofSeq
50
            > List.map (function
51
52
                            LLinear n \rightarrow RLinear(n, t2 length)
                           | LPointStem n | LPointFork(n, ) \rightarrow RPoint(n,
53
                               Minus))
54
            > List.rev
        [ \{id = "1"; length = t1_length; route = route1; \}
55
            route direction = Up
        ; {id = "\overline{2}"; length = t2 length; route = route2;
56
            route direction = Down ]
57
58
   for i in [1..10] do
        let layout = generateLayout i
59
60
        let trains = generateTrains 2 2 layout
        let output file = sprintf
61
            "../../UMCModels/SimpleTwoTrains/model%i.umc" i
        generateUMCModel \{ trains = trains \}
62
63
                           ; layout = CustomLayout layout
```

64 ; show_stats = true 65 ; output_file = Some output_file }

F.2 BranchManyTrains.fsx

Generates four models with an increasing number of trains, where the first model have two trains and the last have four trains.

(The script can easily be adjusted to generate more models with more trains. However, as already mentioned in the Experiments chapter, a model even with just four trains can take many hours to model check)

```
1
   #load "Prelude.fsx"
2
3
   open InterlockingModel
   open ScriptingTools
4
5
6
   let branchLayout xs =
        let rec loop xs = seq 
7
8
            match xs with
9
            | [x;y] \rightarrow
10
                let prev = x + y
                let prev id = string prev
11
12
                yield LPointFork(prev id, Plus), LLinear (string x)
13
                yield LPointFork(prev id, Minus), LLinear (string y)
14
            xs when List.length xs > 2 \rightarrow
                let current id = xs |> Seq.sum |> string
15
16
                let half = (List.length xs) / 2
                let xs_left = xs |> List.take half
17
18
                 let xs right = xs |> List.skip half
                let stem left id = xs left |> Seq.sum |> string
19
                let stem right id = xs right |> Seq.sum |> string
20
21
                yield LPointFork(current id, Plus), LPointStem
22
                     stem left id
23
                 yield! loop xs left
                 yield LPointFork(current id, Minus), LPointStem
24
                     stem right id
                yield! loop xs right
25
26
            -> () }
        let tail = xs |> loop |> List.ofSeq
27
        let stem id = xs |> Seq.sum |> string
28
        let head = LLinear "0", LPointStem stem id
29
30
        head :: tail
31
   let getRouteTrace layout map start end' =
32
33
        let rec loop prev route =
34
            match layout map |> Map.tryFind prev with
35
            Some(LLinear n) when (LLinear n) = (LLinear end') \rightarrow
36
                RLinear(n, 2) :: route
37
            | Some(LLinear n) ->
```

```
38
                 (RLinear(n,2) :: route)
39
                 |> loop (LLinear n)
40
             | Some(LPointStem n) ->
                 let result left =
41
                     //(LPointFork(n, Plus) :: route) |> loop
42
                     (RPoint(n, Plus) :: route)
43
44
                     | > loop (LPointFork(n, Plus))
45
                 let result right =
46
                     //(LPointFork(n, Minus) :: route) |> loop
                     (RPoint(n, Minus) :: route)
47
48
                     |> loop (LPointFork(n, Minus))
                 match result left, result right with
49
50
                 | x :: x s, [ ] \rightarrow x :: x s
51
                   [], y ::: y s \to y ::: y s
                    —> []
52
             Some(LPointFork(n, pos)) ->
53
                 //(LPointStem n :: route) |> loop
54
55
                 (RPoint(n,pos) :: route)
                 |> loop (LPointStem n)
56
             None -> []
57
        loop (LLinear start) [RLinear(start, 2)]
58
59
60
    let dualBranch (levels : int) (num trains : int) =
        let size = int (2.0 * * (float levels))
61
        let [xs; ys] = [1..2*size] |> List.chunkBySize size
62
        let right = branchLayout ys
63
        let left = branchLayout xs |> List.map (fun (x,y) \rightarrow y,x)
64
65
        let layout = [left; right] |> List.concat
        let layout map = Map of List layout
66
67
        let getRouteInLayout = getRouteTrace layout map
        let trains =
68
69
            List.zip xs ys
            > List.map
70
71
                 (fun (l1, l2) ->
                  let lin1 = string l1
72
                  let lin 2 = string 12
73
                  let route = getRouteInLayout lin1 lin2
74
                  {id=lin1; length=2; route=route;
75
                      route direction=Down})
76
            > List.take num trains
            | > List of Seq
77
        layout, trains
78
79
    for i in [2..4] do
80
        let layout, trains = dualBranch 2 i
81
        let output file = sprintf
82
            "../../UMCModels/ManyTrains2/model%i.umc" i
        generateUMCModel { trains = trains
83
84
                           ; layout = CustomLayout layout
85
                           ; show stats = true
                           ; output file = Some output file }
86
```

Appendix G

XML sample

This chapter contains an example of a concrete XML file which is used by the developed system.

The file is referred to as *sample.xml* because it is used by the F# type provider to bootstrap the knowledge about the types stemming from XML files with similar layouts.

The XML file was originally created by Linh H. Vu, and has been obtained from the RobustRailS research project[Col, Hax] repository.



Figure G.1: The network represented in the XML file

```
1 <? xml version = "1.0" encoding = "UTF-8"?>
```

```
2 <xmi:XMI xmi:version="2.4.1"
```

```
\mathbf{xmlns}: \mathbf{xmi}{=}"\; h\; t\; t\; p: / \; / \; www.\; omg\;.\; o\; r\; g \; / \; s\; p\; e\; c \; / \; XMI \; / \; 2 \; . \; 4 \; . \; 1 \; ">
```

```
3 <xmi: Documentation exporter="DK-IXL" exporterVersion="0.1"/>
```

```
<interlocking id="mini" version="0.1">
4
        <network id="mininetwork">
5
            <trackSection id="b10" length="100" type="linear">
6
                 <neighbor ref="t10" side="up"/>
7
8
            </trackSection>
            <trackSection id="t10" length="87" type="linear">
9
                 <neighbor ref="b10" side="down"/>
10
                 <neighbor ref="t11" side="up"/>
11
12
            </trackSection>
            <trackSection id="t11" length="26" pointMachine="spskt11"</pre>
13
                 type="point">
                 <neighbor ref="t10" side="stem"/>
14
                 <neighbor ref="t12" side="plus"/>
15
                 <neighbor ref="t20" side="minus"/>
16
17
            </trackSection>
            <trackSection id="t12" length="3783" type="linear">
18
                 <neighbor ref="t11" side="down"/>
19
                 <neighbor ref="t13" side="up"/>
20
            </trackSection>
21
            <trackSection id="t13" length="81" pointMachine="spskt13"</pre>
22
                 type="point">
                 <neighbor ref="t12" side="plus"/>
23
                 <neighbor ref="t20" side="minus"/>
24
                 <neighbor ref="t14" side="stem"/>
25
26
            </trackSection>
            <trackSection id="t14" length="128" type="linear">
27
                 <neighbor ref="t13" side="down"/>
28
                 <neighbor ref="b14" side="up"/>
29
            </trackSection>
30
31
            <trackSection id="b14" length="128" type="linear">
                 <neighbor ref="t14" side="down"/>
32
            </trackSection>
33
            <trackSection id="t20" length="76" type="linear">
34
                 <neighbor ref="t11" side="down"/>
35
                 <neighbor ref="t13" side="up"/>
36
            </trackSection>
37
            <markerboard distance="50" id="mb10" mounted="up"
38
                 t r a c k = "b 10" />
            <markerboard distance="50" id="mb11" mounted="down"
39
                 t\,r\,a\,c\,k{=}"\,t\,1\,0 " /{>}
            <markerboard distance="50" id="mb12" mounted="down"
40
                 track="t12"/>
            <markerboard distance="50" id="mb13" mounted="up"
41
                 t r a c k = "t 1 2 " />
            <markerboard distance="50" id="mb14" mounted="up"
42
                 t r a c k = "t 1 4 " />
            <markerboard distance="50" id="mb15" mounted="down"
43
                 t r a c k = "b 1 4" />
            <markerboard distance="50" id="mb20" mounted="down"
44
                 \mathrm{t}\,r\,a\,c\,k{=}"\,\mathrm{t}\,2\,0 " /{>}
            <markerboard distance="50" id="mb21" mounted="up"
45
                 \mathrm{t\,r\,a\,c\,k}{=}"\,\mathrm{t\,2\,0} " /{>}
        </network>
46
   <routetable id="miniroutetable" network="mininetwork">
47
      <route id="r 1a" source="mb10" destination="mb13" dir="up">
48
```

```
<condition type='point' val='plus' ref='t11'/>
49
        <condition type='point' val='minus' ref='t13'/>
50
        <condition type='signal' ref='mb11'/>
51
        <condition type='signal' ref='mb12'/>
52
        <condition type='signal' ref='mb20'/>
53
        <condition type='trackvacancy' ref='t10'/>
54
        <condition type='trackvacancy' ref='t11'/>
55
        <condition type='trackvacancy' ref='t12'/>
56
        <condition type='mutualblocking' ref='r 5b'/>
57
        <condition type='mutualblocking' ref='r 7 '/>
58
        <condition type='mutualblocking' ref='r_6b'/>
59
        <condition type='mutualblocking' ref='r 5a'/>
60
        <condition type='mutualblocking' ref='r_2a'/>
61
        <condition type='mutualblocking' ref='r 1b'/>
62
        <condition type='mutualblocking' ref='r 3 '/>
63
        <condition type='mutualblocking' ref='r_2b'/>
64
        <condition type='mutualblocking' ref='r 4 '/>
65
66
      </route>
      <route id="r 1b" source="mb10" destination="mb13" dir="up">
67
        <condition type='point' val='plus' ref='t11'/>
68
        <condition type='signal' ref='mb11'/>
69
        <condition type='signal' ref='mb12'/>
70
        <condition type='signal' ref='mb15'/>
71
        <condition type='signal' ref='mb20'/>
72
        < condition type='signal' ref='mb21'/>
73
        <condition type='trackvacancy' ref='t10'/>
74
        <condition type='trackvacancy' ref='t11'/>
75
        <condition type='trackvacancy' ref='t12'/>
76
        <condition type='mutualblocking' ref='r 5b'/>
77
        <condition type='mutualblocking' ref='r_6b'/>
78
        <condition type='mutualblocking' ref='r 2b'/>
79
        <condition type='mutualblocking' ref='r 6a'/>
80
        <condition type='mutualblocking' ref='r<sup>2</sup>a'/>
81
        82
        <condition type='mutualblocking' ref='r
                                                3
                                                    />
83
                                                7^{-}, ^{\prime}/>
        <condition type='mutualblocking' ref='r
84
        <condition type='mutualblocking' ref='r 5a'/>
85
        <condition type='mutualblocking' ref='r 1a'/>
86
      </\mathrm{route}>
87
      <route id="r 2a" source="mb10" destination="mb21" dir="up">
88
        <condition type='point' val='minus' ref='t11'/>
89
        <condition type='point' val='plus' ref='t13'/>
90
        <condition type='signal' ref='mb11'/>
91
        <condition type='signal' ref='mb12'/>
92
        <condition type='signal' ref='mb20'/>
93
        <condition type='trackvacancy' ref='t10'/>
94
        <condition type='trackvacancy' ref='t11'/>
95
        <condition type='trackvacancy' ref='t20'/>
96
        <condition type='mutualblocking' ref='r 6a'/>
97
        98
99
        <condition type='mutualblocking' ref='r 2b'/>
100
        <condition type='mutualblocking' ref='r 5b'/>
101
        <condition type='mutualblocking' ref='r_6b'/>
102
        <condition type='mutualblocking' ref='r 8 '/>
103
```

```
104
                   <condition type='mutualblocking' ref='r 1a'/>
                   <condition type='mutualblocking' ref='r 1b'/>
105
106
              </\mathrm{route}>
               <route id="r 2b" source="mb10" destination="mb21" dir="up">
107
                   <condition type='point ' val='minus' ref='t11'/>
108
                   <condition type='signal' ref='mb11'/>
109
                   <condition type='signal' ref='mb12'/>
110
                   <condition type='signal' ref='mb13'/>
111
                   <condition type='signal' ref='mb15'/>
112
                   <condition type='signal' ref='mb20'/>
113
                   <condition type='trackvacancy' ref='t10'/>
114
                   <condition type='trackvacancy' ref='t11'/>
115
                   <condition type='trackvacancy' ref='t20'/>
116
                   <condition type='mutualblocking' ref='r 6b'/>
117
                   <condition type='mutualblocking' ref='r 5b'/>
118
                   <condition type='mutualblocking' ref='r 7 '/>
119
                   <condition type='mutualblocking' ref='r 5a'/>
120
                   <condition type='mutualblocking' ref='r_3_</pre>
121
                                                                                                                         15
                   <condition type='mutualblocking' ref='r 4 '/>
122
                   <condition type='mutualblocking' ref='r 6a'/>
123
                   <condition type='mutualblocking' ref='r 1b'/>
124
                   <condition type='mutualblocking' ref='r<sup>2</sup>a'/>
125
                   <condition type='mutualblocking' ref='r 1a'/>
126
127
              </\mathrm{route}>
              <\! \texttt{route id} = "r \ 3 \ " \ \texttt{source} = "mb12" \ \texttt{destination} = "mb11" \ \texttt{dir} = "\texttt{down}" > \texttt{tource} = \texttt{mb11}" \ \texttt{dir} = \texttt{mb11}" \ \texttt{d
128
                   <condition type='point ' val='plus ' ref='t11'/>
129
                   <condition type='signal' ref='mb10'/>
130
                   <condition type='signal' ref='mb20'/>
131
                   <condition type='trackvacancy' ref='t11'/>
132
                   <condition type='trackvacancy' ref='t10'/>
133
                   <condition type='mutualblocking' ref='r 5a'/>
134
                   <condition type='mutualblocking', ref='r 6b'/>
135
                   <condition type='mutualblocking' ref='r 7 '/>
136
                   <condition type='mutualblocking' ref='r 2a'/>
137
                   <condition type='mutualblocking' ref='r 1b'/>
138
                   <condition type='mutualblocking', ref='r_2b'/>
139
                   <condition type='mutualblocking' ref='r 1a'/>
140
              </\mathrm{route}>
141
                   <route id="r 4 " source="mb13" destination="mb14" dir="up">
142
                   <condition type='point' val='plus' ref='t13'/>
143
                   <condition type='signal' ref='mb15'/>
144
                   <condition type='signal' ref='mb21'/>
145
                   <condition type='trackvacancy' ref='t13'/>
146
                   <condition type='trackvacancy' ref='t14'/>
147
                   <condition type='mutualblocking' ref='r 6b'/>
148
                   <condition type='mutualblocking' ref='r 5a'/>
149
                   <condition type='mutualblocking' ref='r 6a'/>
150
                   <condition type='mutualblocking' ref='r 5b'/>
151
                   <condition type='mutualblocking' ref='r 8 '
152
                   <condition type='mutualblocking' ref='r la'/>
153
                   <condition type='mutualblocking' ref='r_2b'/>
154
              </\mathrm{route}>
155
              <route id="r 5a" source="mb15" destination="mb12" dir="down">
156
                   <condition type='point' val='minus' ref='t11'/>
157
                   <condition type='point' val='plus' ref='t13'/>
158
```

201

```
<condition type='signal' ref='mb14'/>
160
        <condition type='signal' ref='mb21'/>
161
        <condition type='trackvacancy' ref='t14'/>
162
        <condition type='trackvacancy' ref='t13'/>
163
        <condition type='trackvacancy' ref='t12'/>
164
165
        <condition type='mutualblocking' ref='r 6b'/>
        <condition type='mutualblocking' ref='r_5b'/>
166
        <condition type='mutualblocking' ref='r 6a'/>
167
        <condition type='mutualblocking' ref='r_8 '/>
168
        <condition type='mutualblocking' ref='r_3'/>
169
        <condition type='mutualblocking' ref='r 1a'/>
170
        <condition type='mutualblocking' ref='r 4 '/>
171
        <condition type='mutualblocking' ref='r 2b'/>
172
        <condition type='mutualblocking' ref='r 1b'/>
173
174
      </route>
      <route id="r 5b" source="mb15" destination="mb12" dir="down">
175
        <condition type='point' val='plus' ref='t13'/>
176
        <condition type='signal' ref='mb10'/>
177
        <condition type='signal' ref='mb13'/>
178
        <condition type='signal' ref='mb14'/>
179
        <condition type='signal' ref='mb20'/>
180
        <condition type='signal' ref='mb21'/>
181
        <condition type='trackvacancy' ref='t14'/>
182
        <condition type='trackvacancy' ref='t13'/>
183
        <condition type='trackvacancy' ref='t12'/>
184
        <condition type='mutualblocking' ref='r 7 '/>
185
        <condition type='mutualblocking' ref='r_6b'/>
186
        <condition type='mutualblocking' ref='r 6a'/>
187
        <condition type='mutualblocking' ref='r 8 '/>
188
        <condition type='mutualblocking' ref='r
                                                  1a'/>
189
        <condition type='mutualblocking' ref='r_2b'/>
190
        <condition type='mutualblocking' ref='r</pre>
                                                  1b'/>
191
        <condition type='mutualblocking' ref='r 4 '/>
192
        <condition type='mutualblocking' ref='r 5a'/>
193
        <condition type='mutualblocking' ref='r 2a'/>
194
195
      </\mathrm{route}>
      <route id="r 6a" source="mb15" destination="mb20" dir="down">
196
        <condition type='point ' val='plus' ref='t11'/>
197
        <condition type='point' val='minus' ref='t13'/>
198
        <condition type='signal' ref='mb13'/>
199
        <condition type='signal' ref='mb14'/>
200
        <condition type='signal' ref='mb21'/>
201
        <condition type='trackvacancy' ref='t14'/>
202
        <condition type='trackvacancy' ref='t13'/>
203
        <condition type='trackvacancy' ref='t20'/>
204
        <condition type='mutualblocking' ref='r 8 '/>
205
        <condition type='mutualblocking' ref='r 6b'/>
206
        <condition type='mutualblocking' ref='r</pre>
                                                  7 '
207
                                                      />
        <condition type='mutualblocking' ref='r 2a'/>
208
        <condition type='mutualblocking' ref='r</pre>
209
                                                  1b'/>
        <condition type='mutualblocking' ref='r 4 '/>
210
        <condition type='mutualblocking' ref='r 5b'/>
211
        <condition type='mutualblocking' ref='r 5a'/>
212
        <condition type='mutualblocking' ref='r 2b'/>
213
```

<condition type='signal' ref='mb13'/>

159

```
214
               </route>
               <route id="r 6b" source="mb15" destination="mb20" dir="down">
215
                    <condition type='point ' val='minus' ref='t13'/>
216
                    < condition type='signal' ref='mb10'/>
217
                    <condition type='signal' ref='mb12'/>
218
                    <condition type='signal' ref='mb13'/>
219
                    <condition type='signal' ref='mb14'/>
220
                    <condition type='signal' ref='mb21'/>
221
                    <condition type='trackvacancy' ref='t14'/>
222
                    <condition type='trackvacancy' ref='t13'/>
223
                    <condition type='trackvacancy' ref='t20'/>
224
                    <condition type='mutualblocking' ref='r 8 '/>
225
                    <condition type='mutualblocking' ref='r 3'/>
226
                    <condition type='mutualblocking' ref='r 5a'/>
227
                    <condition type='mutualblocking' ref='r 2b'/>
228
                    <condition type='mutualblocking' ref='r 1b'/>
229
                    <condition type='mutualblocking' ref='r 4 '/>
230
                    <condition type='mutualblocking' ref='r 1a'/>
231
                    <condition type='mutualblocking' ref='r 5b'/>
232
                    <condition type='mutualblocking' ref='r_6a'/>
233
                    <condition type='mutualblocking' ref='r 2a'/>
234
               </route>
235
236
               <\! \texttt{route id} = "r \ 7 \ " \ \texttt{source} = "mb20" \ \texttt{destination} = "mb11" \ \texttt{dir} = "\texttt{down}" > 1000 \ \texttt{dir} = \texttt{down} = 
                    <condition type='point ' val='minus' ref='t11'/>
237
                    <condition type='signal' ref='mb10'/>
238
                    <condition type='signal' ref='mb12'/>
239
                    <condition type='trackvacancy' ref='t11'/>
240
                    <condition type='trackvacancy' ref='t10'/>
241
                    <condition type='mutualblocking' ref='r 2a'/>
242
                   <condition type='mutualblocking' ref='r 1a'/>
243
                    <condition type='mutualblocking' ref='r_2b'/>
244
                    <condition type='mutualblocking' ref='r 5b'/>
245
                    <condition type='mutualblocking' ref='r 1b'/>
246
                    <condition type='mutualblocking' ref='r 3 '/>
247
                    <condition type='mutualblocking' ref='r 6a'/>
248
249
               </\mathrm{route}>
               <route id="r 8 " source="mb21" destination="mb14" dir="up">
250
                    <condition type='point ' val='minus' ref='t13'/>
251
                    <condition type='signal' ref='mb13'/>
252
                    <condition type='signal' ref='mb15'/>
253
                    <condition type='trackvacancy' ref='t13'/>
254
                    <condition type='trackvacancy' ref='t14'/>
255
                    <condition type='mutualblocking' ref='r 6a'/>
256
                    <condition type='mutualblocking' ref='r_6b'/>
257
                    <condition type='mutualblocking' ref='r lb'/>
258
                    <condition type='mutualblocking' ref='r_5b'/>
259
                    <condition type='mutualblocking' ref='r 4 '
260
                    <condition type='mutualblocking' ref='r 5a'/>
261
                    <condition type='mutualblocking' ref='r_2a'/>
262
263
               </\mathrm{route}>
264
          </r></routetable>
          </interlocking>
265
          </xmi:XMI>
266
```
Bibliography

- [BRA13] EDWIN BRADY. Idris, a general-purpose dependently typed programming language: Design and implementation. Journal of Functional Programming, 23:552-593, 9 2013.
- [CEN11] CENELEC European Committee for Electrotechnical Standardization. EN 50128:2011 – Railway applications – Communications, signalling and processing systems – Software for railway control and protection systems, 2011.
- [CH11] Koen Claessen and John Hughes. Quickcheck: a lightweight tool for random testing of haskell programs. Acm Sigplan Notices, 46(4):53–64, 2011.
- [Col] Multiple Collaborators. About RobustRailS. http://www. robustrails.man.dtu.dk/About-the-project. [Online; accessed November-2016].
- [Fan12] Alessandro Fantechi. Distributing the Challenge of Model Checking Interlocking Control Tables. In Leveraging Applications of Formal Methods, Verification and Validation. Applications and Case Studies, pages 276–289, 2012.
- [Fol15] Andreas Foldager. A graphical domain-specific language for railway interlocking systems, et grafisk domænespecifikt sprog for jernbanesikringsanlæg, 2015.
- [Hax] Anne E. Haxthausen. RobustRailS research project. http:// www.imm.dtu.dk/~aeha/RobustRailS/index/. [Online; accessed November-2016].

- [Hax14] Anne E. Haxthausen. An Institution for Imperative RSL Specifications. In Shusaku Iida, José Meseguer, and Kazuhiro Ogata, editors, Specification, Algebra, and Software. Essays Dedicated to Kokichi Futatsugi, number 8373 in Lecture Notes in Computer Science, pages 441-464. Springer, 2014.
- [HP00] Anne E. Haxthausen and Jan Peleska. Formal Development and Verification of a Distributed Railway Control System. *IEEE Transaction* on Software Engineering, 26(8):687–701, 2000.
- [maa] Open Source multiple authors. Fscheck. https://fscheck.github. io/FsCheck/. [Online; accessed 17-October-2016].
- [mab] Open Source multiple authors. Fsharp.data. http://fsharp.github. io/FSharp.Data. [Online; accessed 17-October-2016].
- [mac] Open Source multiple authors. Nuget. https://www.nuget.org/. [Online; accessed 17-October-2016].
- [mad] Open Source multiple authors. Xunit testing framework. https: //github.com/xunit/xunit. [Online; accessed 17-October-2016].
- [Maza] Franco Mazzanti. UMC 3.3 User Guide. http://fmt.isti.cnr.it/ umc/V4.2/umc.html. [Online; accessed 10-October-2016].
- [Mazb] Franco Mazzanti. Umc web tool. http://fmt.isti.cnr.it/umc/V4. 2/umc.html.
- [Maz09] Franco Mazzanti. Designing uml models with umc. Technical report, Technical report, Technical Report 2009-TR-43, Istituto di Scienza e Tecnologie dell'Informazione "A. Faedo", CNR, 2009.
- [mInB16] Danish magazine "Ingeniøren" and German newspaper "Bild". "forkert nødopkald fra togleder var skyld i fatogulykke", 2016.http://ing.dk/artikel/ tal tysk forkert-noedopkald-fra-togleder-var-skyld-i-fatal-tysk-togulykke-183119 http://www.bild.de/news/inland/ and zugunglueck-bad-aibling/der-tragische-zweite-fehler-des-fahrdienstleiters-45 bild.html, accessed: March 2016.
- [Pao10] Marco Paolieri. Modellazione di un sistema di interlocking distribuito tramite lo strumento umc. 2010.
- [PGS16] Tomas Petricek, Gustavo Guerra, and Don Syme. Types from data: Making structured data first-class citizens in f#. 2016.

- [PS14] Tomas Petricek and Don Syme. The f# computation expression zoo. Lecture Notes in Computer Science (including Subseries Lecture Notes in Artificial Intelligence and Lecture Notes in Bioinformatics), 8324:33-48, 2014.
- [TV09] Gregor. Theeg and Sergej. Vlasenko. Railway signalling and interlocking : international compendium. Eurailpress, 2009.
- [VHP16] Linh Hong Vu, Anne E. Haxthausen, and Jan Peleska. Formal modelling and verification of interlocking systems featuring sequential release. Science of Computer Programming, pages -, 2016.
- [Wika] Wikipedia. Mars climate orbiter. https://en.wikipedia.org/wiki/ Mars_Climate_Orbiter.
- [wikb] wikipedia. Monads. https://en.wikipedia.org/wiki/Monad_ (functional_programming)#Continuation_monad.
- [Wikc] Wikipedia. Therac-25. https://en.wikipedia.org/wiki/ Therac-25.