

Problem 9.3.2

We consider a M/G/1 system with $\lambda = 1$. We can choose between two methods

$$A: \nu = \frac{1}{2}, \tau^2 = 1/5,$$

$$B: \nu = \frac{2}{5}, \tau^2 = 9/10.$$

We apply eq. (9.36) twice to compare the methods:

$$\begin{aligned} W_a &= \nu + \lambda(\tau^2 + \nu^2)/2(1-\rho), \quad (\rho = \lambda\nu) \\ &= \frac{1}{2} + \frac{9}{20}\lambda/(2-\lambda), \end{aligned}$$

$$\begin{aligned} W_b &= \nu + \lambda(\tau^2 + \nu^2)/2(1-\rho) \\ &= \frac{2}{5} + \frac{53}{50}\lambda/(2 - \frac{4}{5}\lambda). \end{aligned}$$

For $\lambda = 1$: $W_a = 19/20$ and $W_b = 77/60$,
i.e. method A is best here.

Note however that method A becomes unstable before (system) method B. You will also find that W_b will be less than W_a for higher values of λ .