Solution for exercise 4.1.1 in Karlin and Pinsky

Let X_n be the amount of balls in urn A. Than the transition matrix can be written as

$$P = \begin{pmatrix} \frac{1}{2} & \frac{1}{2} & 0 & 0 & 0 & 0\\ \frac{1}{2} & 0 & \frac{1}{2} & 0 & 0 & 0\\ 0 & \frac{1}{2} & 0 & \frac{1}{2} & 0 & 0\\ 0 & 0 & \frac{1}{2} & 0 & \frac{1}{2} & 0\\ 0 & 0 & 0 & \frac{1}{2} & 0 & \frac{1}{2}\\ 0 & 0 & 0 & 0 & \frac{1}{2} & \frac{1}{2} \end{pmatrix}$$

Since the matrix is doubly stochastic we can state the stationary distribution immediately. $\pi = \begin{pmatrix} \frac{1}{6} & \frac{1}{6} & \frac{1}{6} & \frac{1}{6} & \frac{1}{6} & \frac{1}{6} \end{pmatrix}$ and therefore the fraction of time where urn A is empty is $\pi_0 = \frac{1}{6}$