02405 Probability 2003-11-12 BFN/bfn

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Question b) We have

$$P\left(Y > \frac{1}{4} \middle| |X| > \frac{1}{2}\right) = 1 \neq \frac{1}{2} = P\left(Y > \frac{1}{4}\right)$$

thus X and Y are *not* independent.