

IMM - DTU

02405 Probability

2003-10-17

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The distribution of  $Y$  is symmetric around 0 so  $E(Y) = 0$ .