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$$\frac{d \tan(\Phi)}{d\Phi}$$

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$$f_Y(y)$$

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$$f_Y(y) = \frac{1}{\pi} \frac{1}{1 + y^2}, -\infty < y < \infty$$

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$$f_Y(y) = \frac{1}{\pi} \frac{1}{1 + y^2}, \quad -\infty < y < \infty$$

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The integral $\int_{-\infty}^{\infty} y f_Y(y) dy$ has to converge absolutely for $E(Y)$ to exist, i.e. $E(Y)$ exists if and only if $E(|Y|)$ exists (e.g. page 263 bottom).