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2003-10-5
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$$\frac{e^{-\lambda}}{\lambda} \sum_{i=0}^{\infty} \frac{\lambda^{i+1}}{(i+1)!} = \frac{1}{\lambda} (1 - e^{-\lambda})$$