Solution for exercise 5.1.6 in Pitman

Question a) Define A_1 and A_2 as the arrival times of Jack and Jill respectively. The probability in question is

$$P(A_2 > A_1 + 2) = \frac{1}{2} \left(\frac{13}{15}\right)^2 = \frac{169}{450} = 0.3756$$

Question b) As in the textbook we will denote $A_{(1)}$ as the smallest and $A_{(10)}$ as the largest of the ten arrival times. The probability in question is $P(A_{(1)} < 5, 10 < A_{(10)})$. This probability has been analyzed in exercise 4.6.3 d) page 330. From that exercise we derive

$$P(A_{(1)} < 5, 10 < A_{(10)}) = 1 - (1 - x)^n - y^n + (y - x)^n = 1 - \left(\frac{2}{3}\right)^{10} - \left(\frac{2}{3}\right)^{10} + \left(\frac{1}{3}\right)^{10}$$
$$= 1 - \frac{1}{3^{10}}(2^{11} - 1)$$

can be solved this way using E.4.6.3, I am looking for a shortcut before finishing the solution. However 4.6.3 is scheduled two weeks before this one.