Solution for exercise 3.1.1 in Pitman

Question a) The probabilities P(X=i), i=0,1,2,3 are given by the bino-

mial distribution,
$$P(X=i)=\left(\begin{array}{c}3\\i\end{array}\right)\frac{1}{2^3}.$$

$$\begin{array}{c|c} i&P(X=i)\\\hline 0&\frac{1}{8}\\\hline 1&\frac{3}{8}\\\hline 2&\frac{3}{8}\\\hline 3&\frac{1}{8}\\\hline \end{array}$$

Question b) We define a random variable Y = |X - 1|, with range 0,1,2.

| Then | i | P(Y=i) |
|------|---|---------------|
| | 0 | 3 8 |
| | 1 | $\frac{1}{2}$ |
| | 2 | $\frac{1}{8}$ |