Solution for exercise 2.2.6 in Pitman

We introduce the events O_i to describe that i voters in the survey oppose the measure. From section 2.1 box at bottom of page 81 we deduce that X is binomially distributed.

Question a) The probability in question is (page 81)

$$P(O_{90}) = \begin{pmatrix} 200\\90 \end{pmatrix} 0.45^{90} 0.55^{110}$$

We evaluate this probability by approximation page 99.

$$P(O_{90}) = \Phi\left(\frac{90 + \frac{1}{2} - 0.45 \cdot 200}{\sqrt{200 \cdot 0.45 \cdot (1 - 0.45)}}\right) - \Phi\left(\frac{90 - \frac{1}{2} - 0.45 \cdot 200}{\sqrt{200 \cdot 0.45 \cdot (1 - 0.45)}}\right)$$
$$= \Phi(0.07) - \Phi(-0.07) = 2 \cdot \Phi(0.07) - 1 = 0.056$$

Question b) The probability in question is

 $P(\text{more than } 100 \text{ voters oppose the measure}) = P\left(\bigcup_{i=101}^{200} O_i\right) \tilde{=}$

$$\Phi\left(\frac{200 + \frac{1}{2} - 0.45 \cdot 200}{\sqrt{200 \cdot 0.45 \cdot (1 - 0.45)}}\right) - \Phi\left(\frac{101 - \frac{1}{2} - 0.45 \cdot 200}{\sqrt{200 \cdot 0.45 \cdot (1 - 0.45)}}\right) = 1 - \Phi(1.49) = 0.0681$$