## Homework 1



- The R-multicast algorithm satisfies validity, since a correct process will eventually *B-deliver* the message to itself.
- The algorithm satisfies integrity, because of
  - (1) the integrity property of the underlying communication channels
  - (2) the fact that duplicates are not delivered.

What about agreement? It follows because... HOMEWORK! :-)





#### TECHNICAL UNIVERSITY OF DENMARK

(M.Sc.Eng.-course)

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### TOPIC 2 (28%): Multicast Communication

Let us consider ordered multicast in distributed systems. Well known ordering delivery requirements are *total ordering*, *causal ordering* and *FIFO ordering*.

### **PROBLEM 2.1 (6%)**

For each of the three ordering delivery requirements, define the delivery requirement and draw an example of computation in which the requirement is met.

### **PROBLEM 2.2 (12%)**

For each of the following 6 statements indicate whether the statement is true or false. In the latter case (that is, the statement is false), justify your answer by means of a counterexample.

Statement 1 (2%): Total ordering implies FIFO ordering.

Statement 2 (2%): FIFO ordering implies total ordering.

Statement 3 (2%): Total ordering implies causal ordering.

Statement 4 (2%): Causal ordering implies total ordering.

Statement 5 (2%): FIFO ordering implies causal ordering.

Statement 6 (2%): Causal ordering implies FIFO ordering.

#### **PROBLEM 2.3 (10%)**

Show informally that if two processes use a FIFO-ordered variant of B-multicast, then the totally ordered multicast is also causally ordered.

# Homework 3



FIFO ordered multicast can be achieved by means of sequence numbers. A key assumption of the basic FIFO multicast algorithm (informally sketched in Figure 2) is that processes are organized in non-overlapping groups.

```
    A process p has variables:

    S<sup>p</sup><sub>o</sub>: how many messages p has sent to group g

   • R<sup>9</sup><sub>a</sub> : sequence number of the latest message p has delivered from
     process q that was sent to group g

    For p to FO-multicast a message to group g:

     it piggy backs the value SPg onto the message;
     it B-multicasts the message to g;
     S_{q}^{p} = S_{q}^{p} + 1.

    Upon a receipt of a message from q bearing the seq. number S, p checks:

    IF (S = R^{q}_{a} + 1) THEN it FO-delivers the message, setting R^{q}_{a} := S.
    ELSIF (S > R^{q}_{a} + 1) THEN
       it places the message in its hold-back queue until
       the intervening messages have been delivered and
       S = R^{q}_{\alpha} + 1.
```

Figure 2: Basic FIFO Multicast Algorithm





Question 1: Show that the FIFO multicast algorithm does not work for overlapping groups.

*Question 2:* Adapt the FIFO multicast algorithm to work for this case, that is considering also overlapping groups of processes.

Homework 4



 Suggest how to adapt the causally ordered multicast protocol to handle overlapping groups.

## Homework 5



• Let us consider the reliable multicast algorithm. Explain why reversing the order of lines 11-12 makes the algorithm no longer satisfy agreement.

```
On initialization
 2
      Received := \{\};
 3
   For process p to R-multicast message m to group g
 4
      B-multicast(g, m); // p \in g is included as a destination
 5
 6
   On B-deliver(m) at process q with g = group(m)
 7
      if (m \notin Received)
 8
      then
 9
                  Received := Received \cup {m};
10
                  if (q \neq p) then B-multicast(g, m); end if
11
                  R-deliver m;
      end if
13
```