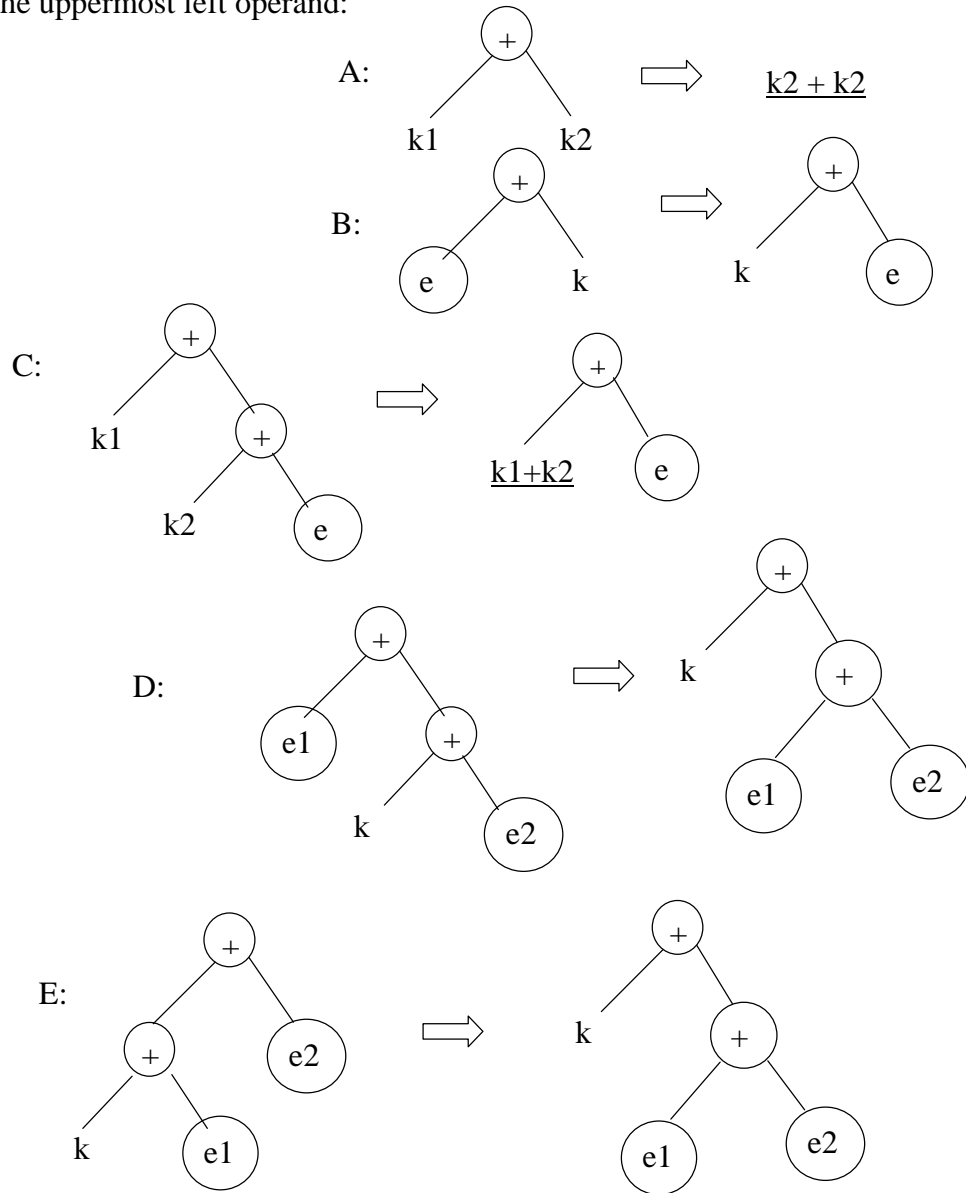


## Simplifying Expressions by Tree-Rewriting

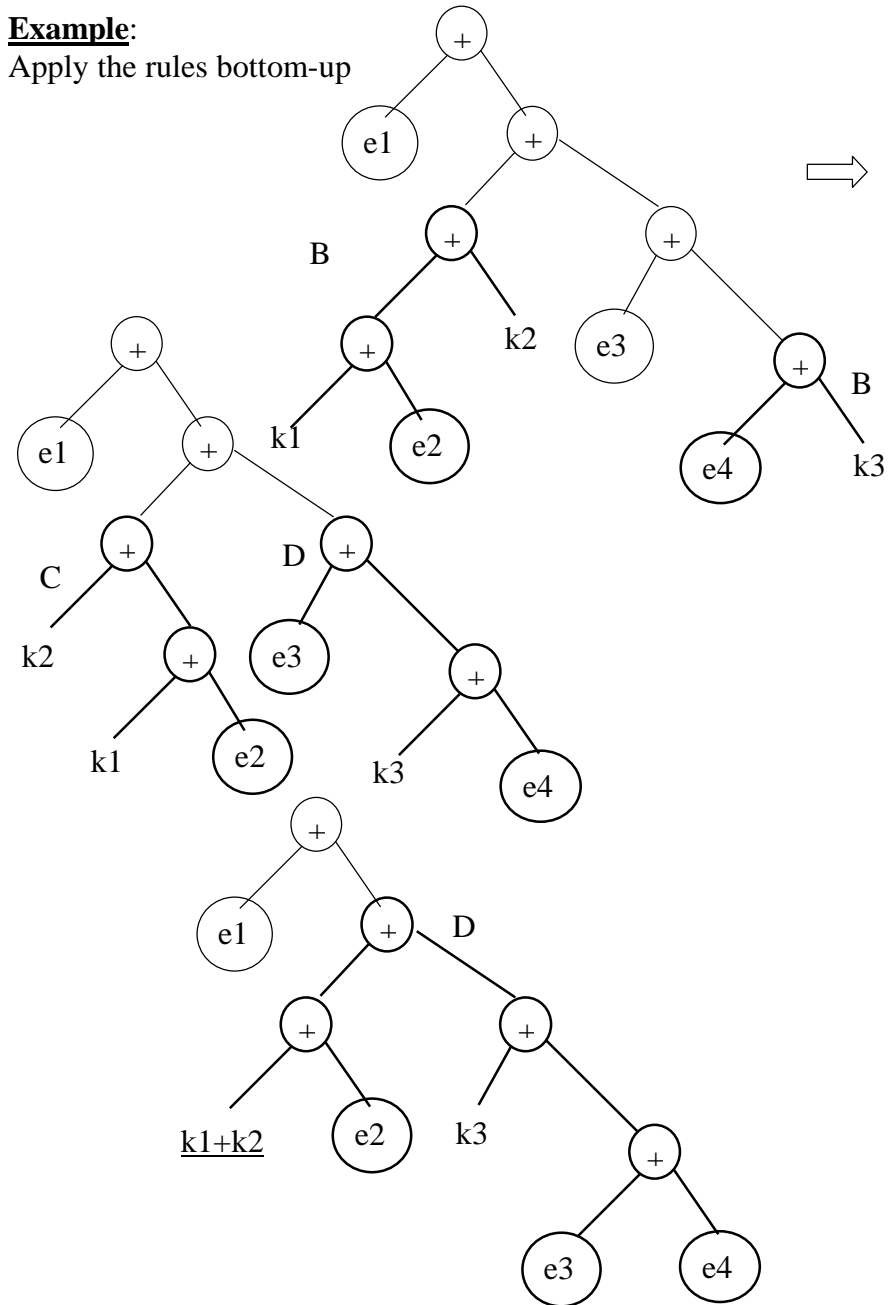
Rewrite-rules exploiting commutative and associative rule for + to compute addition of constants; strategy: move constants to the left/ move constants to the uppermost left operand:



## Simplifying Expressions by Tree-Rewriting

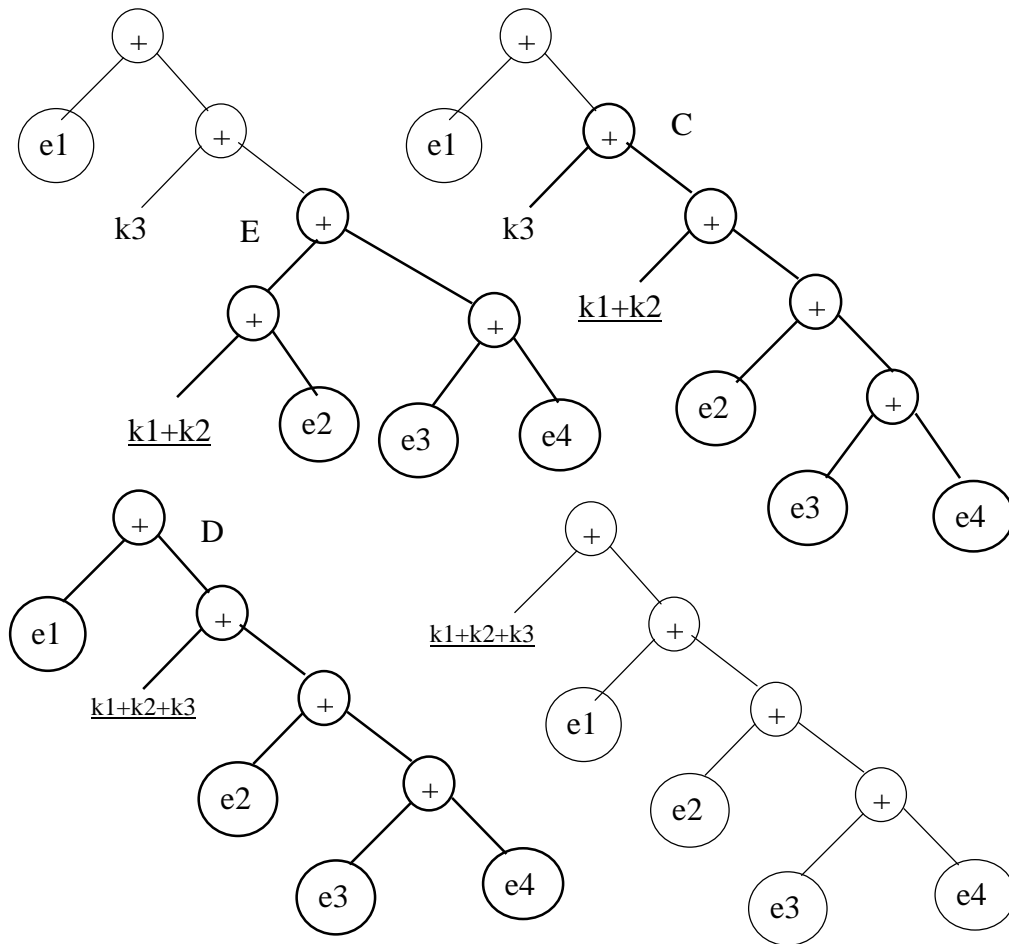
### Example:

Apply the rules bottom-up



## Simplifying Expressions by Tree-Rewriting

**Example:** Apply the rules bottom-up



## Simplifying Expressions/Folding Bin-Expressions

This is an outline of a proposal for simplifying binary expressions. The idea is at each (+,-) level and (\*,/) level to move all constants to the left.

### Splitting

Operator +, - :  $\oplus$   $e1 \oplus e2$

split each operand e1 and e2 into a triple: [constant, operator, optional expr]

operand	triple
$c \oplus e$	[c, $\oplus$ , e]
c	[c, +, nil]
e (all other expr's)	[0, +, e]

Splitting depends on the context operator

Operator \*, / :  $\otimes$   $e1 \otimes e2$

split each operand e1 and e1 into a triple: [constant, operator, optional expr]

operand	triple
$c \otimes e$	[c, $\otimes$ , e]
c	[c, *, nil]
e (all other expr's)	[1, *, e]

### Folding

Simplify/Fold BinExpr(oprt,e1,e2) , oprt  $\in$  {+,-,\*,/}:

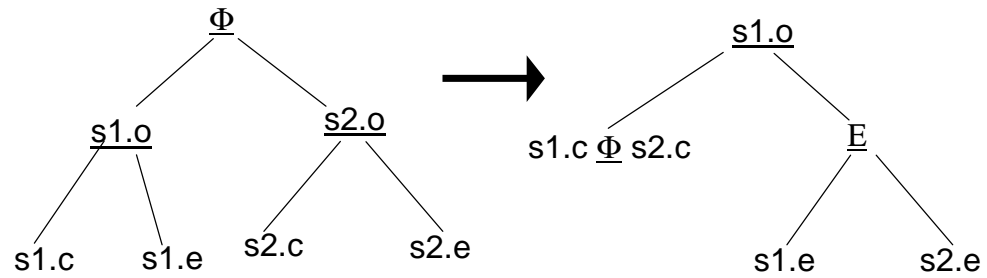
I) fold subexpressions:  $s1 = e1.fold()$  ,  $s2 = e2.fold()$

II) split folded subexpressions

$[s1.c, s1.o, s1.e] = \text{split}(\text{oprt}) s1$  ,  $[s2.c, s2.o, s2.e] = \text{split}(\text{oprt}) s2$

Then construct the simplified/folded expression as shown below for s1.e and s2.e being non-nil expressions.

## Fold BinExpr



$$(s1.c \ \underline{s1.o} \ s1.e) \ \underline{\Phi} \ (s2.c \ \underline{s2.o} \ s2.e) \Rightarrow \\ (s1.c \ \underline{\Phi} \ s2.c) \ \underline{s1.o} \ (s1.e \ \underline{E} \ s2.e)$$

where

$\underline{s1.o}, \underline{s2.o}, \underline{\Phi}, \underline{E} \in \{\text{Plus}, \text{Minus}\} \vee$   
 $\underline{s1.o}, \underline{s2.o}, \underline{\Phi}, \underline{E} \in \{\text{Mult}, \text{Div}\}$

<u>s1.o</u>	<u>Φ</u>	<u>s2.o</u>	<u>E</u>
+	+	+	+
+	+	-	-
+	-	+	-
+	-	-	+
-	+	+	-
-	+	-	+
-	-	+	+
-	-	-	-

Application of the rules  $0+e=e$  and  $1*e=e$  is not shown.