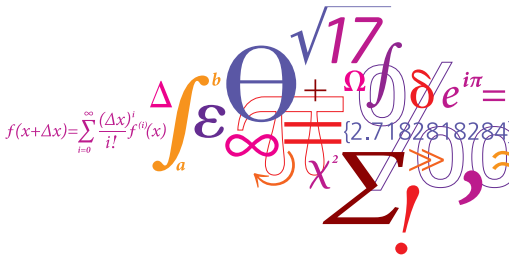


02157 Functional Programming

Lecture 9: Module System – briefly

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- Supports modular program design including
 - encapsulation
 - abstraction and
 - reuse of software components.
- A module is characterized by:
 - a *signature* – an interface specifications and
 - a matching *implementation* – containing declarations of the interface specifications.
- Example based (incomplete) presentation to give the flavor.

Sources:

- Chapter 7: Modules. (A fast reading suffices.)

An example: Search trees

Consider the following implementation of search trees:

```
type tree = Lf
          | Br of tree*int*tree;;
```

```
let rec insert i = function
| Lf          -> Br(Lf,i,Lf)
| Br(t1,j,t2) as tr ->
    match compare i j with
    | 0          -> tr
    | n when n<0 -> Br(insert i t1 , j, t2)
    | _          -> Br(t1,j, insert i t2);;
```

```
let rec memberOf i = function
| Lf          -> false
| Br(t1,j,t2) -> match compare i j with
                  | 0    -> true
                  | n when n<0 -> memberOf i t1
                  | _      -> memberOf i t2;;
```

Is this implementation adequate?

No. Search tree property can be violated by a programmer:

```
toList(insert 2 (Br(Br(Lf,3,Lf), 1, Br(Lf,0,Lf)))));;  
> val it = [3;1;0;2]: int list
```

Solution: Hide the internal structure of search trees.

A **module** is a combination of a

- **signature**, which is a specification of an interface to the module (the user's view), and an
- **implementation**, which provides declarations for the specifications in the signature.

The signature specifies one type and eight values:

```
// Vector signature
module Vector
type vector
val ( ~-. ) : vector -> vector          ;;; Vector sign change
val ( +. ) : vector -> vector -> vector ;;; Vector sum
val ( -. ) : vector -> vector -> vector ;;; Vector difference
val ( *. ) : float -> vector -> vector ;;; Product with number
val ( &. ) : vector -> vector -> float  ;;; Dot product
val norm : vector -> float              ;;; Length of vector
val make : float * float -> vector      ;;; Make vector
val coord : vector -> float * float     ;;; Get coordinates
```

The specification 'vector' does not reveal the implementation

- Why is `make` and `coord` introduced?

An implementation must declare each specification of the signature:

```
// Vector implementation
module Vector
type vector = V of float * float ;;
let (~-.) (V(x,y))           = V(-x,-y) ;;
let (+.) (V(x1,y1)) (V(x2,y2)) = V(x1+x2,y1+y2) ;;
let (-.) v1                v2      = v1 +. -. v2 ;;
let ( *.) a                 (V(x1,y1)) = V(a*x1,a*y1) ;;
let (&.) (V(x1,y1)) (V(x2,y2)) = x1*x2 + y1*y2 ;;
let norm  (V(x1,y1))           = sqrt(x1*x1+y1*y1) ;;
let make  (x,y)                = V(x,y)      ;;
let coord (V(x,y))             = (x,y)       ;;
```

- Since the representation of 'vector' is **hidden in the signature**, the type must be **implemented by either a tagged value or a record**.

Suppose

- the signature is in a file '`Vector.fsi`'
- the implementation is in a file '`Vector.fs`'

A library file '`Vector.dll`' is constructed by the following command:

```
C:\mrh\Kurser\02157-11\Week 10\fsc -a Vector.fsi Vector.fs
```

The library '`Vector`' can now be used just like other libraries, such as '`Set`' or '`Map`'.

A library must be referenced before it can be used.

```
#r @"c:\mrh\Kursen\02157-11\Week 10\Vector.dll";  
--> Referenced 'c:\mrh\Kursen\02157-11\Week 10\Vector.dll'  
open Vector ;;  
  
let a = make(1.0,-2.0);;  
val a : vector  
let b = make(3.0,4.0);;  
val b : vector  
let c = 2.0 *. a -. b;;  
val c : vector  
  
coord c ;;  
val it : float * float = (-1.0, -8.0)  
  
let d = c &. a;;  
val d : float = 15.0  
  
let e = norm b;;  
val e : float = 5.0
```

Notice: the implementation of `vector` is not visible and it cannot be exploited.

A *type augmentation*

- adds declarations to the definition of a tagged type or a record type
- allows declaration of (overloaded) operators.

In the 'Vector' module we would like to

- overload $+$, $-$ and $*$ to also denote **vector** operations.
- overload $*$ is even overloaded to denote two different operations on vectors.

Type augmentation – signature

```
module Vector
```

```
[<Sealed>]
```

```
type vector =
```

```
  static member ( ~- ) : vector -> vector
```

```
  static member ( + ) : vector * vector -> vector
```

```
  static member ( - ) : vector * vector -> vector
```

```
  static member ( * ) : float * vector -> vector
```

```
  static member ( * ) : vector * vector -> float ;;
```

```
val make : float * float -> vector ;;
```

```
val coord: vector -> float * float ;;
```

```
val norm : vector -> float ;;
```

- The *attribute* [`<Sealed>`] is mandatory when a type augmentation is used.
- The “member” specification and declaration of an infix operator (e.g. `+`) correspond to a type of form $type_1 * type_2 \rightarrow type_3$
- The operators can still be used on numbers.

Type augmentation – implementation and use

```

module Vector

type vector =
  | V of float * float
  static member (~-) (V(x,y))           = V(-x,-y)
  static member (+) (V(x1,y1),V(x2,y2)) = V(x1+x2,y1+y2)
  static member (-) (V(x1,y1),V(x2,y2)) = V(x1-x2,y1-y2)
  static member (*) (a, V(x,y))         = V(a*x,a*y)
  static member (*) (V(x1,y1),V(x2,y2)) = x1*x2 + y1*y2 ;;
let make (x,y)      = V(x,y) ;;
let coord (V(x,y)) = (x,y)  ;;
let norm (V(x,y))  = sqrt(x*x + y*y) ;;

```

The operators `+`, `-`, `*` are available on vectors even without opening:

```

let a = Vector.make(1.0,-2.0);;
val a : Vector.vector

let b = Vector.make(3.0,4.0);;
val b : Vector.vector

let c = 2.0 * a - b;;
val c : Vector.vector

```

Customizing the string function

```

module Vector
type vector =
  | V of float * float
  override v.ToString() =
    match v with | V(x,y) -> string(x,y) ;;

let make (x,y)      = V(x,y) ;;
...
type vector with
  static member (~-) (V(x,y))          = V(-x,-y)
  ...

```

- The default ToString function that do not reveal a meaningful value is overridden to give a string for the pair of coordinates.
- A type extension is used.

Example:

```

let a = Vector.make(1.0,2.0);;
val a : Vector.vector = (1, 2)

string(a+a);;
val it : string = "(2, 4)"

```

Modular program development

- program libraries using signatures and structures
- type augmentation, overloaded operators, customizing string (and other) functions
- Encapsulation, abstraction, reuse of components, division of concerns, ...
- ...