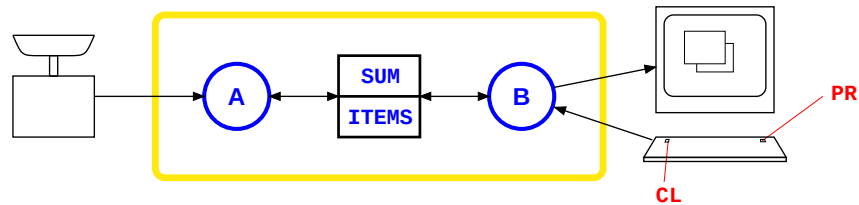


The Sharing Problem



```
process A =  
  loop  
    read w  
    SUM := SUM + w  
    ITEMS := ITEMS + 1  
  end loop
```

```
process B =  
  loop  
    read key  
    case key  
      PR : if ITEMS ≠ 0 then  
        print SUM/ITEMS  
      CL : SUM := 0  
        ITEMS := 0  
    end loop
```

Critical Region Properties

Assumptions

- Critical sections are established with *entry* and *exit protocols*
- A process *eventually leaves* the critical section

Properties

- **Mutual Exclusion** At most one process in a region at a time
- **Obligingness** A lonely process will succeed
[Absence of unnecessary delay]
- **Resolution** One out of several processes will succeed
[Absence of deadlock and livelock]
- **Fairness** Any process will succeed
[Eventual entry]

Critical Regions with Shared Variables

Coarse-grained solution

- **var** *in1, in2* : *bool* := *false*;

```
process P1  
  loop  
     $\langle \neg in2 \rightarrow in1 := true \rangle$ ;  
    critical section1;  
    in1 := false;  
    noncritical section1  
  end loop
```

```
process P2  
  loop  
     $\langle \neg in1 \rightarrow in2 := true \rangle$ ;  
    critical section2;  
    in2 := false;  
    noncritical section2  
  end loop
```

Critical Regions with Shared Variables

Fine-grained attempt I

- **var** *in1, in2* : *bool* := *false*;

```
process P1  
  loop  
    while in2 do skip;  
    in1 := true;  
    critical section1;  
    in1 := false;  
    noncritical section1  
  end loop
```

```
process P2  
  loop  
    while in1 do skip;  
    in2 := true;  
    critical section2;  
    in2 := false;  
    noncritical section2  
  end loop
```

Critical Regions with Shared Variables

Fine-grained attempt II

- **var** *in1, in2* : *bool* := *false*;

```
process P1  
  loop  
    in1 := true;  
    while in2 do skip;  
    critical section1;  
    in1 := false;  
    noncritical section1  
  end loop
```

```
process P2  
  loop  
    in2 := true;  
    while in1 do skip;  
    critical section2;  
    in2 := false;  
    noncritical section2  
  end loop
```

Critical Regions with Shared Variables

Fine-grained attempt III (Back-off)

- **var** *in1, in2* : *bool* := *false*;

```
process P1  
  loop  
    in1 := true;  
    while in2 do { in1 := false;  
                    delay;  
                    in1 := true }  
    critical section1;  
    in1 := false;  
    noncritical section1  
  end loop
```

```
process P2  
  loop  
    in2 := true;  
    while in1 do { in2 := false;  
                    delay;  
                    in2 := true }  
    critical section2;  
    in2 := false;  
    noncritical section2  
  end loop
```

Critical Regions with Shared Variables

Dekker's Algorithm

- **var** $in1, in2 : \text{bool} := \text{false};$
 $turn : \text{int} := 1;$

```
process  $P_1$ 
loop
   $in1 := \text{true};$ 
  while  $in2$  do
    if  $turn = 2$  then
      {  $in1 := \text{false};$ 
        while  $turn = 2$  do skip
           $in1 := \text{true}$ };
      critical section1;
       $in1 := \text{false};$ 
       $turn := 2;$ 
    noncritical section1
  end loop

process  $P_2$ 
loop
   $in2 := \text{true};$ 
  while  $in1$  do
    if  $turn = 1$  then
      {  $in2 := \text{false};$ 
        while  $turn = 1$  do skip
           $in2 := \text{true}$ };
      critical section2;
       $in2 := \text{false};$ 
       $turn := 2;$ 
    noncritical section2
  end loop
```

Critical Regions with Shared Variables

Peterson's Algorithm

- **var** $in1, in2 : \text{bool} := \text{false};$
 $turn : \text{int} := 1;$

```
process  $P_1$ 
loop
   $in1 := \text{true};$ 
   $turn := 2;$ 
  while  $\neg in2 \wedge turn = 2$  do skip;
  critical section1;
   $in1 := \text{false};$ 
  noncritical section1
end loop

process  $P_2$ 
loop
   $in2 := \text{true};$ 
   $turn := 1;$ 
  while  $\neg in1 \wedge turn = 1$  do skip;
  critical section2;
   $in2 := \text{false};$ 
  noncritical section2
end loop
```

Critical Regions with Shared Variables

Test-and-Set Solution

- Let $TS(\text{var } l) = \langle \text{var } r : \text{bool}; (r, l) := (l, \text{true}); \text{return } r \rangle$
- $\text{var } lock : \text{bool} := \text{false};$

<pre>process P_1 loop while $TS(lock)$ do skip; critical section₁; lock := false; noncritical section₁ end loop</pre>	<pre>process P_2 loop while $TS(lock)$ do skip; critical section₂; lock := false; noncritical section₂ end loop</pre>
---	---

Critical Regions with Shared Variables

Test-and-Set Solution

- Let $TS(\text{var } l) = \langle \text{var } r : \text{bool}; (r, l) := (l, \text{true}); \text{return } r \rangle$
- $\text{var } lock : \text{bool} := \text{false};$

```
process  $P[i : 1..n]$ 
  loop
    while  $TS(lock)$  do skip;
    critical sectioni;
    lock := false;
    noncritical sectioni;
  end loop
```

Critical Regions with Shared Variables

Test-and-Test-and-Set Solution

- Let $TS(\text{var } l) = \langle \text{var } r : \text{bool}; (r, l) := (l, \text{true}); \text{return } r \rangle$
- **var** $lock : \text{bool} := \text{false};$
process $P[i : 1..n]$
 loop
 while $lock$ **do skip;**
 while $TS(lock)$ **do**
 while $lock$ **do skip;**
 critical section _{i} ;
 $lock := \text{false};$
 noncritical section _{i}
 end loop

Critical Regions with Shared Variables

Ticket Algorithm

- **var** $number, next : \text{integer} := 1;$
 $turn[i : 1..n] : \text{integer} := 0;$
process $P[i : 1..n]$
 loop
 $\langle turn_i := number; number := number + 1 \rangle;$
 $\langle \text{await } turn_i = next \rangle;$
 critical section _{i} ;
 $\langle next := next + 1 \rangle;$
 noncritical section _{i} ;
 end loop

Invariant

- $next > 0 \wedge$
 $\forall i: turn_i < number \wedge$
 $(in\ crit_i \Rightarrow turn_i = next) \wedge$
 $(turn_i > 0 \Rightarrow \forall j \neq i: turn_i \neq turn_j)$