

# Model Checking

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Kim Guldstrand  
Larsen



BRICS

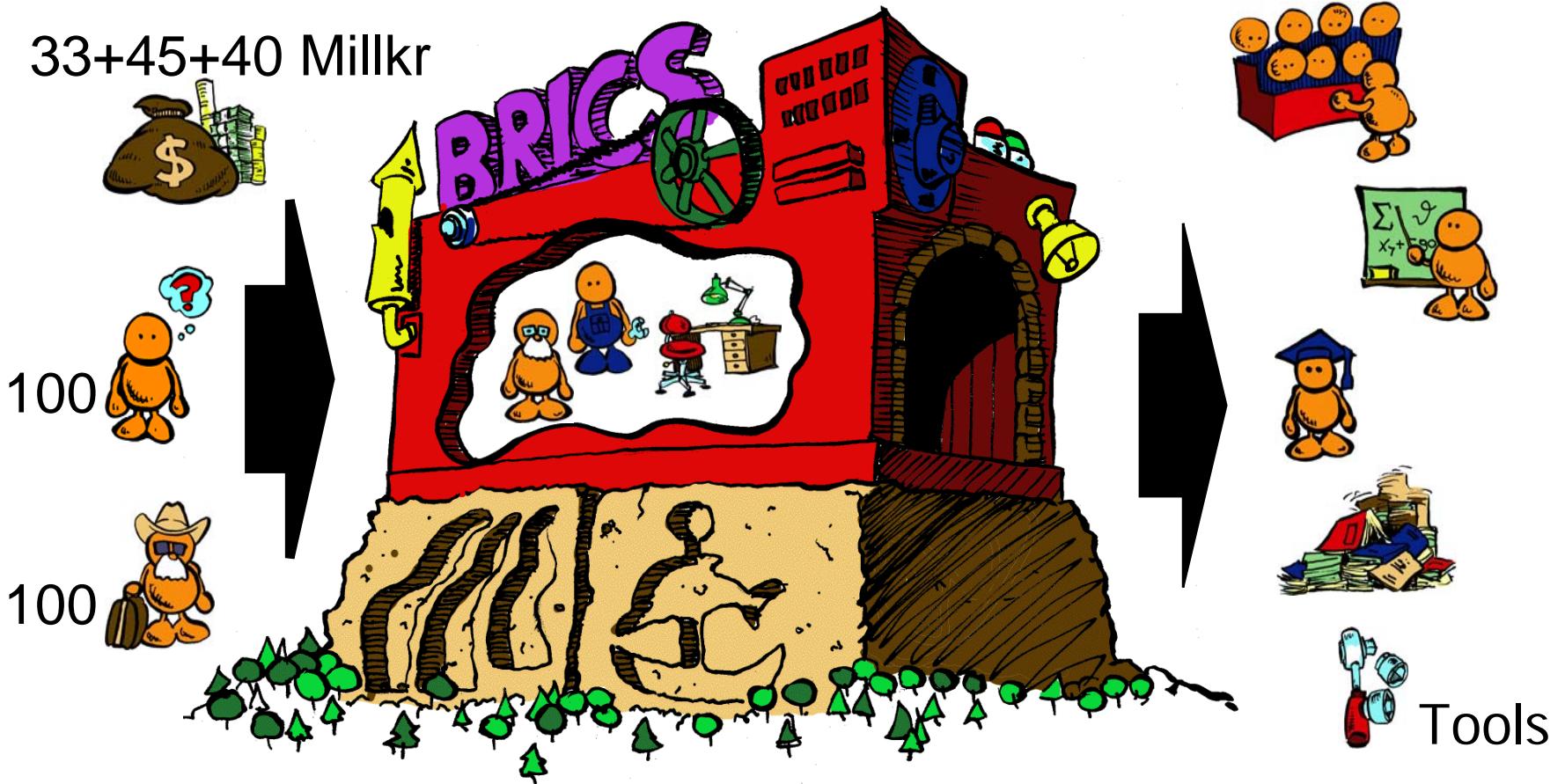
Basic Research  
in Computer Science



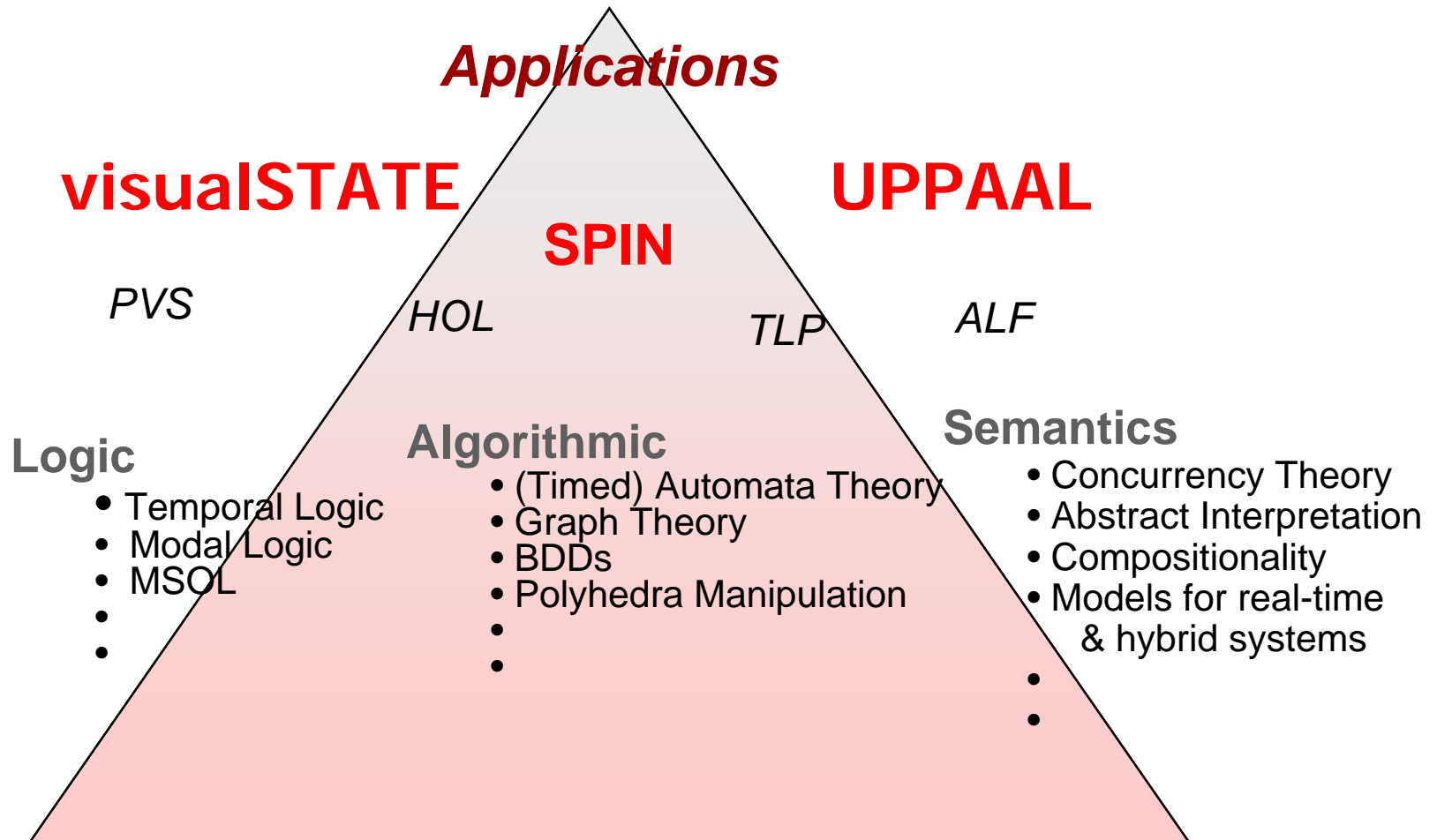
CENTER FOR INDLEJREDE SOFTWARE SYSTEMER

# BRICS Machine

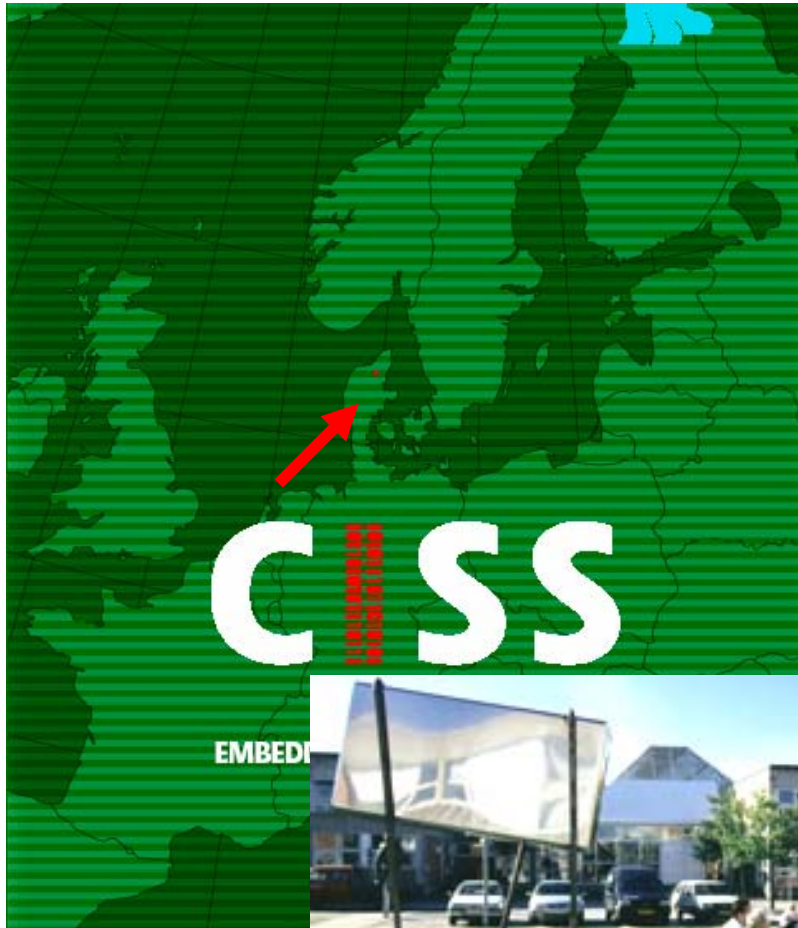
Basic Research in Computer Science, 1993-2006



# Tools and BRICS



# **CISS:** *Center for Embedded Software Systems*



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or

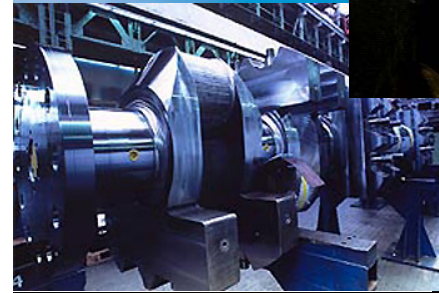
**CISS**  
[www.ciss.dk](http://www.ciss.dk)  
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# Why CISS ?

- 80% of all software is embedded
- Demands for **increased functionality** with **minimal resources**
- Requires multitude of skills
  - Software construction
  - hardware platforms,
  - communication
  - testing & verification
- **Goal:**  
 Give a qualitative lift to current industrial practice  
 !!!!!



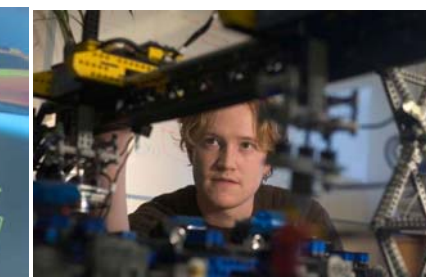
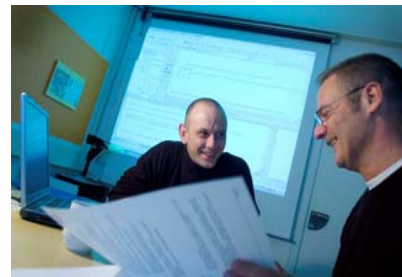
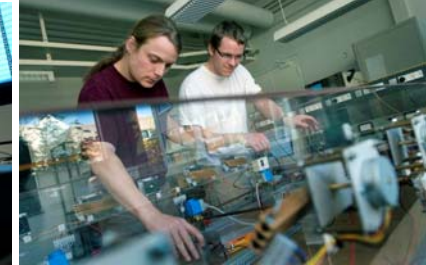


# CISS in Numbers

- Jutland-Fun IT-initiative, 2002:

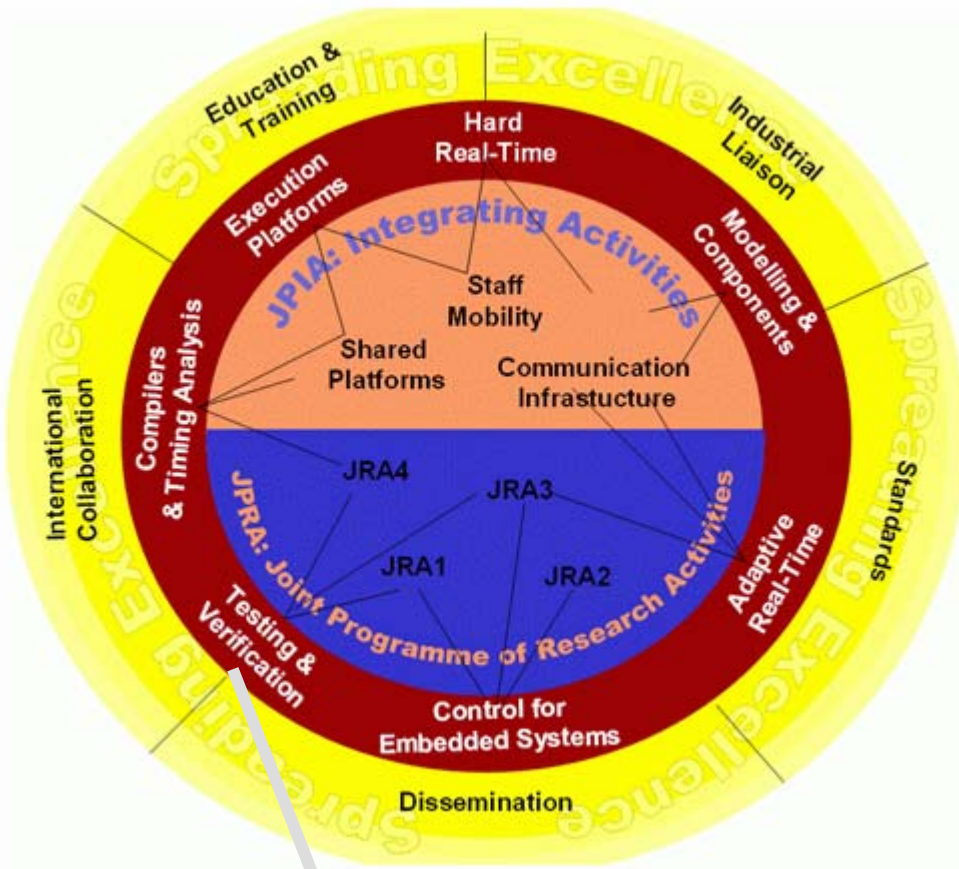
**25,5** mil. kr Ministry  
**6** mil. kr North Jutland  
**6** mil. kr Aalborg City  
**12,75** mil. kr Companies  
**12,75** mil. kr AAU

- **26** projects
- **20** CISS employees
- **25** CISS associated researcher at 3 different research groups at AAU
  
- **16** industrial PhDs



# ARTIST2 European Network of Excellence

6,5MEuro, 32 partners

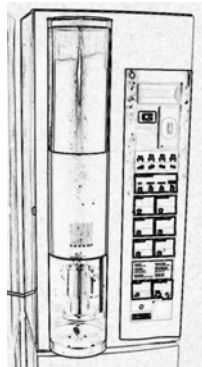


EU's 7<sup>th</sup> Framework  
 →  
 ARTEMIS Research Platform  
 →  
 Centers of Excellence

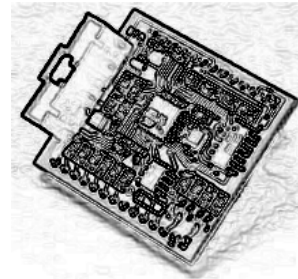
**Testing & Verification**  
**CISS koordinator**

# Modelling Checking

**Plant**  
*Continuous*



**Controller Program**  
*Discrete*



sensors

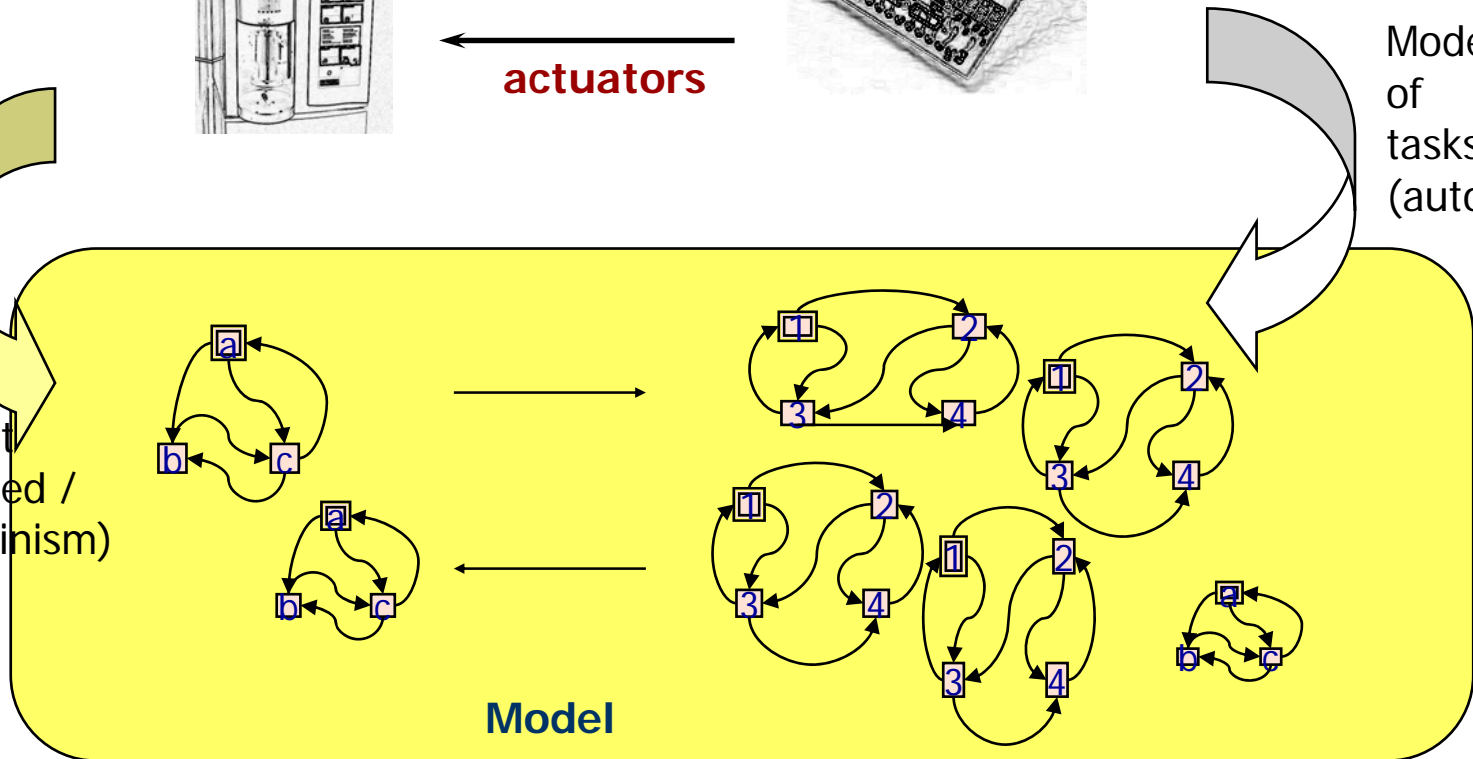


actuators



Model  
of  
tasks  
(automatic?)

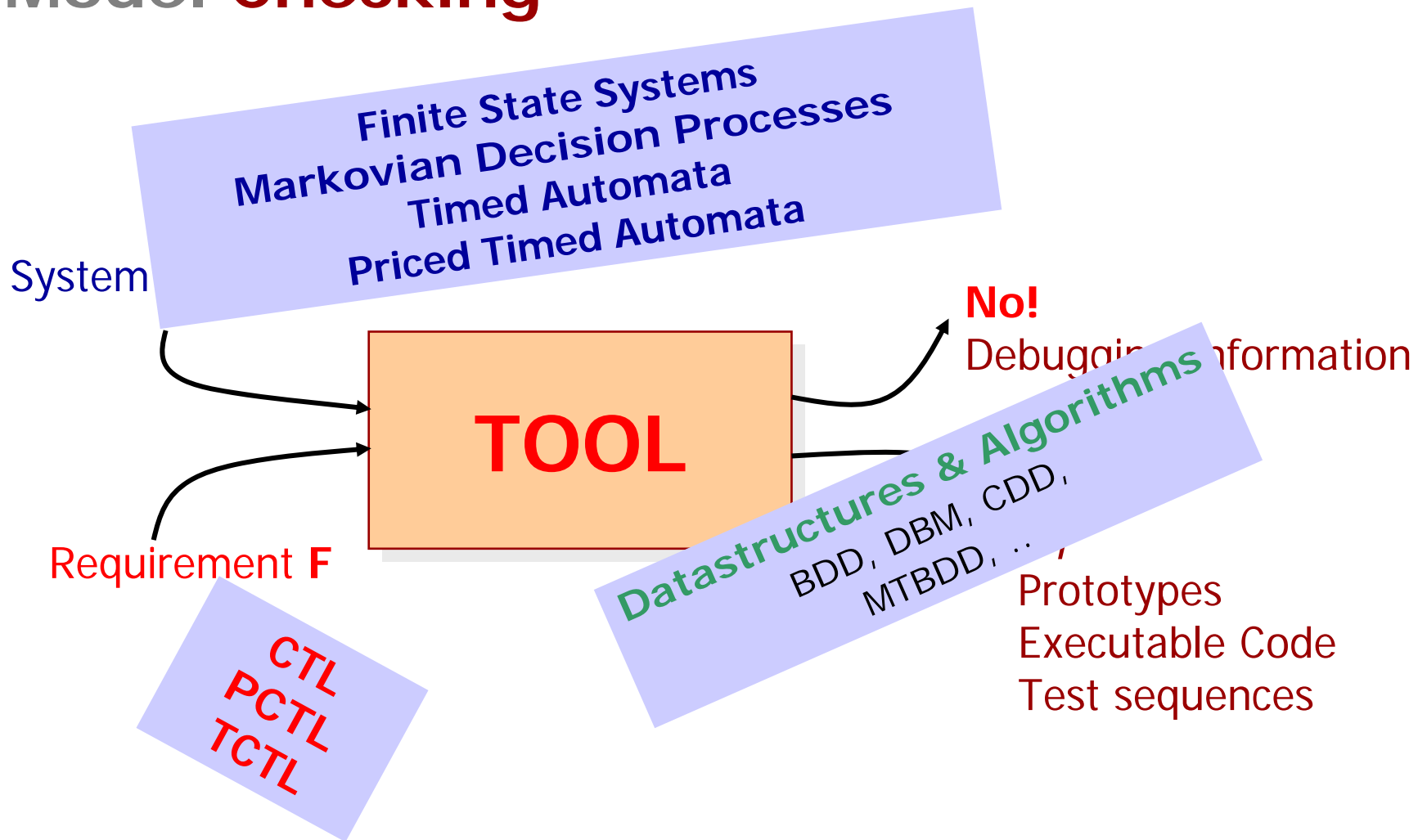
Model  
of  
environment  
(user-supplied /  
non-determinism)



**Model**



# Model Checking



**Tools:** UPPAAL, visualSTATE, PRISM, RAPTURE, SPIN, Statemate, Verilog, Formalcheck,...

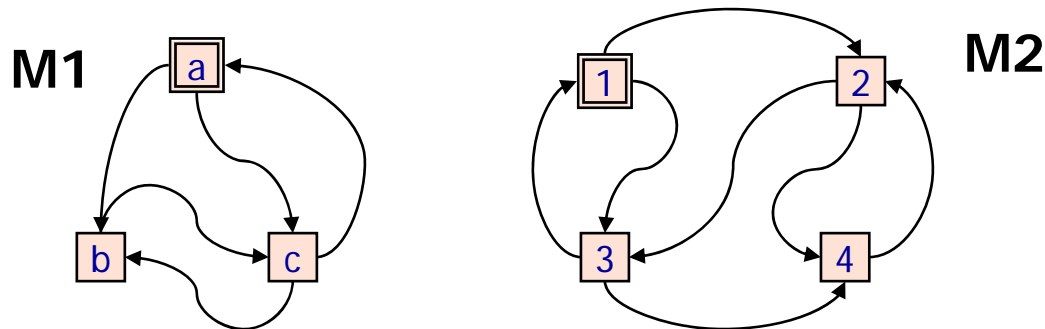
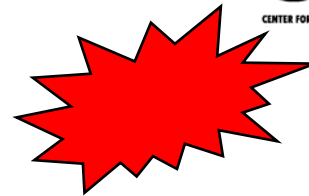
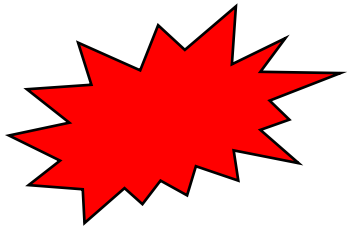
# Benefits of Model Checking

- General Verification approach (hardware, embedded systems, software)
- Support of partial verification.
- Insensitive to likelihood of error (in contrast to testing).
- Provision of diagnostic information
- Push-button technology
- Rapidly increasing interest by industry (in particular hardware and embedded systems).
- Shorten development time.
- Easily integrated in existing development cycle.
- Not too steep learning curve.
- Sound and mathematical underpinning.

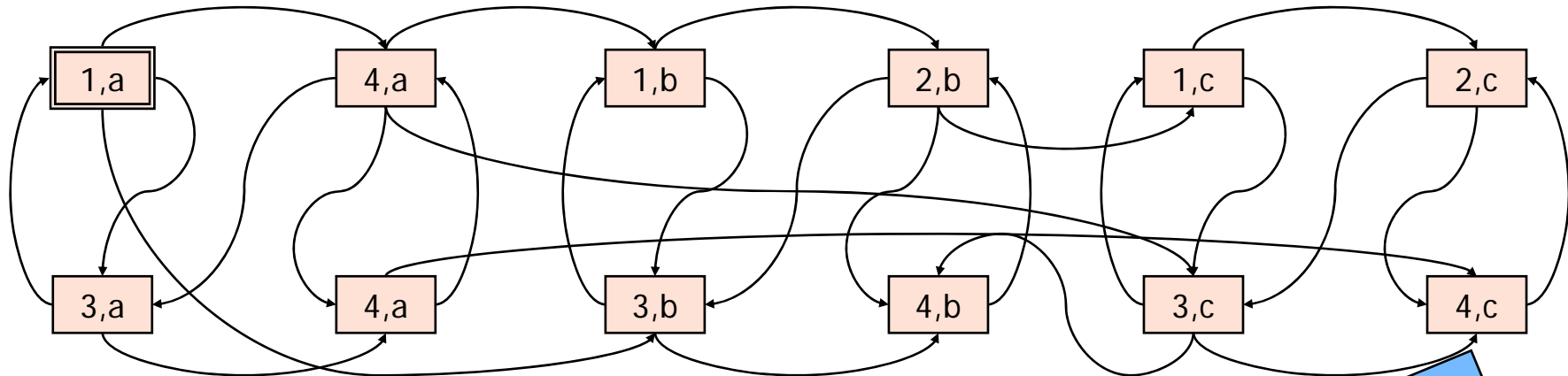
# Weaknesses of Model Checking

- Mainly appropriate to control-intensive and less to data-intensive applications.
- Limited by decidability issues.
- Verification of *system model* and not actual system.
- Only check for *stated properties*.
- Suffers from *state-explosion*.
- Requires expertise in finding appropriate abstractions and requirements.
- Model checkers may themselves have bugs.
- Verification of instances with specific parameters and no. of components.

# 'State Explosion' Problem



**M1 x M2**



**All combinations:  
 exponential in no. of components**

**Provably theoretical  
 intractable**

# Overview (Day 1)

## ■ Finite State Model Checking

- Kripke Structures
- CTL: Computational Tree Logic
- Explicit Model Checking Algorithms

## ■ Symbolic Model Checking

- Binary Decision Diagrams
- Symbolic Model Checking of CTL
- Compositional Backwards Reachability

## ■ Probabilistic Model Checking

- Discrete Time Markov Chains & Decision Processes
- Probabilistic Reachability
- Probabilistic CTL
- Abstraction/Refinement



# Overview (Day 2)

- **Real Time Model Checking**
  - Timed Automata
  - Timed CTL
- **Symbolic Real Time Model Checking**
  - Regions and Zones
  - Symbolic Reachability Checking
  - Symbolic Liveness Checking
- **Further Optimizations**
  - Abstractions & Approximate Analyses
  - Modelling Patterns
  - ...
- **Optimal Scheduling using Model Checking**
  - Priced Timed Automata, Priced Zones
  - Optimal Reachability
  - Optimal Safety

# Reading Material

- Consult CAV'06: "25 Years of Model Checking".
- R. Bryant: *Symbolic Boolean Manipulation with Ordered Binary Decision-Diagrams*. ACM Computing Surveys, Vol. 24, No. 3 September 1992.
- Jørgen Staunstrup, Henrik Reif Andersen, Kim G. Larsen, Henrik Leerberg, Niels Bo Theilgaard et al.: *Practical Verification of Embedded Software*. IEEE Computer May 2000.
- J.L-Nielsen, G. Behrmann, H. R. Andersn, H. Hulgaard, K. Kristoffers, K.G. Larsen: *Verification of Large State/Event Systems Using Compositionality and Dependency Analysis*. Formal Methods in System Design, 18, 5–23, 2001
- H.Hansson, B.Jonsson: *A Logic for Reasoning about Time and Reliability*. Formal Aspects of Computing (1994) 6: 512-535.

# Reading Material

- G. Behrmann, A. David, K.G. Larsen: *Tutorial on UPPAAL* (see [www.uppaal.com](http://www.uppaal.com))
- J. Bengtsson, W. Yi: *Timed Automata: Semantics, Algorithm and Tools*. (see [www.uppaal.com](http://www.uppaal.com)).
- G. Behrmann, K. G. Larsen, J. I. Rasmussen: *Optimal Scheduling Using Priced Timed Automata*. ACM SIGMETRICS Performance Evaluation Review, vol. 32, nb. 4, 2005, pp. 34-40, ACM Press.
  
- BOOKS:
  - *Model Checking* by Ed Clarke, Orna Grumberg, Doron Peled
  - *Systems and Software Verification* by B. Berard, M. Bidoit, A. Finkel, F. Laroussinie, A. Petit, L. Petrucci, P. Schnoebelen
  - *Reactive Systems: Modelling, Specification and Verification* by L. Aceto, A. Ingólfssdóttir, K.G. Larsen, J. Srba  
coming soon at a book-store near you.